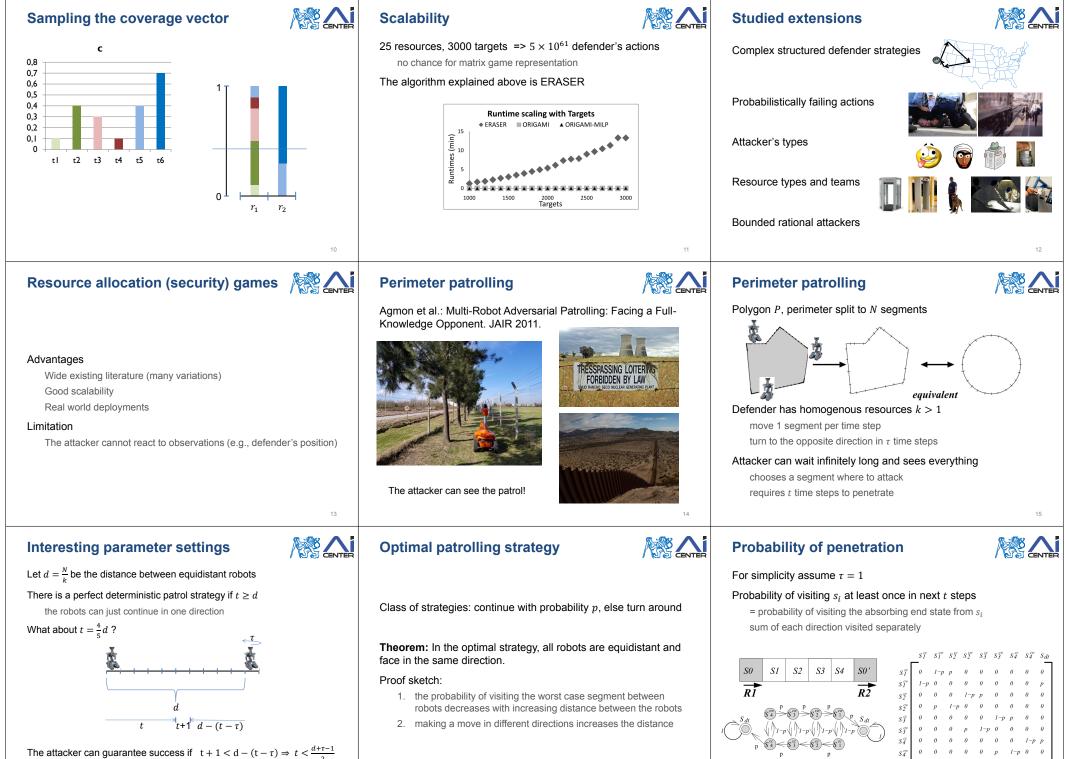


NE: (U,L) -> 4; Pure SE: (D,R) -> 5; Mixed SE ~ 5.5



Probability of penetration



Algorithm 1 Algorithm FindFunc(d, t)1: Create matrix M of size (2d+1)(2d+1), initialized with 0s 2: Fill out all entries in M as follows: 3: M[2d+1, 2d+1] = 14: for $i \leftarrow 1$ to 2d do 5: $M[i, \max\{i+1, 2d+1\}] = p$ $M[i, \min\{1, i-2\}] = 1-p$ 7: Compute $MT = M^t$ 8: Res = vector of size d initialized with 0s 9: for 1 < loc < d do V = vector of size 2d + 1 initialized with 0s. 10: $V[2loc] \leftarrow 1$ 11: 12: $Res[loc] = V \times MT[2d+1]$

13: Return Res

All computations are symbolic. The result are functions $ppd_i: [0,1] \rightarrow [0,1]$ expressing the probability of penetration at *i* for a given probability of turn.

Area patrolling

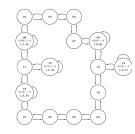
Basilico et al.: Patrolling security games: Definition and algorithms for solving large instances with single patroller and single intruder. AIJ 2012.



Scaling up

25

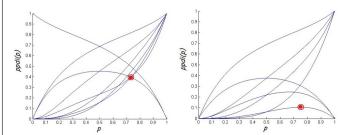
No need to visits nodes not on shortest paths between targets With multiple shortest paths, only the closer to targets is relevant It is suboptimal to stay at a node that is not a target



Optimal turn probability

Maximin value for p

Each line represents one segment (ppd_i)



Iterate all pairs of intersection and maximal points to find solution it is all polynomials

Area patrolling - Formal model

GT can be applied to real world problems in robotics

AI (GT) problems can often be solved by transformation to

Environment represented as a graph

Targets $T = \{6, 8, 12, 14, 18\}$

Penetration time d(t)

 $(v_d(t), v_a(t))$

Defender: Markov policy Attacker: wait. attack(t)

Pursuit-evasion games

Patrolling

Perfect information capture

Visibility-based tracking

resource allocation perimeter patrolling

area patrolling

mathematical programming

Target values

Summary



Solving zero-sum patrolling game

We assume $\forall t \in T : v_a(t) = v_d(t)$



21

$$\begin{split} a(i,j) &= 1 \text{ if the patrol can move form } i \text{ to } j \text{ in one step; else 0} \\ P_{c}(t,h) \text{ is the probability of stopping an attack at target } t \text{ started when the patrol was at node } h \\ \gamma_{i,j}^{w,t} \text{ is the probability that the patrol reaches node } j \text{ from } i \text{ in } w \text{ steps without visiting target } t \\ \max u \\ \alpha_{i,j} &\geq 0 \quad \forall i, j \in V \\ \sum_{j \in V} \alpha_{i,j} = 1 \quad \forall i \in V \\ u_{d}(x) = \left\{ \sum_{l \in T} v_{d}(i), \quad x = \text{intruder-capture or no-attack} \\ \alpha_{i,j} &\leq a(i, j) \quad \forall i, j \in V \\ \gamma_{i,j}^{1,t} = \alpha_{i,j} \quad \forall t \in T, i, j \in V \setminus \{t\} \\ \gamma_{i,j}^{w,t} = \sum_{x \in V \setminus \{t\}} (\gamma_{i,x}^{w-1,t} \alpha_{x,j}) \quad \forall w \in \{2, \ldots, d(t)\}, t \in T, i, j \in V \setminus \{t\} \\ P_{c}(t,h) = 1 - \sum_{j \in V \setminus \{t\}} \gamma_{h,j}^{d(t),t} \quad \forall t \in T, h \in V \\ u \leq u_{d}(\text{intruder-capture})P_{c}(t,h) + u_{d}(\text{penetration-t})(1 - P_{c}(t,h)) \\ \text{What type of optimization problem is this? LP? MILP? Convex?} 24 \end{split}$$

Resources

Kiekintveld, C., Jain, M., Tsai, J., Pita, J., Ordóñez, F. and Tambe, M. "Computing optimal randomized resource allocations for massive security games." AAMAS 2009.

Agmon, Noa, Gal A. Kaminka, and Sarit Kraus. "Multi-robot adversarial patrolling: facing a full-knowledge opponent." Journal of Artificial Intelligence Research 42 (2011): 887-916.

Basilico, Nicola, Nicola Gatti, and Francesco Amigoni. "Patrolling security games: Definition and algorithms for solving large instances with single patroller and single intruder." Artificial Intelligence 184 (2012): 78-123.



Perimeter patrol – summary

Split the perimeter to segments traversable in unit time

Continue with probability p turn around with probability (1-p)

Distribute patrollers uniformly along the perimeter

Coordinate them to always face the same way



26