



Classification

Daniel Novák

20.12, 2018, Prague

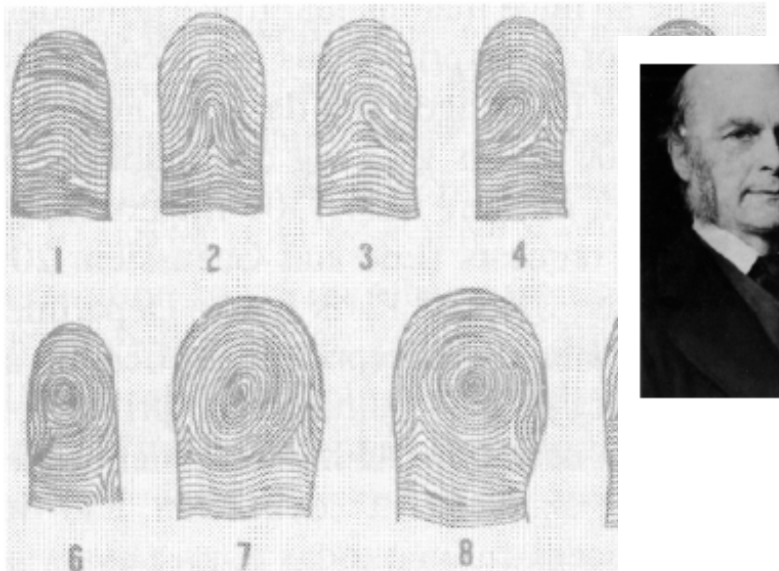
**Acknowledgments: Xavier Palathingal, Andrzej Drygajlo,
Handbook of Fingerprint Recognition**





History

- In 1823, **Purkinji** proposed the first fingerprint classification, which classified into nine categories: (transverse curve, central longitudinal stria, oblique stripe, oblique loop, almond whorl, spiral whorl, ellipse, circle, and double whorl)
- **Sir Francis Galton** introduced the minutae features for fingerprint matching in late 19th century



MR. FRANCIS GALTON'S ANTHROPOMETRIC LABORATORY.

The Laboratory communicates with the "Western Gallery" in which the Scientific Collections of the South Kensington Museum are contained. The Western Gallery runs parallel to Queen's Gate, and is entered either from Queen's Gate or from the new Imperial Institute Road. The latter entrance is close to the Laboratory. Admission is free.

Date of Measurement.			Initials.	Birth-day.			Eye Color.	Sex.	Single, Married, or Widowed?	Page of Register.
Day.	Month.	Year.		Day.	Month.	Year.				
20	12	89	J. H. S.	22	2	70	Brown Grey	m	S	2310
Heel length, maximum	Heel breadth, maximum.	Height, standing, less heels of shoes.	Span of arms from opposite finger tips.	Weight in ordinary clothing.	Strength of grasp.	Breathing capacity.		Kernson of Eyesight.		Color Vision.
Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	lbs.	lbs.	lbs.	Cubic inches.	Inches.	Inches.	No. of Type ? Normal.
7.3	5 9/2	66.6	67	7 1/2	93	88	200	19	19.	56 Yes
Height sitting above seat of chair.	Height of top of knee, when sitting, less heels.	Length, elbow to finger tip, left arm.	Length of middle finger of left hand.	Kernson of hearing.	Height audible area, (by whistle)	Reaction time.		Left Thumb.		Right Thumb.
Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	? Normal.	Vibrations per second.	Headwidths of a second.	To right.	To second.		
85.5	20	7 1/2	4 5	Yes	21,000	15	15			

One page of the Register is assigned to each person measured, in which his measurements at successive periods are entered in successive lines. No names appear on the Register. Copies of the entries can be obtained through application of the persons measured, or by their representatives, under such conditions and restrictions as may be fixed from time to time.

Classes



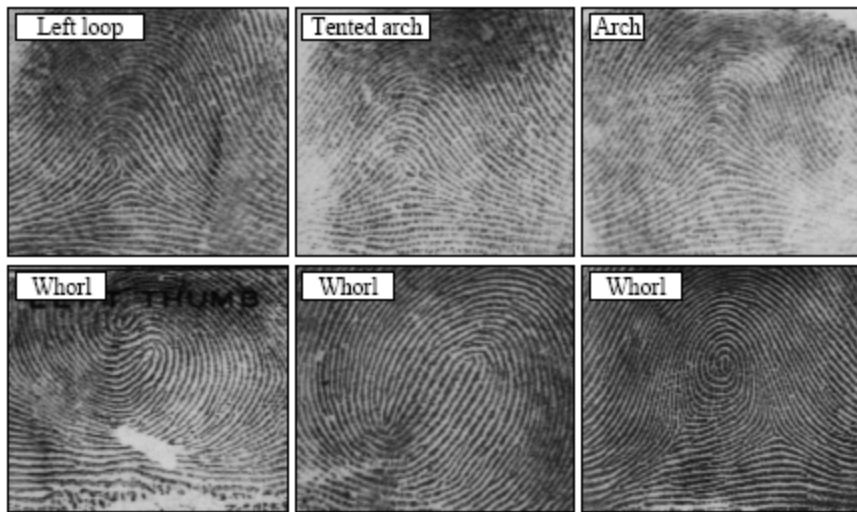
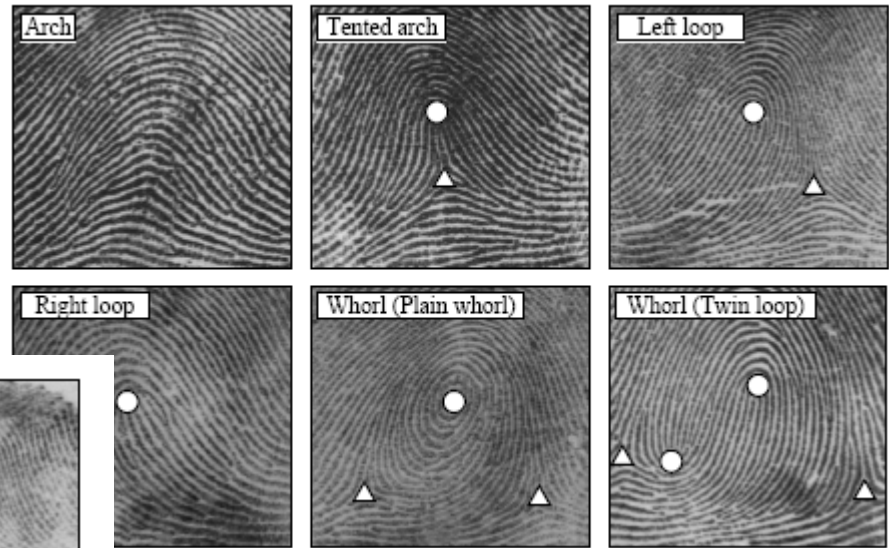
– Arch: 3.7%, tented arch: 2.9%, left loop: 33.8%, right loop: 31.7%, whorl: 27.9%

– Pattern recognition

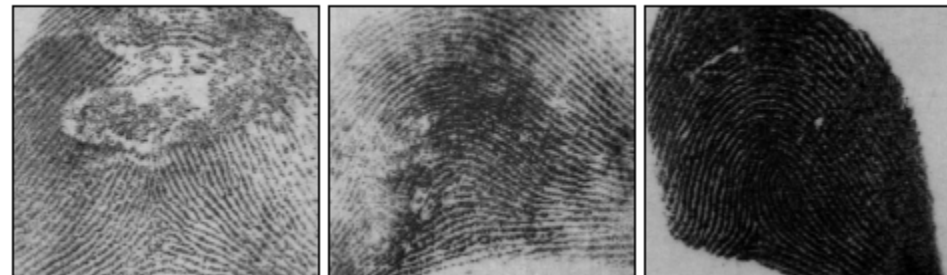
PROBLEM

Small-inter class variability

Large intra-class variability

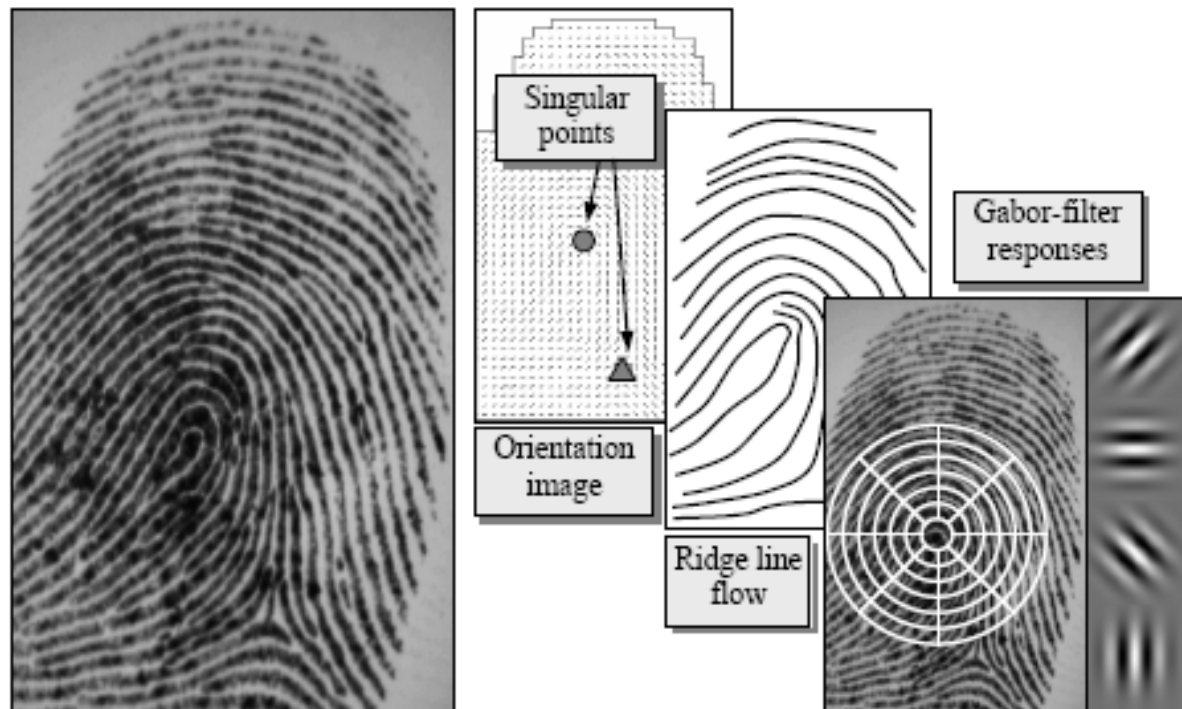


presence of noise



Features

- Based on global features
- Ridge line flow, orientation image, singular point, Gabor filters
- A-priori information: sex, race, age.



Techniques



- Features:
 - O = orientation image
 - S = singularities
 - R = ridge flow,
 - G = Gabor
- classification technique
 - Rb = rule-based
 - Sy = syntactic
 - Str = structural,
 - Sta = statistical
 - Nn = neural network
 - Mc = multiple classifiers

Fingerprint classification approach	Features				Classifier					
	O	S	R	G	Rb	Sy	Str	Sta	Nn	Mc
Moayer and Fu (1975)	√					√				
Moayer and Fu (1976)	√					√				
Rao and Balck (1980)	√					√				
Kawagoe and Tojo (1984)		√	√		√					
Hughes and Green (1991)	√								√	
Bowen (1992)	√	√							√	
Kamijo, Mieno, and Kojima (1992)	√								√	
Kamijo (1993)	√								√	
Moscinska and Tyma (1993)	√				√				√	
Wilson, Candela, and Watson (1994)	√								√	
Candela et al. (1995)	√		√		√				√	√
Omidvar, Blue, and Wilson (1995)	√								√	
Halici and Ongun (1996)	√								√	
Karu and Jain (1996)		√			√					
Maio and Maltoni (1996)	√						√			
Ballan, Sakarya, and Evans (1997)		√			√					
Chong et al. (1997)			√		√					
Senior (1997)			√				√			
Wei, Yuan, and Jie (1998)	√				√				√	√
Cappelli et al. (1999)	√						√			
Cappelli, Maio, and Maltoni (1999)	√							√		
Hong and Jain (1999)		√	√		√					√
Jain, Prabhakar, and Hong (1999)				√				√	√	√
Lumini, Maio, and Maltoni (1999)	√						√			
Cappelli, Maio, and Maltoni (2000a)	√							√		√
Cho et al. (2000)		√			√					
Bartesaghi, Fernández, and Gómez (2001)		√			√					
Bernard et al. (2001)	√								√	
Marcialis, Roli, and Frasconi (2001)	√			√			√	√	√	√
Pattichis et al. (2001)	√				√				√	√
Senior (2001)	√		√		√		√		√	√
Yao, Frasconi, and Pontil (2001)				√				√		√
Cappelli, Maio, and Maltoni (2002a)	√							√		√
Jain and Minut (2002)			√		√					
Cappelli et al. (2003)	√							√		√
Yao et al. (2003)	√			√			√	√	√	√

Overview



Fingerprint classification approach	Features				Classifier					
	O	S	R	G	Rb	Sy	Str	Sta	Nn	Mc
Cappelli and Maio (2004)	√							√		√
Klimanee and Nguyen (2004)	√	√			√					
Senior and Bolle (2004)	√		√		√		√		√	√
Shah and Sastry (2004)								√	√	√
Wang and Xie (2004)	√	√	√		√					
Zhang and Yan (2004)	√	√	√		√					
Park and Park (2005)	√							√		
Neuhaus and Bunke (2005)	√						√			
Tan, Bhanu, and Lin (2005)	√							√		
Min, Hong, and Cho (2006)				√				√		√
Kristensen, Borthen, and Fyllingsnes (2007)				√					√	
Wang and Dai (2007)	√	√			√					
Hong et al. (2008)	√	√		√				√		√
Li, Yau, and Wang (2008)	√	√						√		



Syntactic & Structural approach

- Syntactic: terminal symbols & production rules, [nice source](#)

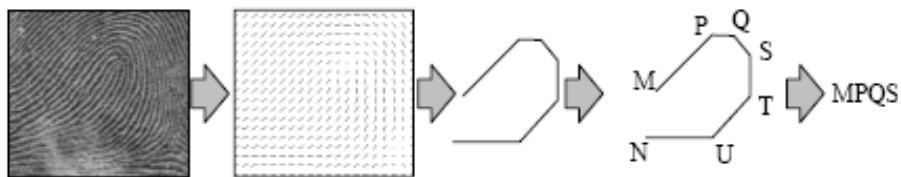
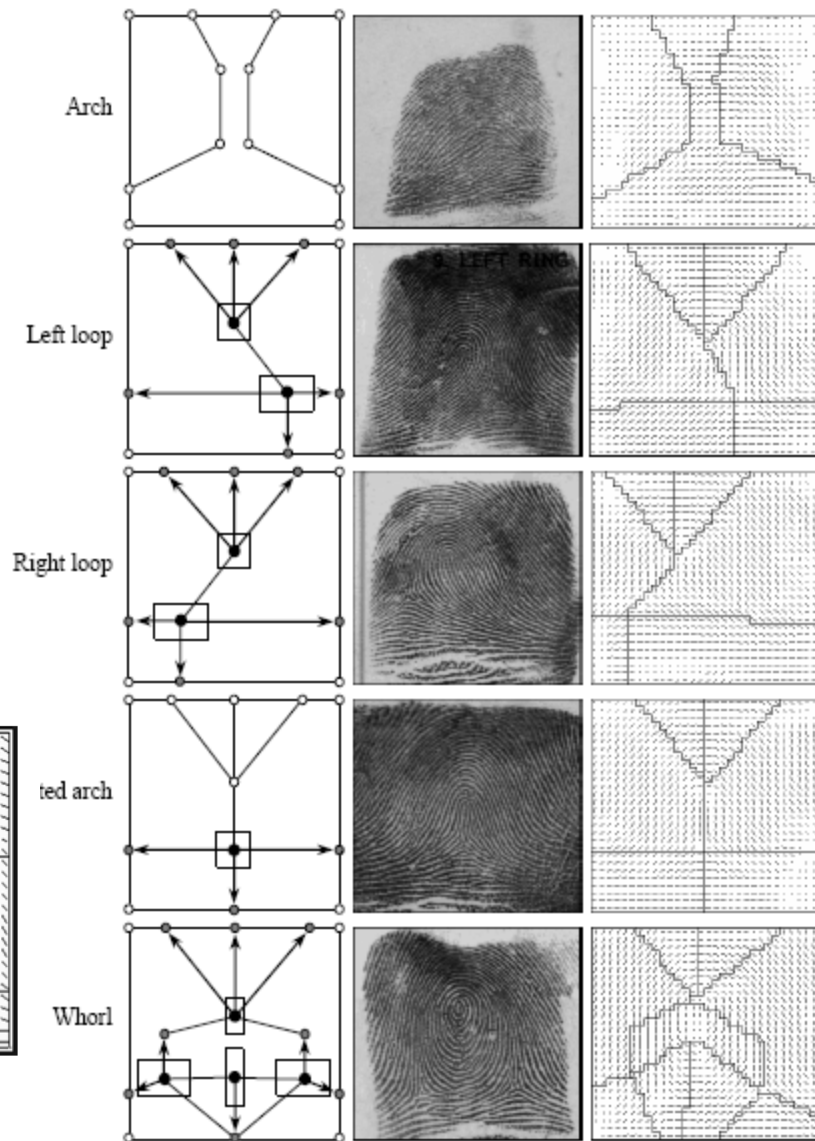
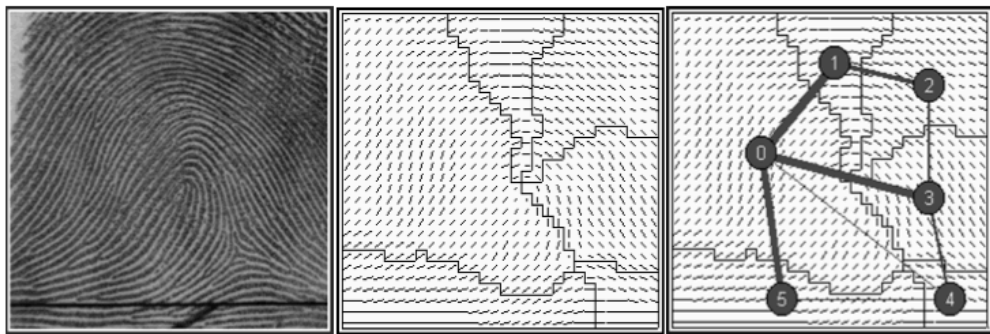


Figure 5.7. A schema of the string-construction approach in Rao and Balck (1986)

- Structural approach
- COST fce-> minimizing variation of orientation



Statistical approach



- Statistical
 - Orientation image
 - k-nearest neighbor
 - 30x30 array, 1800 elements, training impossible, high dimension
 - PCA (the Karhunen-Loeve) transform

$$\mathbf{d} = [r \cdot \cos(2\theta), r \cdot \sin(2\theta)].$$

- Another examples: Bayes decision rule, Support Vector Machine
- Neural networks
 - orientation image
 - multilayer perceptron





Multiple approach I

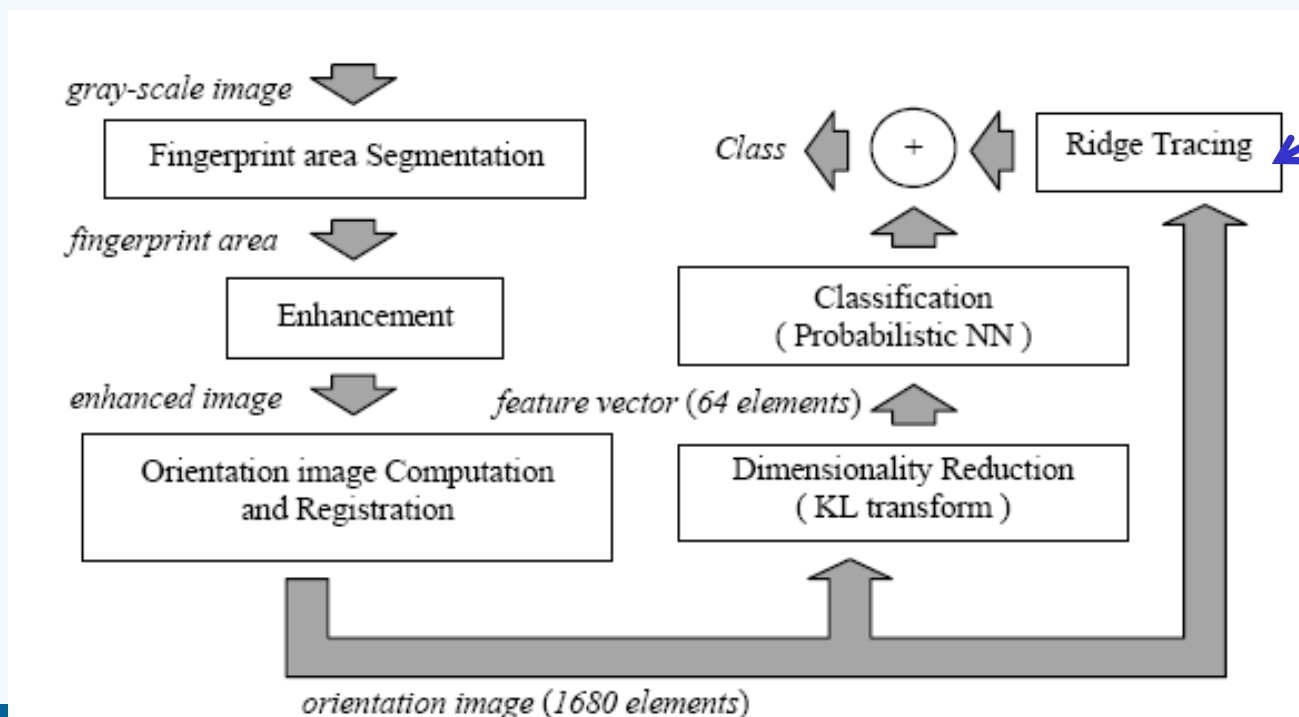
	Distinct features	Distinct classifiers	Distinct training sets	Combination strategy
Candela et al. (1995)	Yes	Yes	No	Rule-based
Jain, Prabhakar, and Hong (1999)	No	Yes	No	Sequential (two stages)
Cappelli, Maio, and Maltoni (2000a)	No	Yes	Yes	Majority vote rule
Senior (2001)	Yes	Yes	No	Neural network
Marcialis, Roli, and Frasconi (2001)	Yes	Yes	No	k-nearest neighbor
Yao et al. (2003)	Yes	Yes	No	k-nearest neighbor
Cappelli et al. (2003)	No	Yes	No	Sequential (two stages)
Shah and Sastry (2004)	Yes	Yes	No	Sequential (two stages)
Hong et al. (2008)	Yes	Yes	No	Bayes rule



Multiply approach II

- Multiple classifier-based approaches
- PCASYS: Pattern-level Classification Automation system
- Open Source: <http://ffpis.sourceforge.net/>
- Developed by NIST: <http://www.nist.gov/index.html>
 - National Institute of Standards and Technology

**Whorl
module**

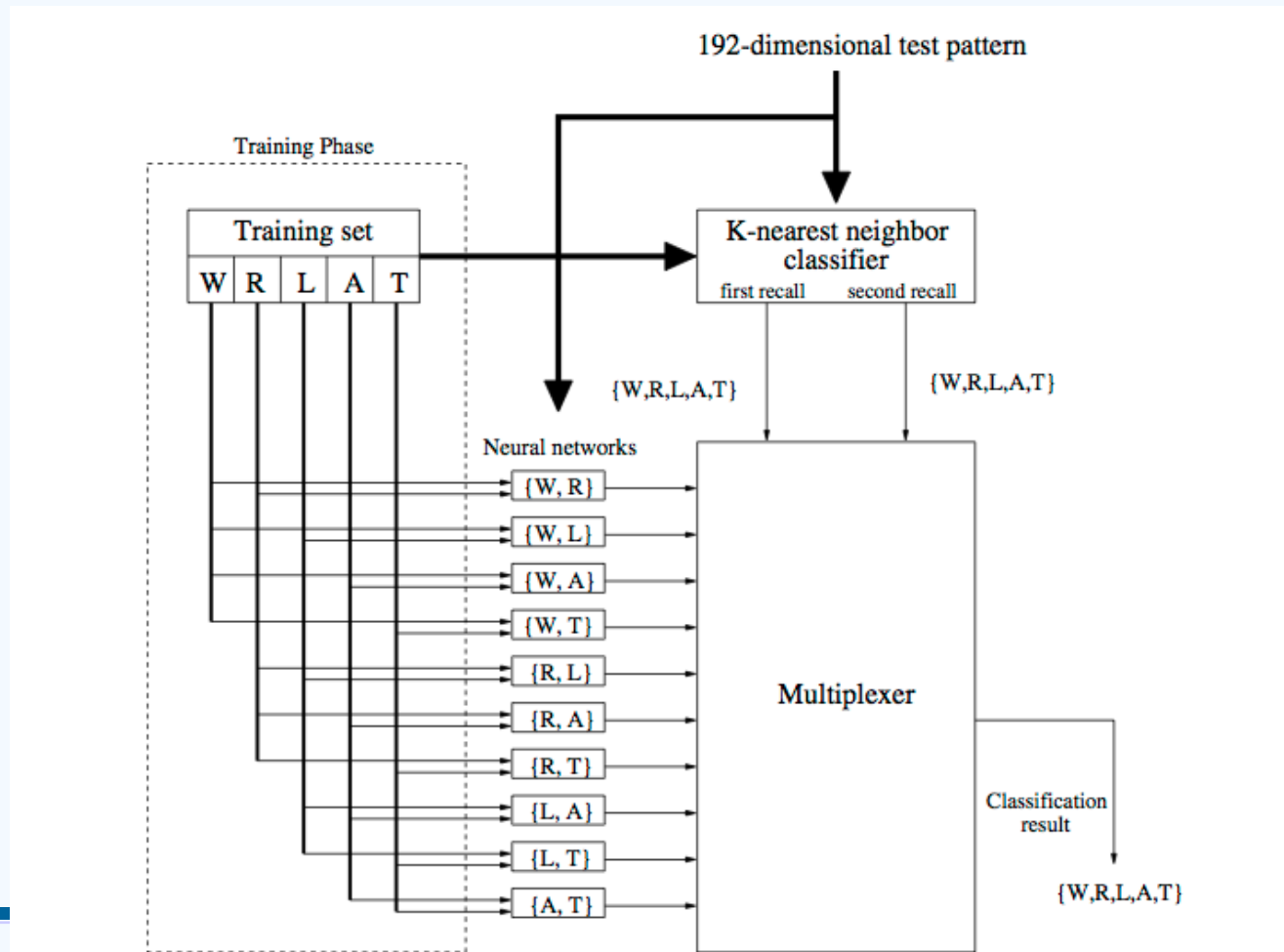


laboratory
Gerstner



Multiply approach III

- Finger code features – k-two most likely classes, neural networks distinguishing two classes



Prize of GOLD



- Good large database > very expensive (FP, ECG, EEG, etc.)
 - DB4, DB14: STANDARDS for classification systems
 - 8bit- grey level images of rolled FP scanned from cards,
 - Manual annotation by a human expert (A, L, R, T, W)
 - 2000 FPs: DB4
 - 27000 FPs: DB14
 - All classes are distributed equally. However, Arch: 3.7%, tented arch: 2.9%, left loop: 33.8%, right loop: 31.7%, whorl: 27.9%
 - Therefore some authors weight results according class distribution



Classification Evaluation



- Accuracy
 - Rejection can improve accuracy

$$\text{error rate} = \frac{\text{number of misclassified fingerprints} \times 100}{\text{total number of fingerprints}}\%$$

$$\text{accuracy} = 100\% - \text{error rate}.$$

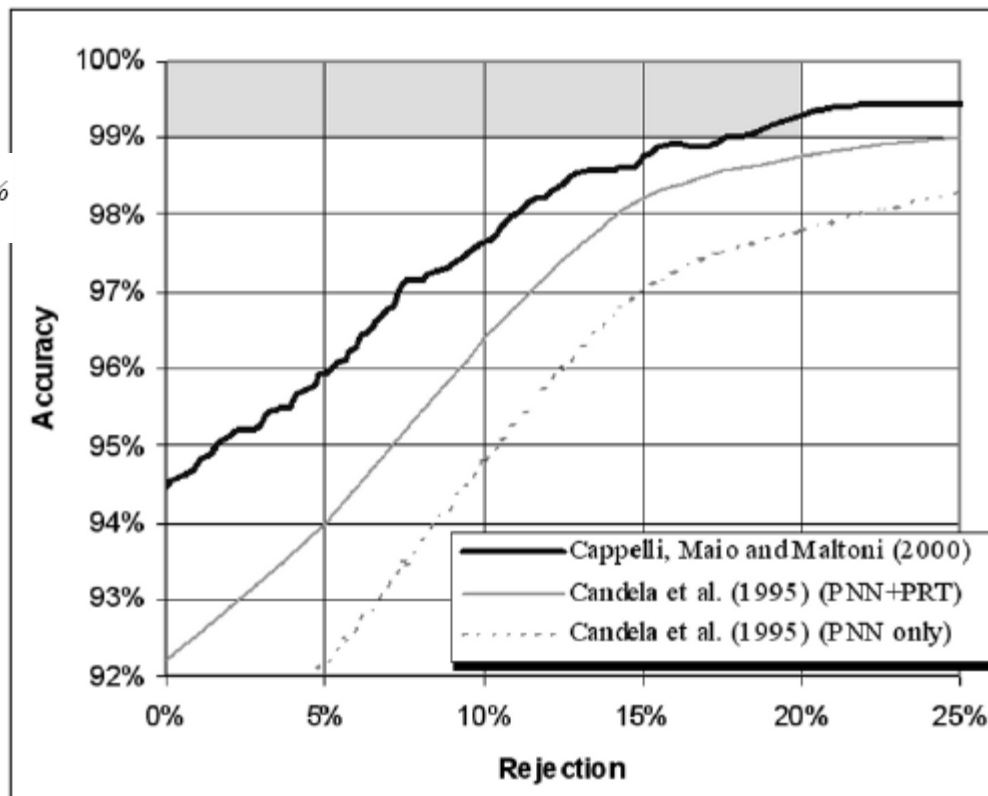
- Penetration rate: time constraint

$$\text{penetration rate} = \frac{\text{number of accessed fingerprints} \times 100}{\text{total number of fingerprints in the database}}\%$$

- Confusion matrix (DB4)

True class	Hypothesized class				
	A	L	R	W	T
A	420	6	3	1	11
L	3	376	3	9	11
R	5	1	392	6	16
W	2	5	14	377	1
T	33	18	9	0	278

- Rejection can improve accuracy (DB14)
 - Unknown class
 - FBI target: shaded area
 - **NIST database -DB 4, DB14**





Results on DB4, DB14

– Results on DB4

True class	Hypothesized class				
	A	L	R	W	T
A	420	6	3	1	11
L	3	376	3	9	11
R	5	1	392	6	16
W	2	5	14	377	1
T	33	18	9	0	278

True class	Hypothesized class			
	A+T	L	R	W
A+T	782	10	17	6
L	6	373	2	4
R	7	1	381	9
W	0	4	7	391

– Results on DB14, last 2700 examples for testing

Method	Error rate (%)
Candela et al. (1995)	7.8
Wei, Yuan, and Jie (1998)	6.0
Cappelli, Maio, and Maltoni (2000a)	5.6

Method	Test set	5 classes		4 classes	
		%	Weighted (%)	%	Weighted (%)
Candela et al. (1995)	Second half	–	–	11.4	6.1
Karu and Jain (1996)	Whole DB	14.6	11.9	8.6	9.4
Senior (1997)	Random 542	–	–	–	8.4
Cappelli, Maio, and Maltoni (1999)	Second half	7.9	6.5	5.5	–
Hong and Jain (1999)	Whole DB	12.5	10.6	7.7	–
Jain, Prabhakar, and Hong (1999)	Second half ^(*)	10.0	7.0	5.2	–
Marcialis, Roli, and Frasconi (2001)	Second half ^(*)	12.1	9.6	–	–
Senior (2001)	Second half	–	–	–	5.1
Yao, Frasconi, and Pontil (2001)	Second half ^(*)	10.7	9.0	6.9	–
Jain and Minut (2002)	Whole DB	–	–	8.8	9.3
Cappelli et al. (2003)	Second half	4.8	3.7	3.7	3.4
Yao et al. (2003)	Second half ^(*)	10.0	8.1	–	–
Cappelli and Maio (2004)	Second half	7.0	5.9	4.7	5.4
Wang and Xie (2004)	Whole DB	–	–	18.0	–
Zhang and Yan (2004)	Whole DB	15.7	11.0	7.3	8.3
Neuhaus and Bunke (2005)	Second half	19.8	–	–	–
Park and Park (2005)	Second half	9.3	7.9	6.0	–
Tan, Bhanu, and Lin (2005)	Second half	8.4	8.0	6.7	7.5
Min, Hong, and Cho (2006)	Second half ^(*)	9.6	7.2	–	–
Wang and Dai (2007)	Whole DB	11.5	9.4	–	–
Hong et al. (2008)	Second half ^(*)	9.2	6.2	5.1	–
Li, Yau, and Wang (2008)	Second half	6.5	7.0	5.0	–



Synthetic fingerprint generation

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**Acknowledgments: Xavier Palathingal, Andrzej Drygajlo,
Handbook of Fingerprint Recognition**



Synthetic fingerprint generation

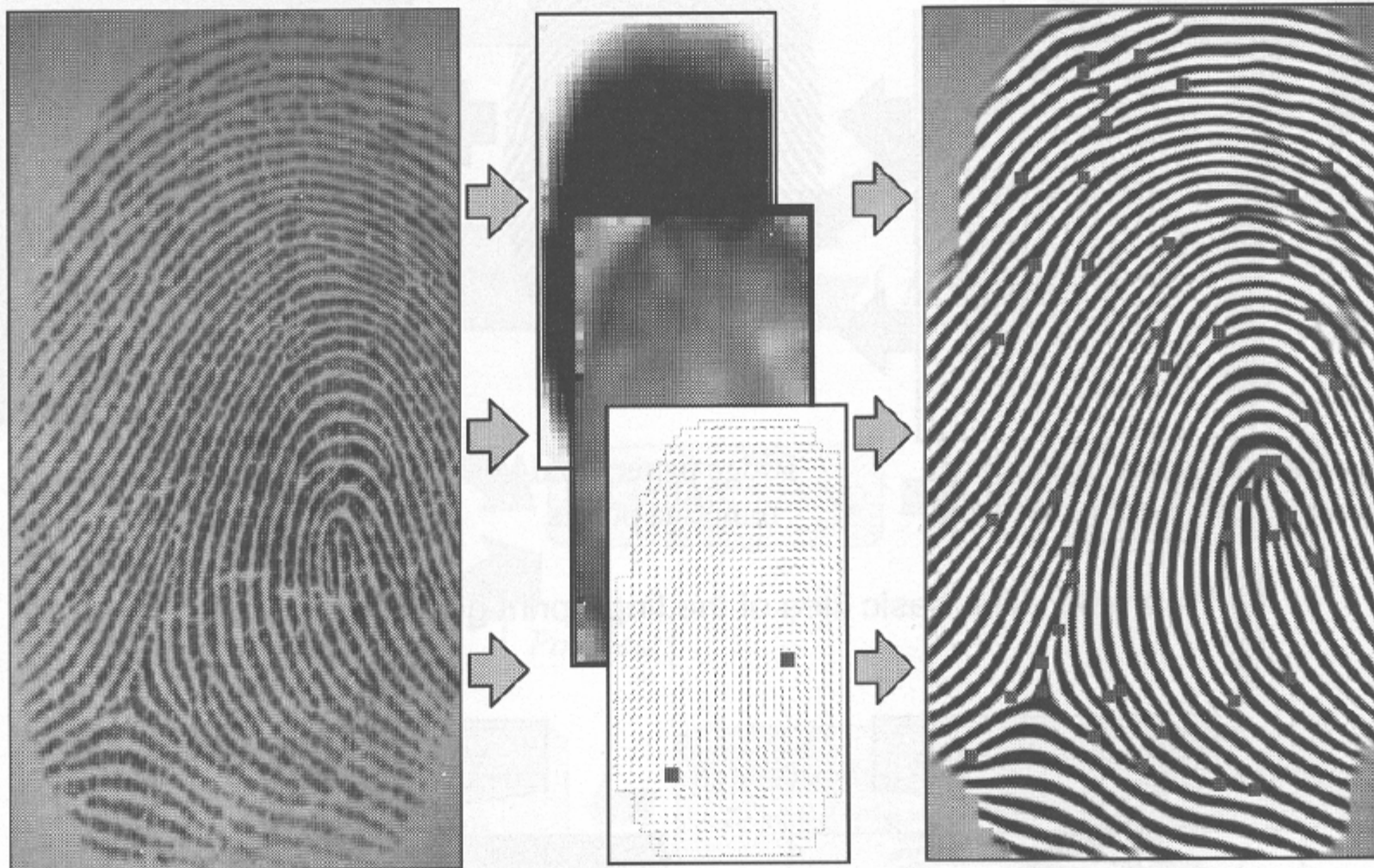
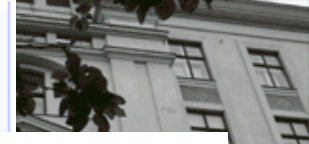


- **Motivation**
 - Accuracy of each algorithm is usually evaluated on relatively small proprietary databases
 - Evaluation on small databases makes the accuracy estimates highly data dependent
 - When the databases are proprietary, the accuracy of various fingerprint matching algorithms cannot be compared directly
- **Synthetic fingerprint generation** can be used to automatically create large databases of fingerprints, thus allowing fingerprint recognition algorithms to be effectively trained, tested, optimized, and compared

8



Feature extraction process



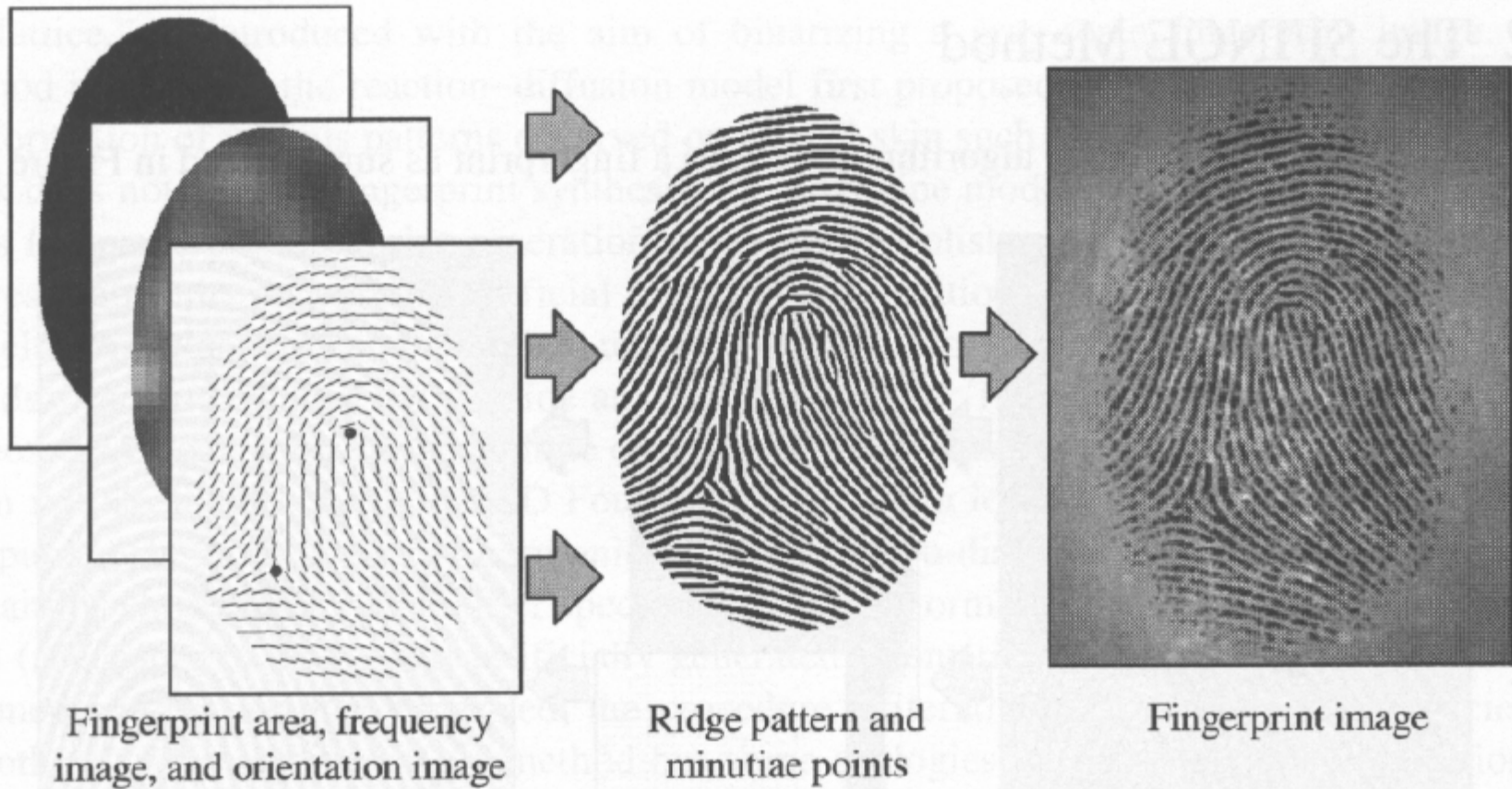
Fingerprint image

Fingerprint area, frequency image, and orientation image

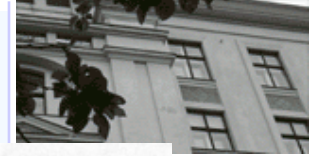
Ridge pattern and minutiae points



Basic idea



From master to final impression



Individuality data



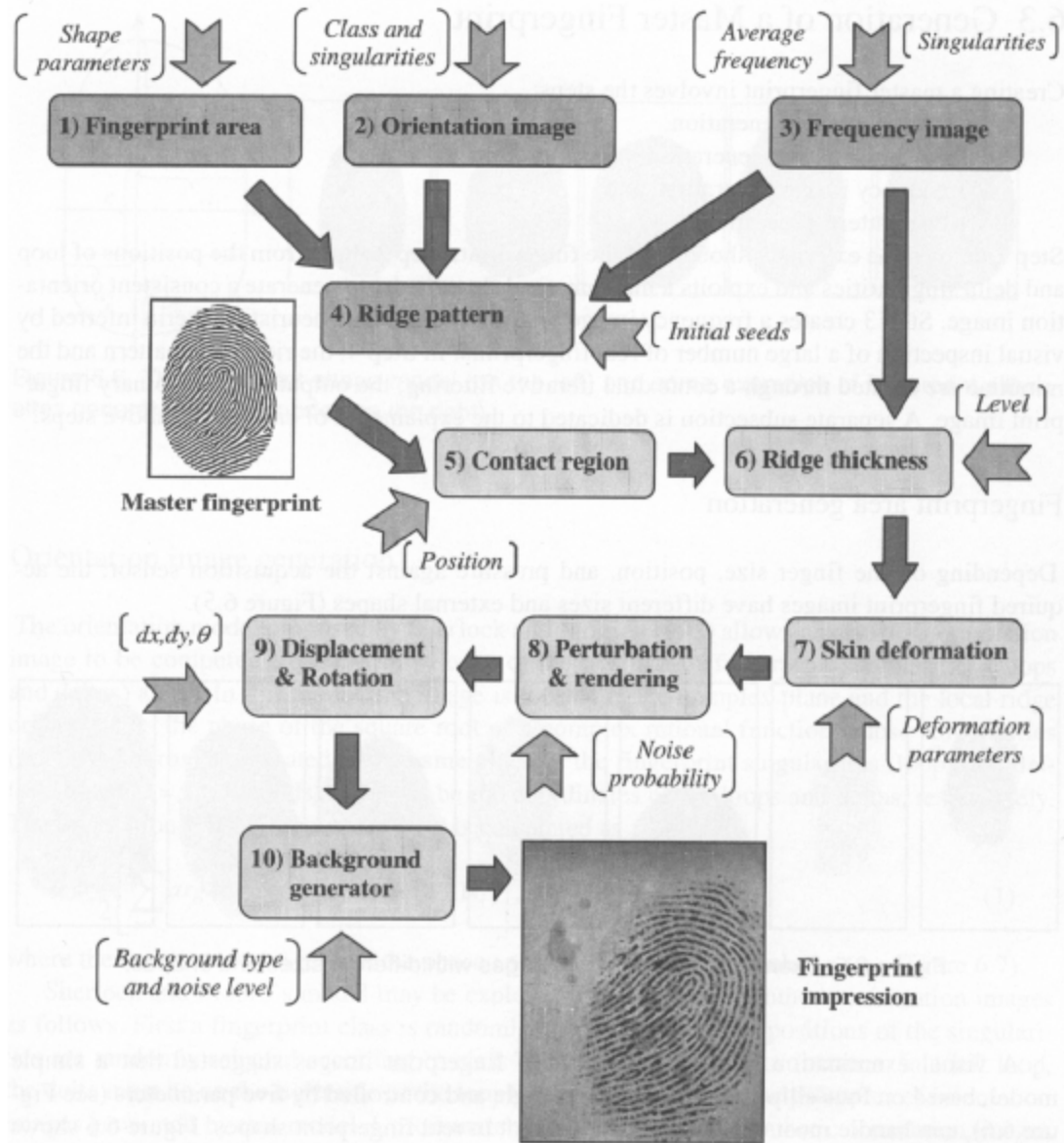
Master fingerprint



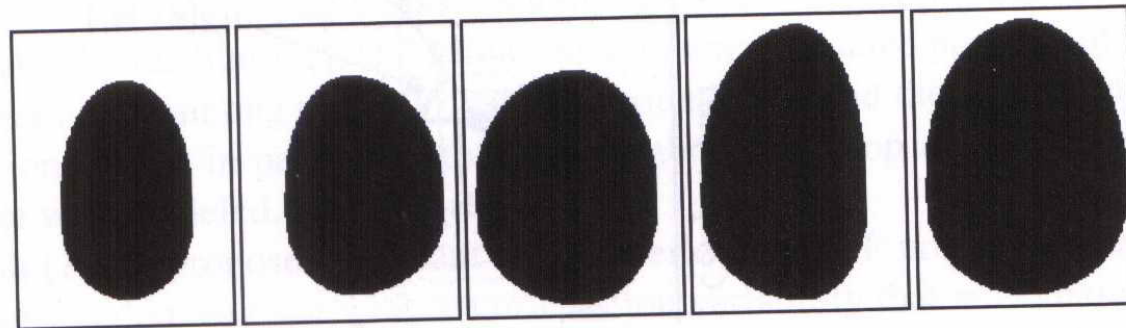
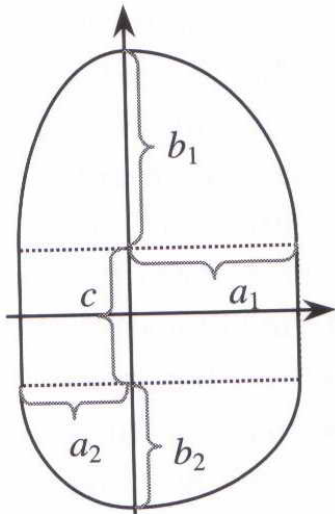
Variability data



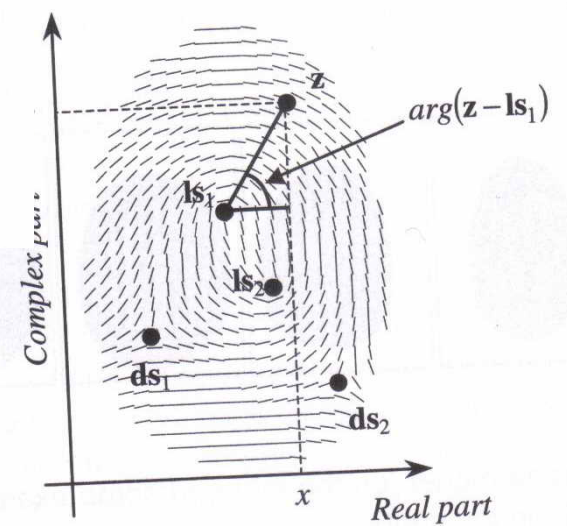
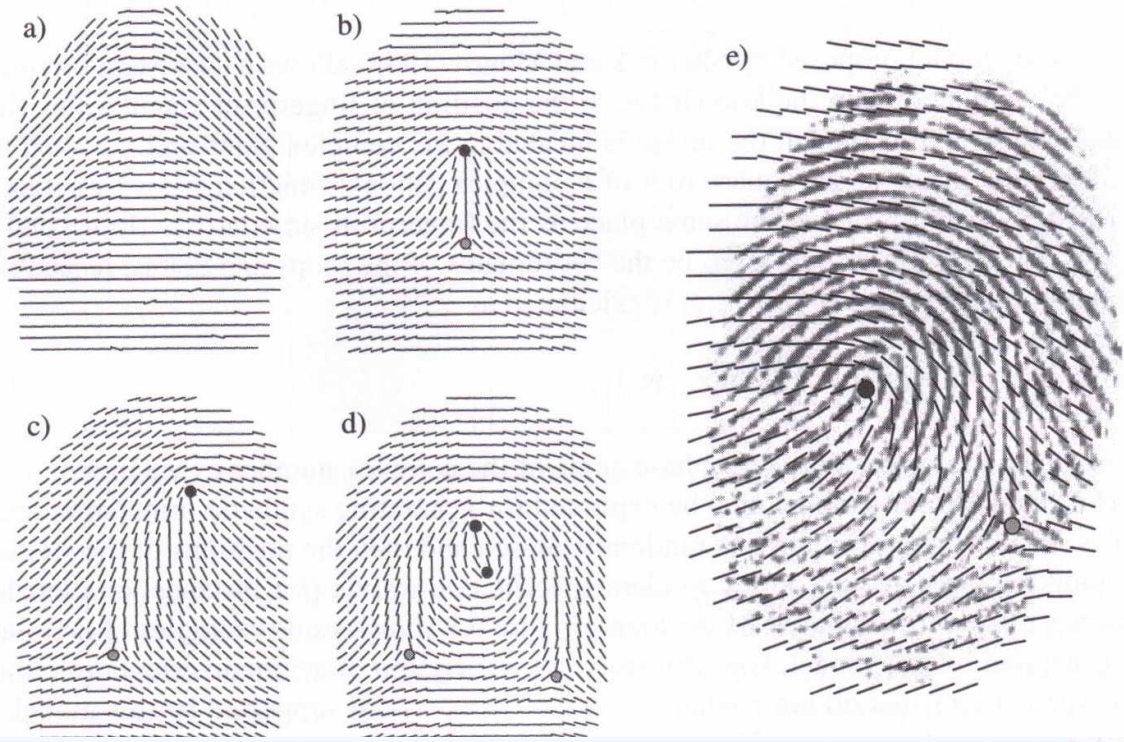
SFINGE



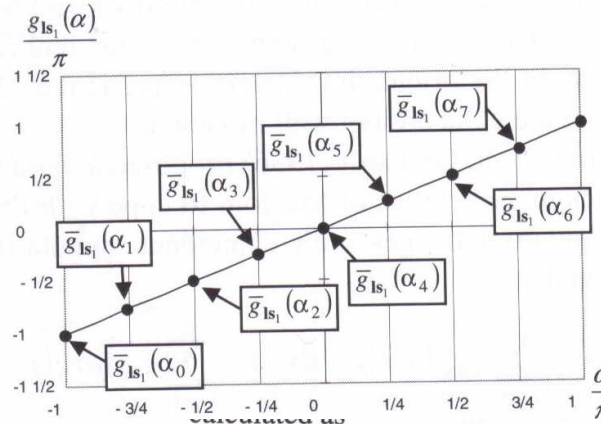
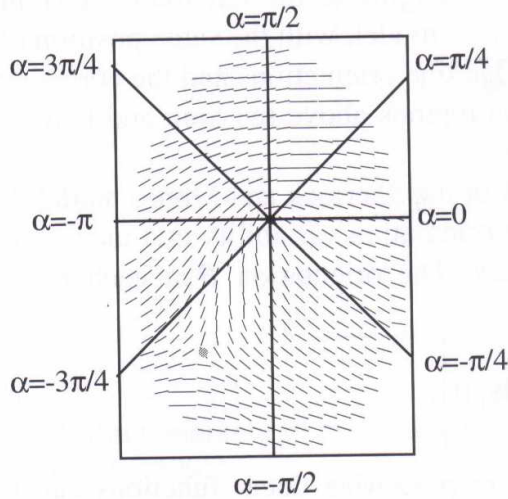
FP area generation



Orientation



Orientation

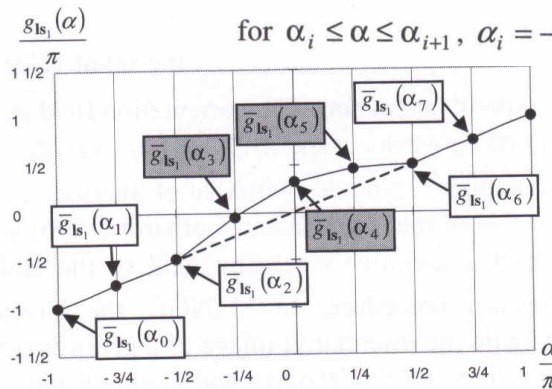
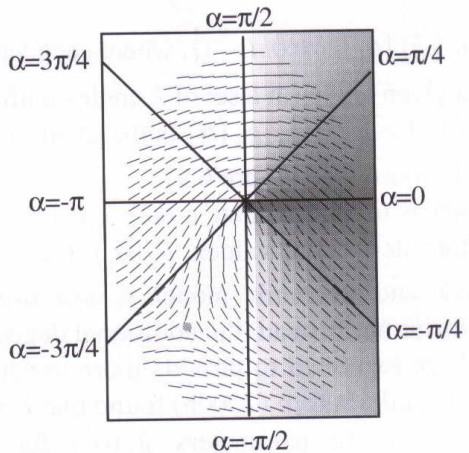


$$\theta = \frac{1}{2} \left[\sum_{i=1}^{n_d} g_{\mathbf{d}s_i}(\arg(\mathbf{z} - \mathbf{d}s_i)) - \sum_{i=1}^{n_c} g_{\mathbf{l}s_i}(\arg(\mathbf{z} - \mathbf{l}s_i)) \right], \quad (2)$$

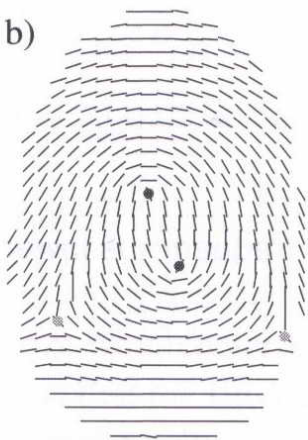
where $g_k(\alpha)$, for $k \in \{\mathbf{l}s_1, \dots, \mathbf{l}s_{n_c}, \mathbf{d}s_1, \dots, \mathbf{d}s_{n_d}\}$, are piecewise linear functions capable of locally correcting the orientation field with respect to the value given by the Sherlock and Monroe model:

$$g_k(\alpha) = \bar{g}_k(\alpha_i) + \frac{\alpha - \alpha_i}{2\pi/L} (\bar{g}_k(\alpha_{i+1}) - \bar{g}_k(\alpha_i)), \quad (3)$$

$$\text{for } \alpha_i \leq \alpha \leq \alpha_{i+1}, \quad \alpha_i = -\pi + \frac{2\pi i}{L}.$$



Orientation



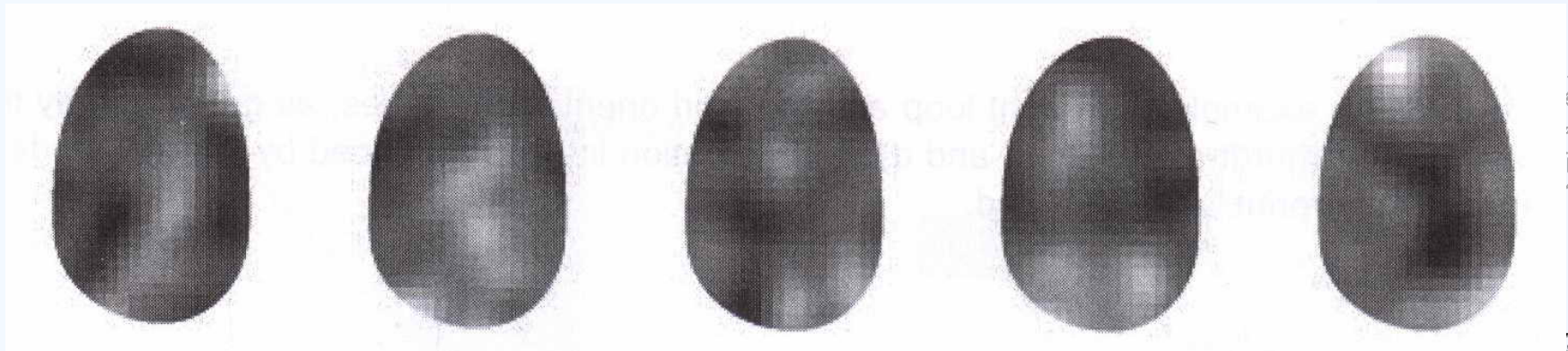
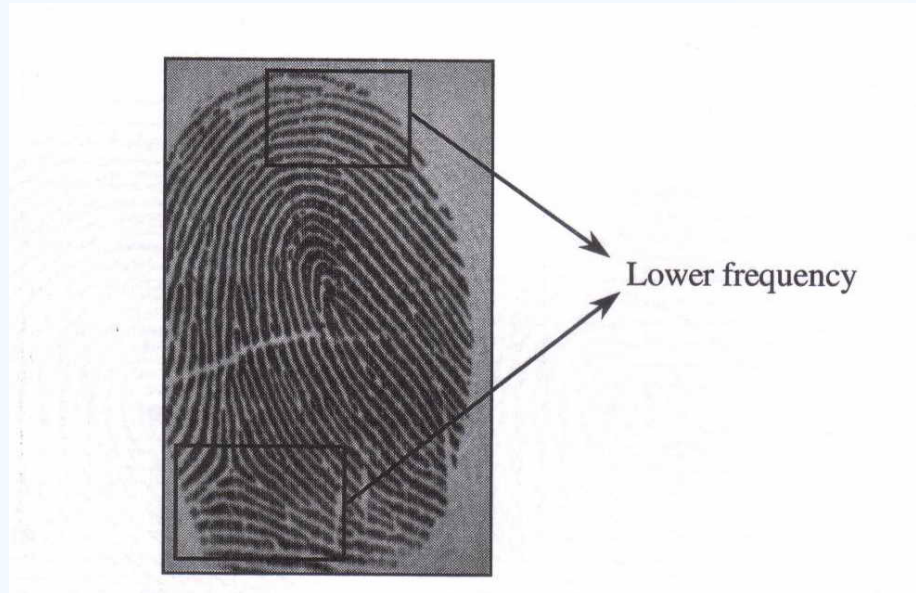
Sherlock and Monro



Vizcaya and Gerhardt



Frequency

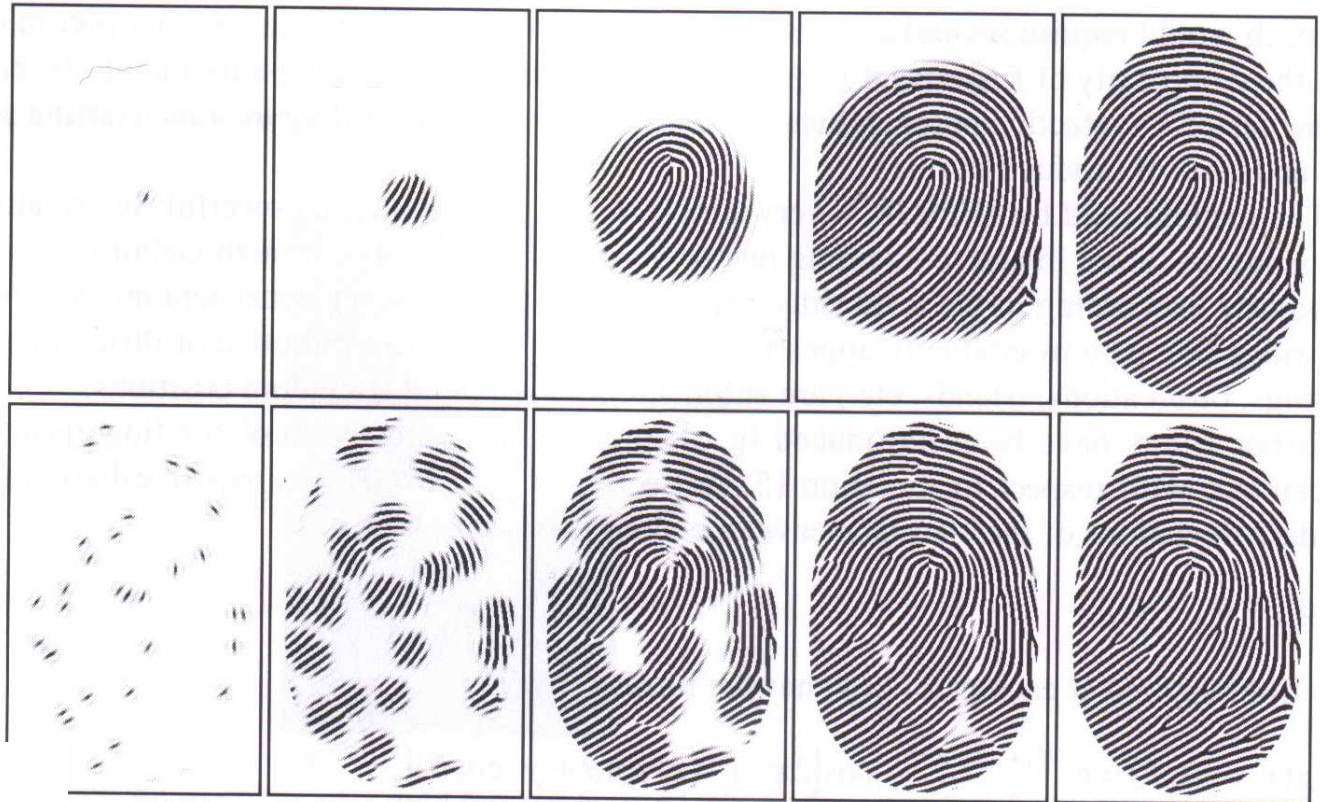


Ridge line

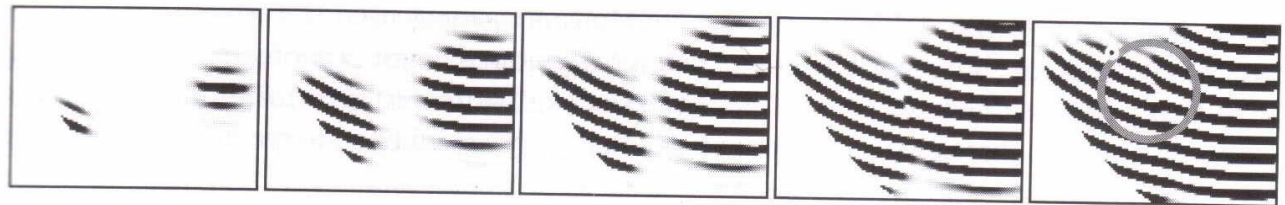


- Gabor filter
- Seeds

$$\sigma_x = \sigma_y = \sigma$$

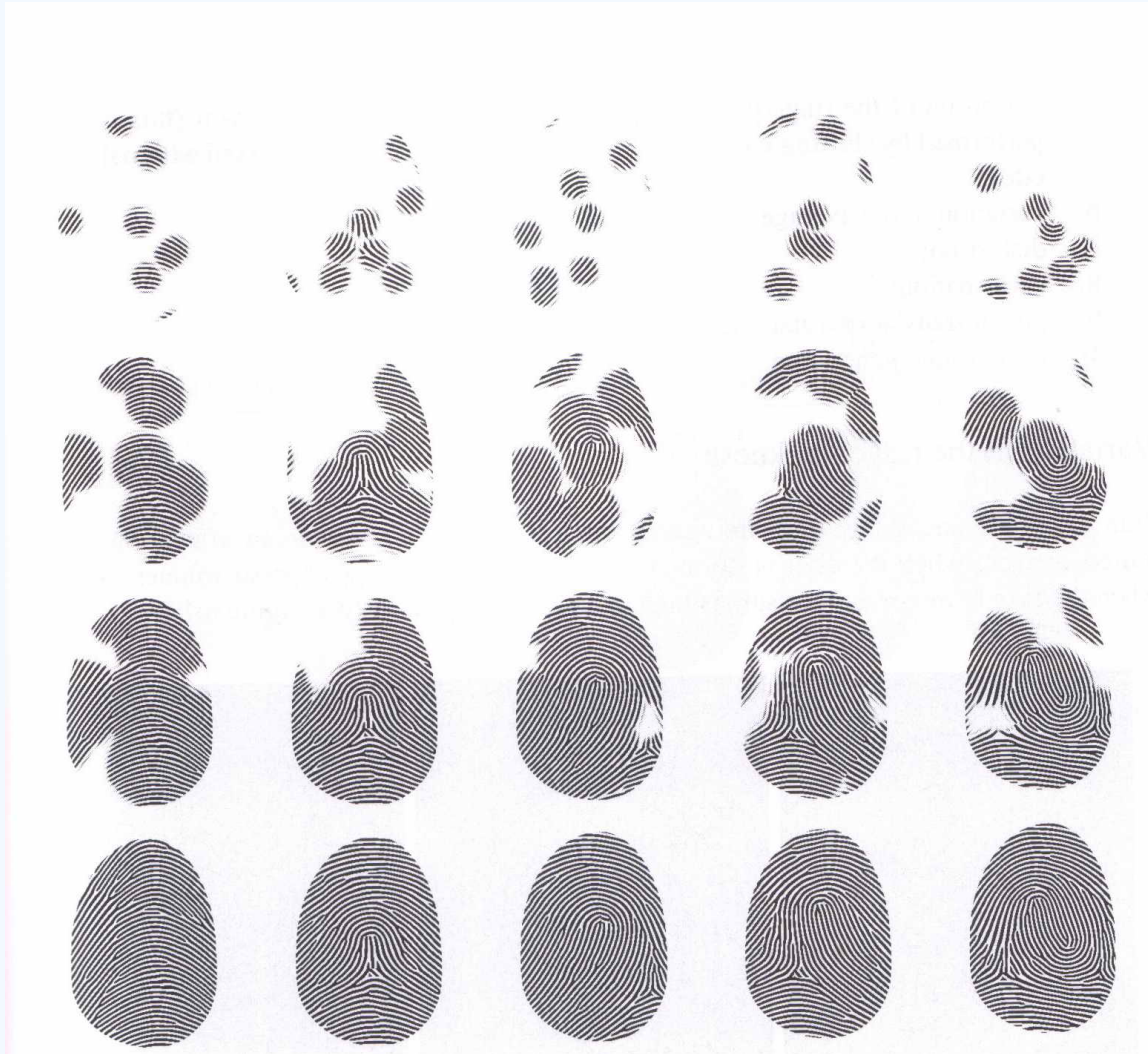
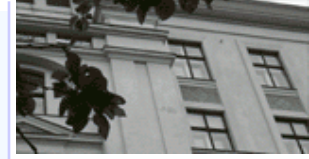


$$e^{-\left(\left(\frac{3}{2f}\right)^2 / 2\sigma^2\right)} = 10^{-3}$$

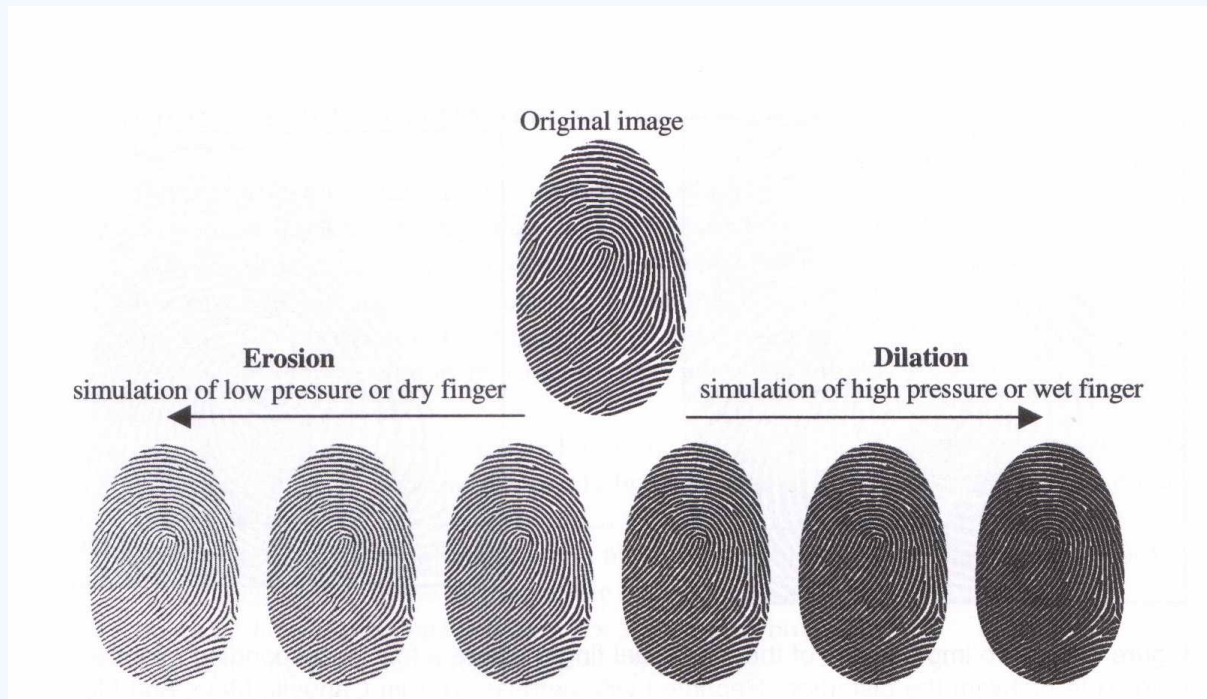


$$g(x, y; \theta, f) = e^{-((x^2 + y^2) / 2\sigma^2)} \cdot \cos[2\pi \cdot f \cdot (x \cdot \sin \theta + y \cdot \cos \theta)],$$

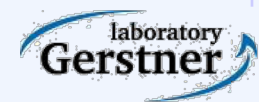
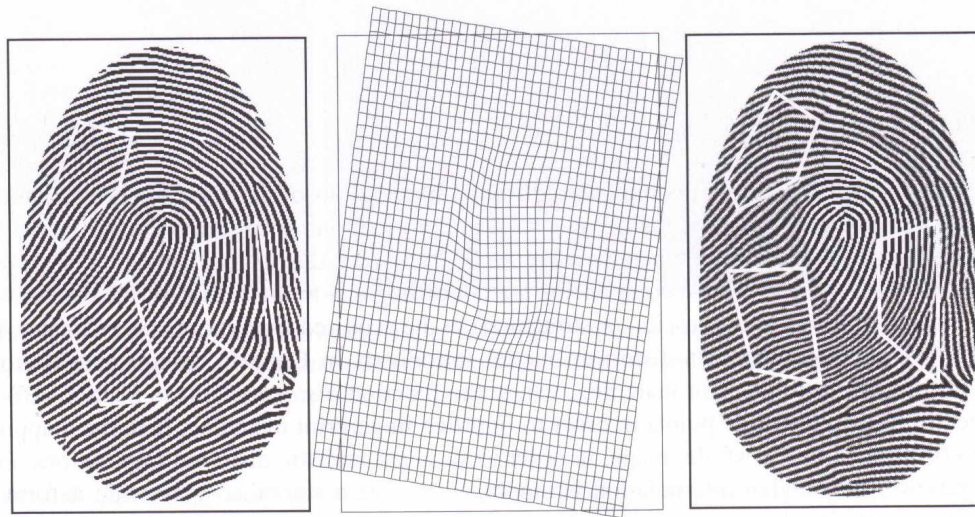
Ridge line



Ridge thickness

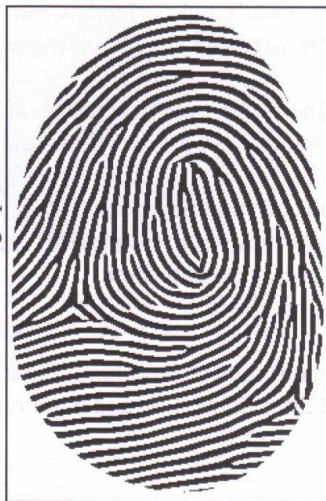


Distortion



Perturbation & Translation

Master fingerprint



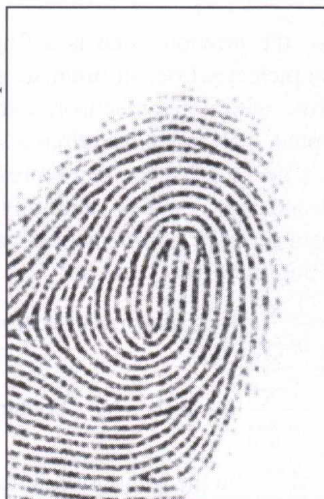
Noising: after Step 2



Noising: after Step 4



Global translation/rotation: after Step 5



Background



- $\bar{\mathbf{b}} = \frac{1}{m} \sum_{\mathbf{b} \in B} \mathbf{b}$ be their mean vector;
- $\mathbf{C} = \frac{1}{m} \sum_{\mathbf{b} \in B} (\mathbf{b} - \bar{\mathbf{b}})(\mathbf{b} - \bar{\mathbf{b}})^T$ be their covariance matrix;
- $\Phi \in \mathcal{R}^{n \times n}$ be the orthonormal matrix that diagonalizes \mathbf{C} ; that is, $\Phi^T \mathbf{C} \Phi = \Lambda$,
 $\Lambda = \text{Diag}(\lambda_1, \lambda_2, \dots, \lambda_n)$, $\Phi = [\varphi_1, \varphi_2, \dots, \varphi_n]$,

where λ_i and φ_i , $i = 1..n$ are the eigenvalues and the eigenvectors of \mathbf{C} , respectively.

1. a k -dimensional vector $\mathbf{y} = [y_1, y_2, \dots, y_k]$ is randomly generated according to k normal distributions: $y_j = N(0, \lambda_{i_j}^{1/2})$, $j = 1..k$;
2. the corresponding n -dimensional vector \mathbf{b} is obtained as: $\mathbf{b} = \Phi_k \mathbf{y} + \bar{\mathbf{b}}$.

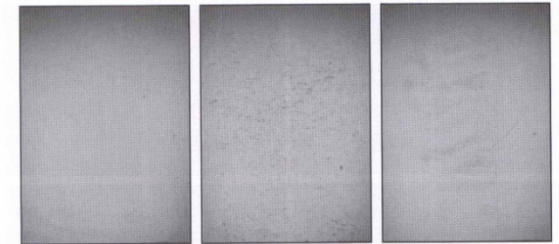


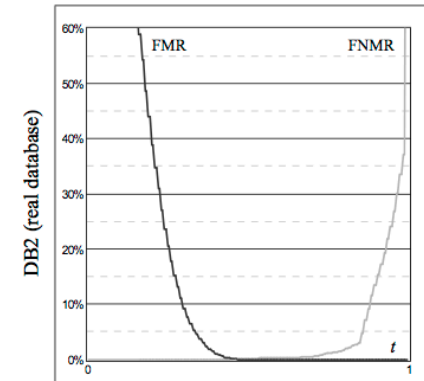
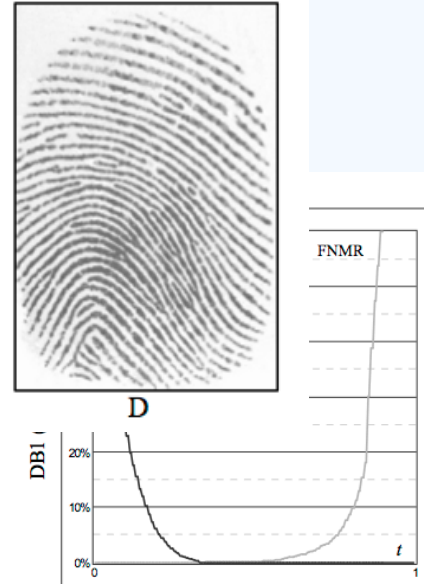
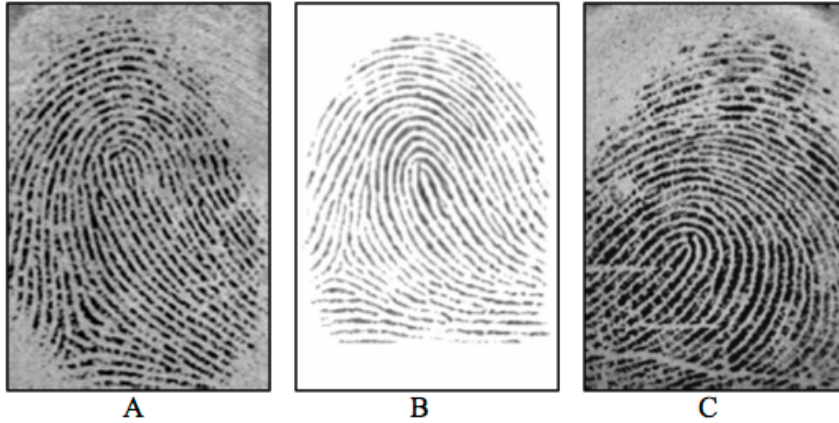
Figure 6.22. Examples of background-only images (acquired from an optical scanner) used for training the background generator.



Figure 6.23. Three synthetic images with backgrounds generated according to the model (the parameters used for training are $m = 65$ and $k = 8$).

Is it working?

- 1st experimtn, 90 experts recognizing synthetic FP -> 23%



- 2nd experiment
- DB1,2,3-real, DB4 synthetic, FMR FNMR

