



Classification

Daniel Novák

6.12, 2011, Prague

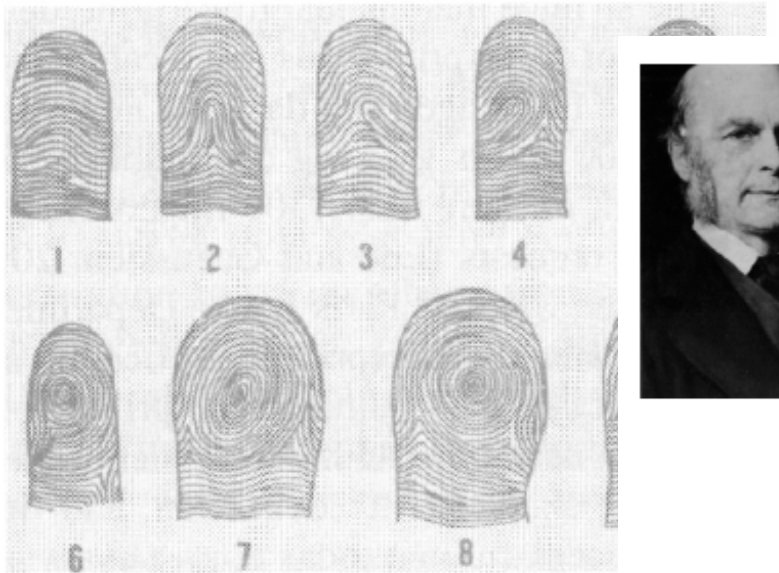
**Acknowledgments: Xavier Palathingal, Andrzej Drygajlo,
Handbook of Fingerprint Recognition**







History

- In 1823, **Purkinji** proposed the first fingerprint classification, which classified into nine categories: (transverse curve, central longitudinal stria, oblique stripe, oblique loop, almond whorl, spiral whorl, ellipse, circle, and double whorl)
- **Sir Francis Galton** introduced the minutae features for fingerprint matching in late 19th century



MR. FRANCIS GALTON'S ANTHROPOMETRIC LABORATORY.

The Laboratory communicates with the "Western Gallery" in which the Scientific Collections of the South Kensington Museum are contained. The Western Gallery runs parallel to Queen's Gate, and is entered either from Queen's Gate or from the new Imperial Institute Road. The latter entrance is close to the Laboratory. Admission is free.

Date of Measurement.			Initials.			Birth-day.			Eye Color.	Sex.	Single, Married, or Widowed?	Page of Register.	
Day.	Month.	Year.	Day.	Month.	Year.	Day.	Month.	Year.					
20	12	89	J. H.	S	22	2	70	1870	Grey	m	S	2310	
Head length, maximum.	Head breadth, maximum.	Height, standing, less heels of shoes.	Span of arms from opposite finger tips.	Weight in ordinary clothing.	Strength of grasp, Right hand.	Left hand.	Knowledge of Eyesight.		Breathing capacity.		Distance of reading diamond uncorrected.	Snellen's type read at 20 feet.	Color sense.
Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	lbs. Oz.	lbs. Oz.	lbs. Oz.	Cubic inches.	Inches.	Inches.	No. of Type	? Normal.		
7.3	5.9 1/2	66.6	67.7	128	93	88	200	19	19.	56	Yes		
Height sitting, above seat of chair.	Height of eye of knee, when sitting, less heels.	Length, elbow to finger tip, left arm.	Length of middle finger of left hand.	Knowledge of hearing.	Height, audible voice, (by whistle).	Reaction time.		Left Thumb.		Right Thumb.			
Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	Inch. Tenths.	? Normal.	Vibrations per second.	Headwidths of a second.	Headwidths of a second.						
35.5	20.7	17.7 1/2	4.5	Yes	21,000	15	15						

One page of the Register is assigned to each person measured, in which his measurements at successive periods are entered in successive lines. No names appear on the Register. Copies of the entries can be obtained through application of the persons measured, or by their representatives, under such conditions and restrictions as may be fixed from time to time.



Classes

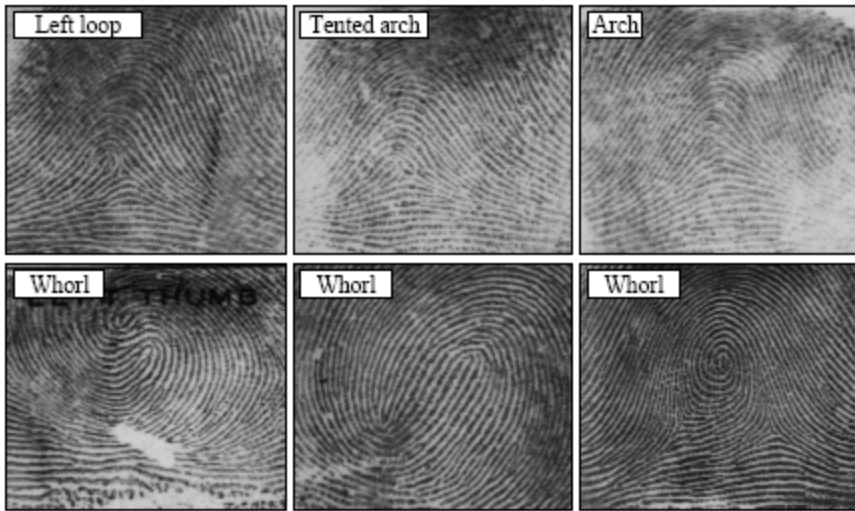
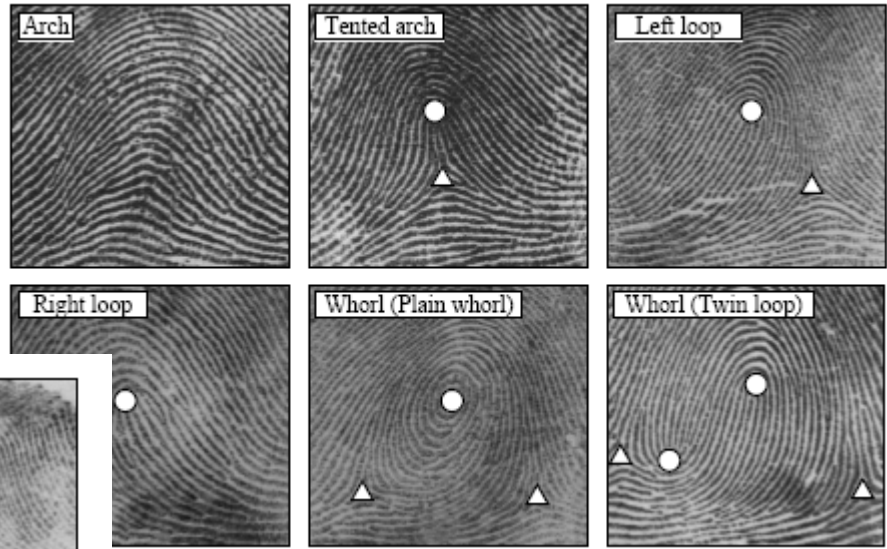
- Arch: 3.7%, tented arch: 2.9%, left loop: 33.8%, right loop: 31.7%, whorl: 27.9%

- Pattern recognition

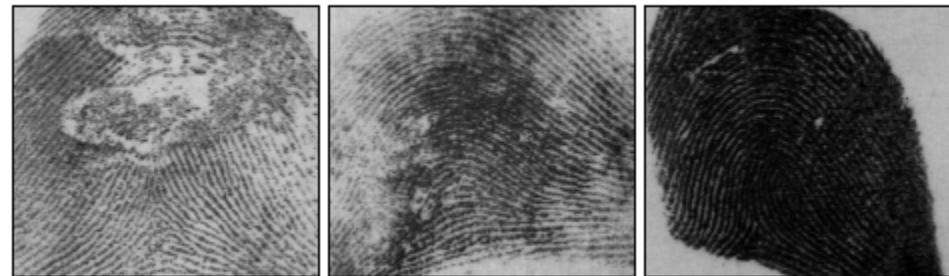
PROBLEM

Small-inter class variability

Large intra-class variability



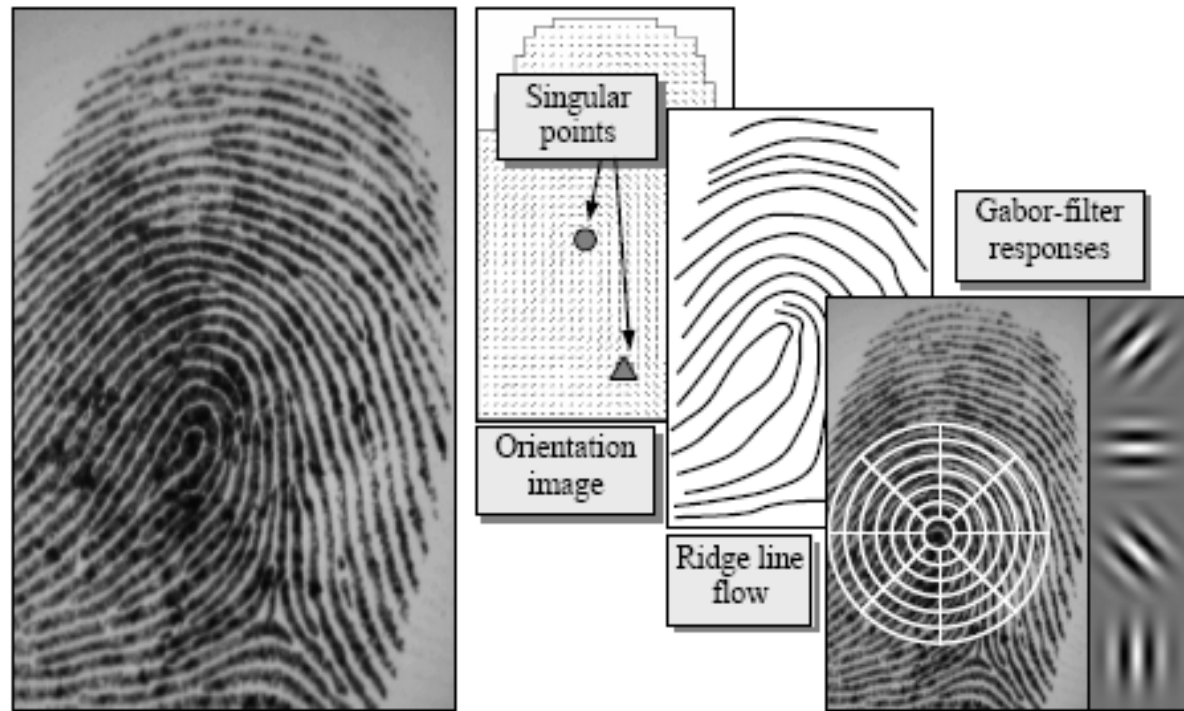
presence of noise





Features

- Based on global features
- Ridge line flow, orientation image, singular point, Gabor filters



Techniques



- Features:
 - O = orientation image
 - S = singularities
 - R = ridge flow,
 - G = Gabor
- classification technique
 - Rb = rule-based
 - Sy = syntactic
 - Str = structural,
 - Sta = statistical
 - Nn = neural network
 - Mc = multiple classifiers

Fingerprint classification approach	Features				Classifier					
	O	S	R	G	Rb	Sy	Str	Sta	Nn	Mc
Moayer and Fu (1975)	√					√				
Moayer and Fu (1976)	√					√				
Rao and Balck (1980)	√					√				
Kawagoe and Tojo (1984)		√	√		√					
Hughes and Green (1991)	√								√	
Bowen (1992)	√	√							√	
Kamijo, Mieno, and Kojima (1992)	√								√	
Kamijo (1993)	√								√	
Moscinska and Tyma (1993)	√				√				√	
Wilson, Candela, and Watson (1994)	√								√	
Candela et al. (1995)	√		√		√				√	√
Omidvar, Blue, and Wilson (1995)	√								√	
Halici and Ongun (1996)	√								√	
Karu and Jain (1996)		√			√					
Maio and Maltoni (1996)	√						√			
Ballan, Sakarya, and Evans (1997)		√			√					
Chong et al. (1997)			√		√					
Senior (1997)			√				√			
Wei, Yuan, and Jie (1998)	√				√				√	√
Cappelli et al. (1999)	√						√			
Cappelli, Maio, and Maltoni (1999)	√							√		
Hong and Jain (1999)		√	√		√					√
Jain, Prabhakar, and Hong (1999)				√				√	√	√
Lumini, Maio, and Maltoni (1999)	√						√			
Cappelli, Maio, and Maltoni (2000a)	√							√		√
Cho et al. (2000)		√			√					
Bartasaghi, Fernández, and Gómez (2001)		√			√					
Bernard et al. (2001)	√								√	
Marcialis, Roli, and Frasconi (2001)	√			√			√	√	√	√
Pattichis et al. (2001)	√				√				√	√
Senior (2001)	√		√		√		√		√	√
Yao, Frasconi, and Pontil (2001)				√				√		√
Cappelli, Maio, and Maltoni (2002a)	√							√		√
Jain and Minut (2002)			√		√					
Cappelli et al. (2003)	√							√		√
Yao et al. (2003)	√			√			√	√	√	√



Techniques



Fingerprint classification approach	Features				Classifier					
	O	S	R	G	Rb	Sy	Str	Sta	Nn	Mc
Cappelli and Maio (2004)	√							√		√
Klimanee and Nguyen (2004)	√	√			√					
Senior and Bolle (2004)	√		√		√		√		√	√
Shah and Sastry (2004)								√	√	√
Wang and Xie (2004)	√	√	√		√					
Zhang and Yan (2004)	√	√	√		√					
Park and Park (2005)	√							√		
Neuhaus and Bunke (2005)	√						√			
Tan, Bhanu, and Lin (2005)	√							√		
Min, Hong, and Cho (2006)				√				√		√
Kristensen, Borthen, and Fyllingsnes (2007)				√					√	
Wang and Dai (2007)	√	√			√					
Hong et al. (2008)	√	√		√				√		√
Li, Yau, and Wang (2008)	√	√						√		

Techniques II



- Syntactic: terminal symbols & production rules

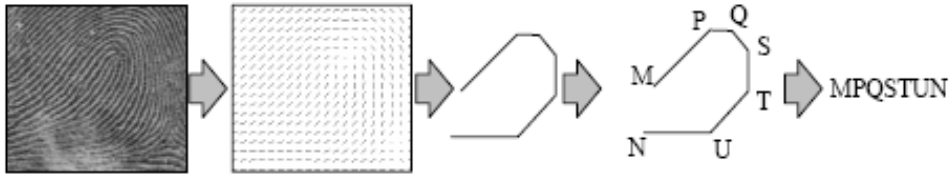
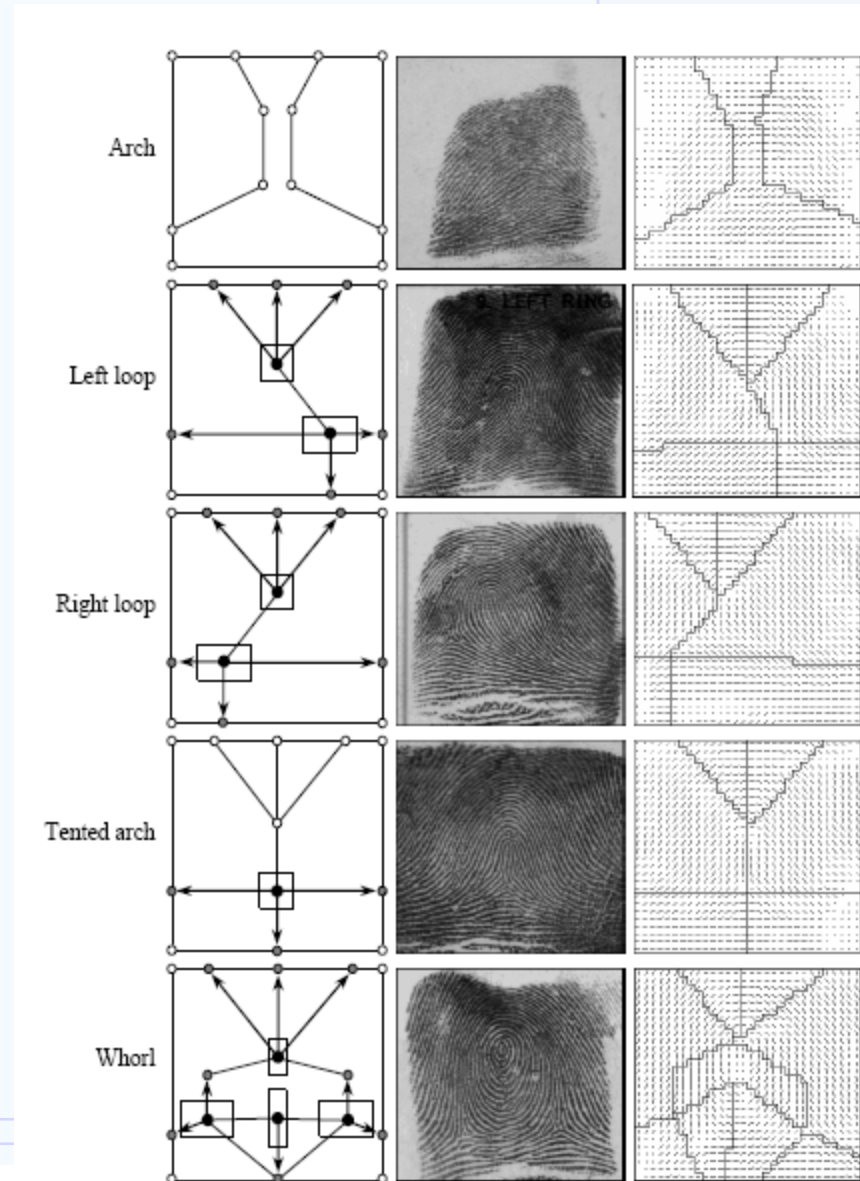


Figure 5.7. A schema of the string-construction approach in Rao and Balck (1980).

- Structural approach
- Statistical
 - Orientation image
 - k-nearest neighbor
 - 30x30 array, 1800 elements
 - PCA (the Karhunen-Loeve) transform

$$\mathbf{d} = [r \cdot \cos(2\theta), r \cdot \sin(2\theta)]$$

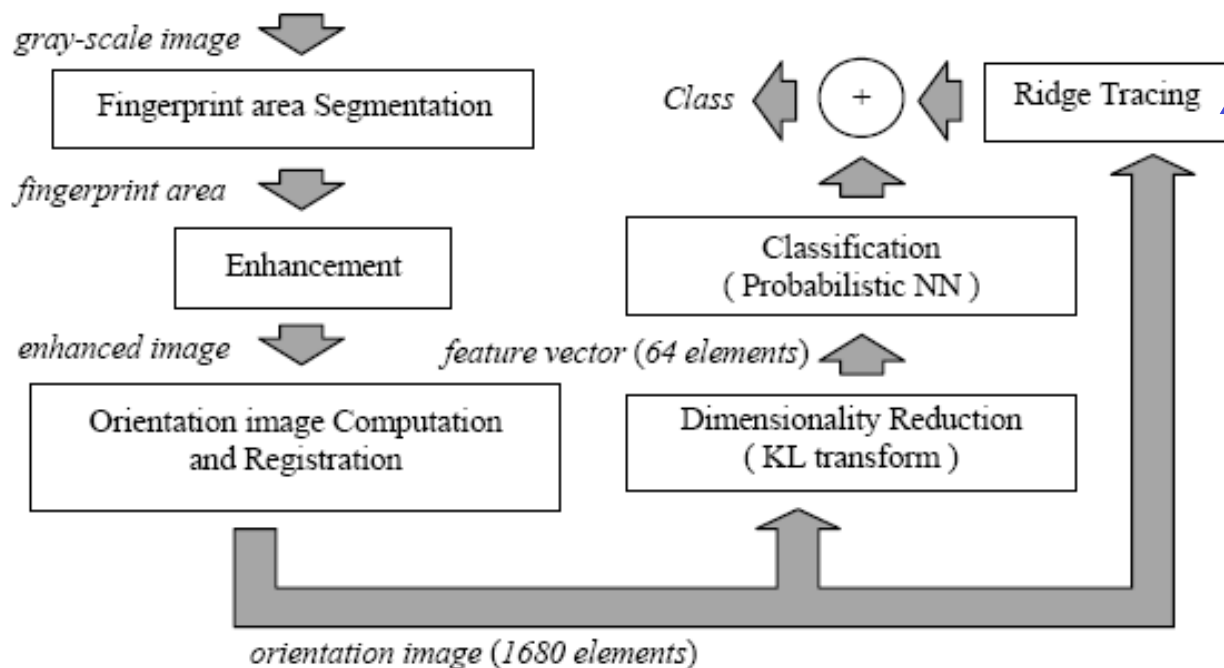


Techniques III



- Multiple classifier-based approaches
- PCASYS: Pattern-level Classification Automation system
- Open Source: <http://ffpis.sourceforge.net/>
- Developed by NIST: <http://www.nist.gov/index.html>
 - National Institute of Standards and Technology

**Whorl
module**



laboratory
Gerstner

Classification Evaluation



- Accuracy
 - Rejection can improve accuracy

$$\text{error rate} = \frac{\text{number of misclassified fingerprints} \times 100}{\text{total number of fingerprints}}\%$$

$$\text{accuracy} = 100\% - \text{error rate}.$$

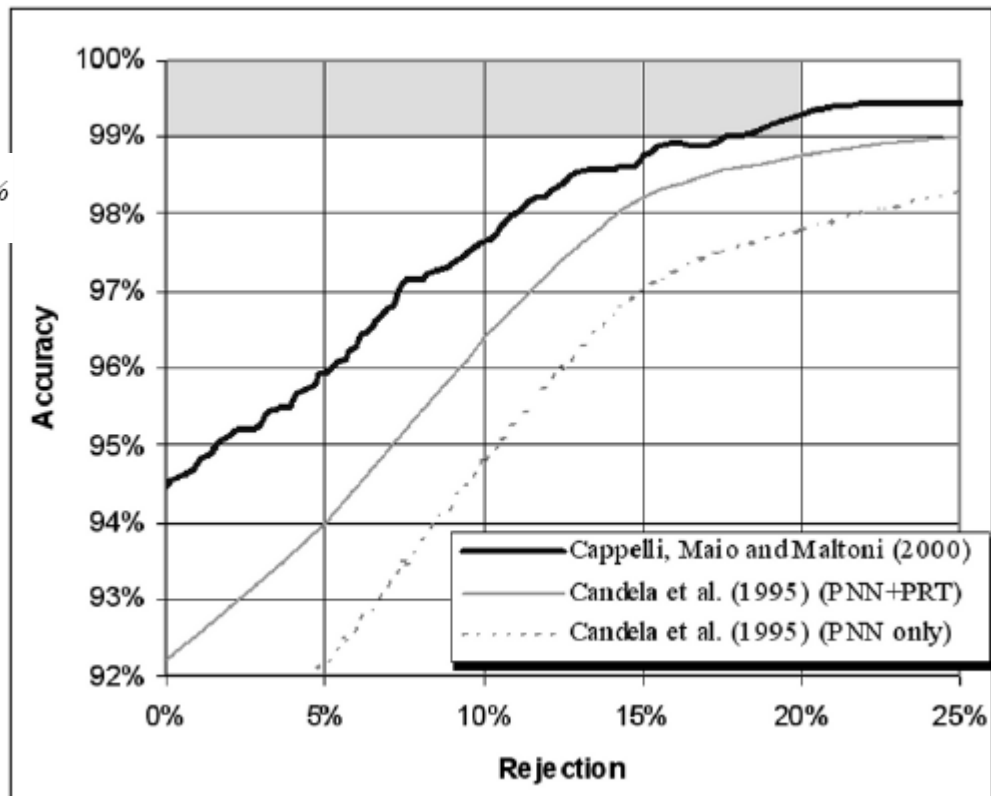
- Rejection can improve accuracy (DB14)
 - Unknown class
 - FBI target
 - **NIST database -DB 4, DB14**

- Penetration rate: time constraint

$$\text{penetration rate} = \frac{\text{number of accessed fingerprints} \times 100}{\text{total number of fingerprints in the database}}\%$$

- Confusion matrix (DB4)

True class	Hypothesized class				
	A	L	R	W	T
A	420	6	3	1	11
L	3	376	3	9	11
R	5	1	392	6	16
W	2	5	14	377	1
T	33	18	9	0	278





Results on DB4, DB14

- Results on DB4

True class	Hypothesized class				
	A	L	R	W	T
A	420	6	3	1	11
L	3	376	3	9	11
R	5	1	392	6	16
W	2	5	14	377	1
T	33	18	9	0	278

True class	Hypothesized class			
	A+T	L	R	W
A+T	782	10	17	6
L	6	373	2	4
R	7	1	381	9
W	0	4	7	391

- Results on DB14

Method	Error rate (%)
Candela et al. (1995)	7.8
Wei, Yuan, and Jie (1998)	6.0
Cappelli, Maio, and Maltoni (2000a)	5.6

Method	Test set	5 classes		4 classes	
		%	Weighted (%)	%	Weighted (%)
Candela et al. (1995)	Second half	-	-	11.4	6.1
Karu and Jain (1996)	Whole DB	14.6	11.9	8.6	9.4
Senior (1997)	Random 542	-	-	-	8.4
Cappelli, Maio, and Maltoni (1999)	Second half	7.9	6.5	5.5	-
Hong and Jain (1999)	Whole DB	12.5	10.6	7.7	-
Jain, Prabhakar, and Hong (1999)	Second half ^(*)	10.0	7.0	5.2	-
Marcialis, Roli, and Frasconi (2001)	Second half ^(*)	12.1	9.6	-	-
Senior (2001)	Second half	-	-	-	5.1
Yao, Frasconi, and Pontil (2001)	Second half ^(*)	10.7	9.0	6.9	-
Jain and Minut (2002)	Whole DB	-	-	8.8	9.3
Cappelli et al. (2003)	Second half	4.8	3.7	3.7	3.4
Yao et al. (2003)	Second half ^(*)	10.0	8.1	-	-
Cappelli and Maio (2004)	Second half	7.0	5.9	4.7	5.4
Wang and Xie (2004)	Whole DB	-	-	18.0	-
Zhang and Yan (2004)	Whole DB	15.7	11.0	7.3	8.3
Neuhaus and Bunke (2005)	Second half	19.8	-	-	-
Park and Park (2005)	Second half	9.3	7.9	6.0	-
Tan, Bhanu, and Lin (2005)	Second half	8.4	8.0	6.7	7.5
Min, Hong, and Cho (2006)	Second half ^(*)	9.6	7.2	-	-
Wang and Dai (2007)	Whole DB	11.5	9.4	-	-
Hong et al. (2008)	Second half ^(*)	9.2	6.2	5.1	-
Li, Yau, and Wang (2008)	Second half	6.5	7.0	5.0	-



Biometrics errors

Daniel Novák

6.12, 2011, Prague

**Acknowledgments: Xavier Palathingal, Andrzej Drygajlo,
Handbook of Fingerprint Recognition**





Example Iris & Speech

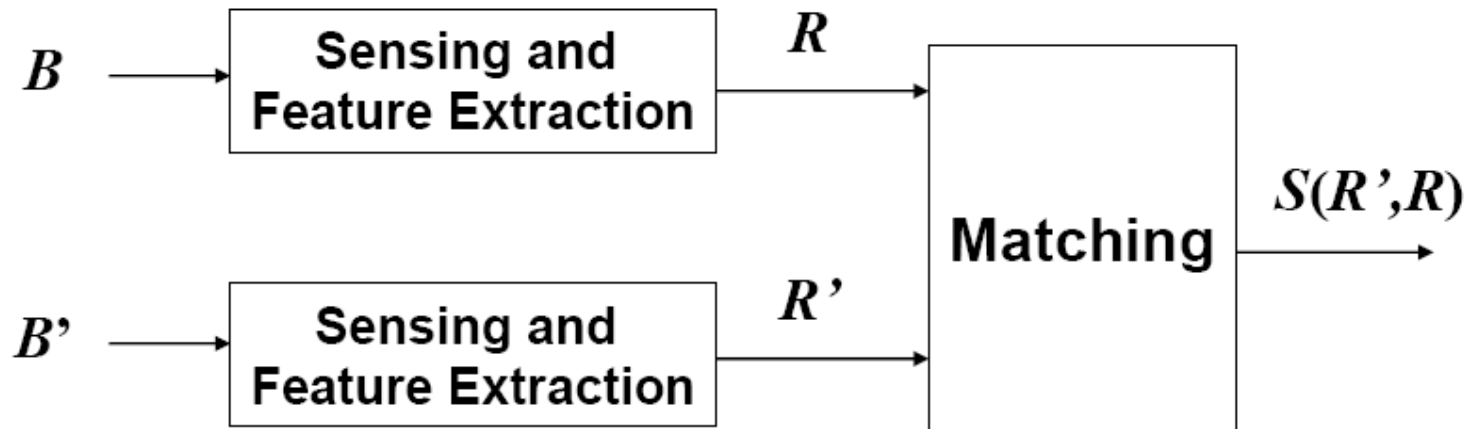
- Example
 - Assume 10'000 customers are signed up for biometric authentication and 1'000 transactions are done weekly
 - Assume best-case biometric verification error of **1 in 1 million (iris)**
 - Assume best-case speaker verification error of **1 in 1 hundred**
 - How often are customers falsely billed?
- Answer
 - On average **10 people are falsely billed each week**
 - On average **100 000 people are falsely billed each week**



Matching

Real-world
biometrics

Features

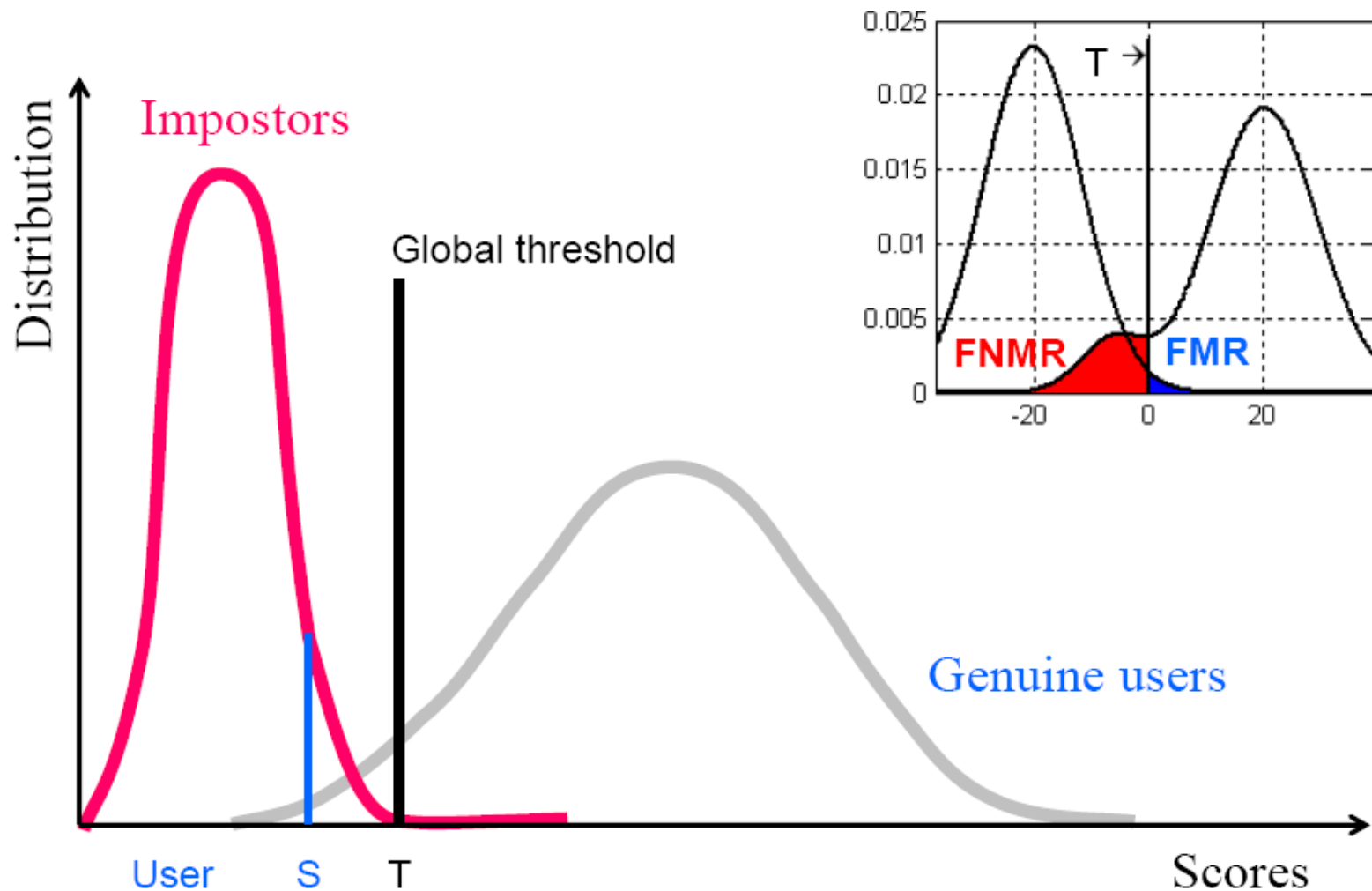


$$s(R', R) = s(f_{t'}(B'(t')), f_t(B(t)))$$

Biometric matching makes a decision by computing a measure of the likelihood that the two input samples from two persons are the « same » and hence that the subjects are the same real-world identity.

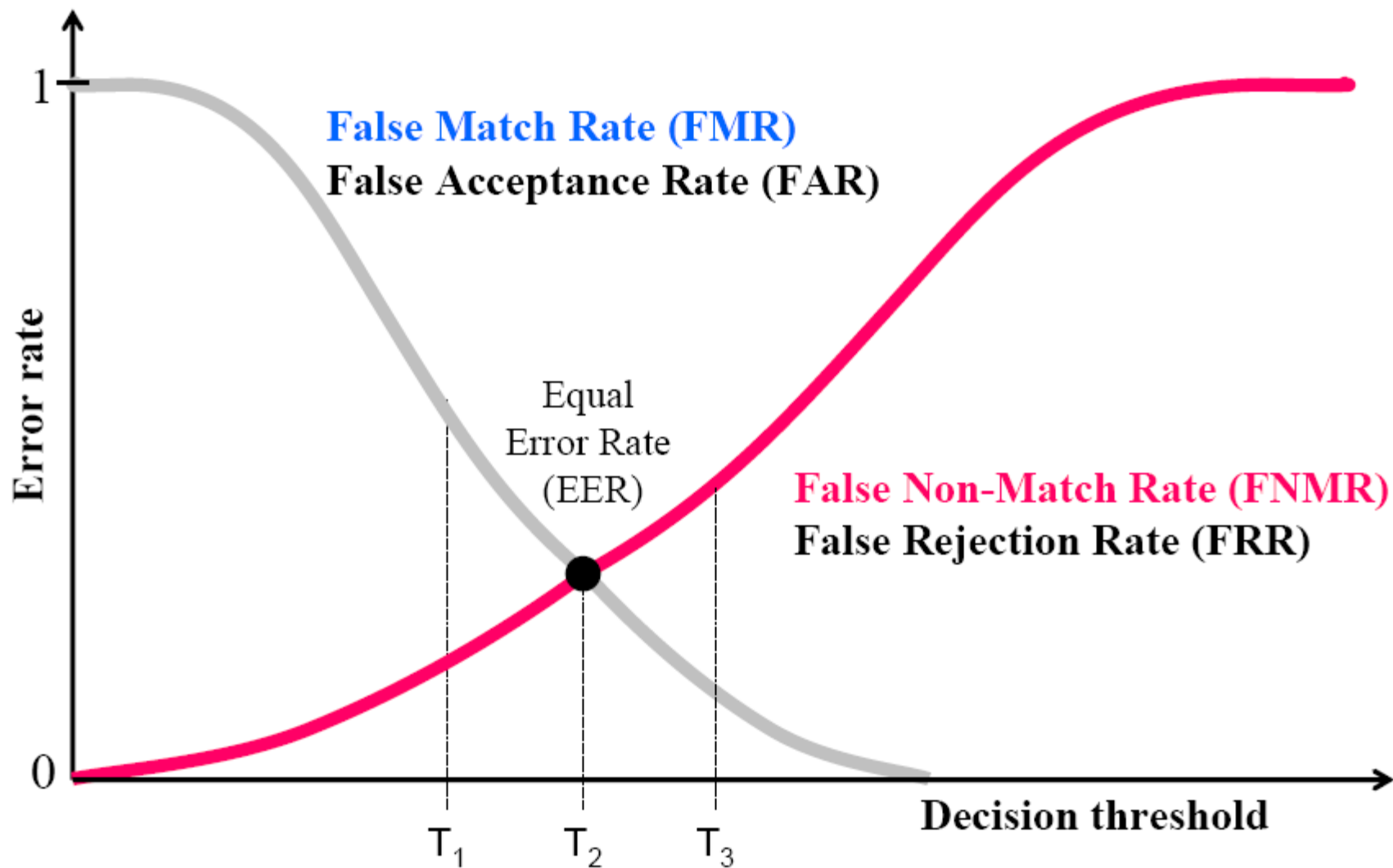


Performance evaluation





FMR and FNMR



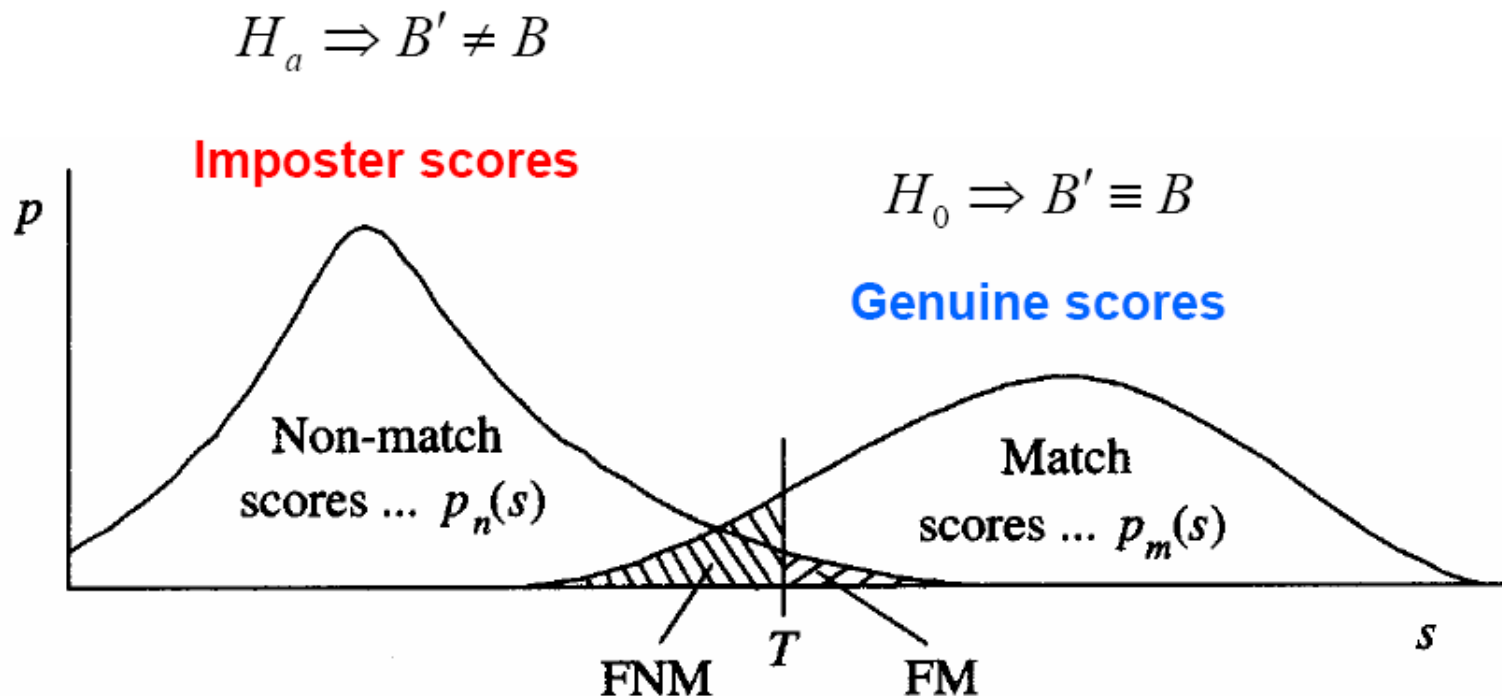


FA & FR

- **False Accept (FA):** Deciding that a (claimed) identity is a legitimate one while in reality it is an imposter; False Accept Rate (FAR)
- **False Reject (FR):** Deciding that a (claimed) identity is not legitimate when in reality the person is genuine; False Reject Rate (FRR)
- A **FA** results in **security** breaches, with an unauthorized person being admitted
- A **FR** results in **convenience** problems, since genuinely enrolled identities are denied access to the application



Scores distribution



Given two biometric samples, we can construct two possible hypotheses:

The null hypothesis: $H_0 \Rightarrow$ the two samples match

The alternate hypothesis: $H_a \Rightarrow$ the two samples do not match



Two kinds of error

- Verification:

Decide H_0 is true: if $s > T$,

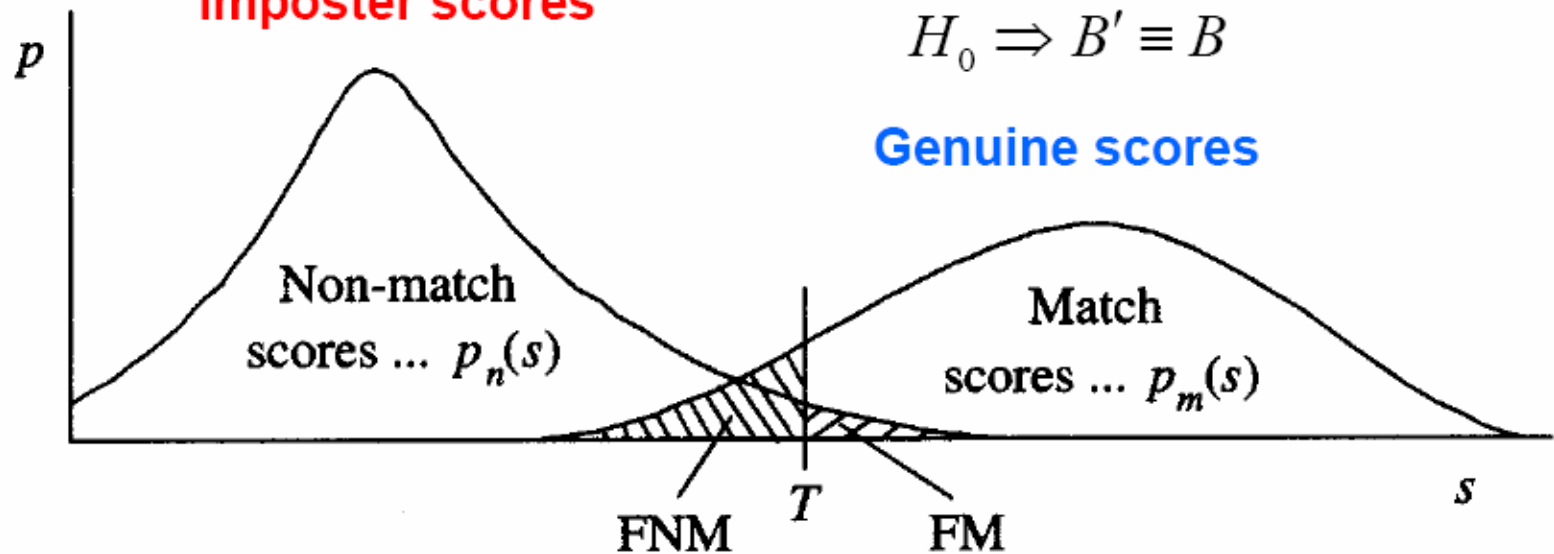
Decide H_a is true: if $s \leq T$.

- Type I Error - **False Match (FM)**: Deciding that two biometrics are from the same identity, while in reality they are from different identities; the frequency with which this occurs is called the False Match Rate (FMR)
- Type II Error – **False Non-Match (FNM)**: Deciding that two biometrics are not from the same identity, while in reality they are from the same identity: the frequency with which this occurs is called the False Non-Match Rate (FNMR)
- **Correct Match**: correctly deciding that two biometric samples match
- **Correct Non-Match**: correctly deciding that the samples do not match

Two kinds of error

$$H_a \Rightarrow B' \neq B$$

Imposter scores



$$H_0 \Rightarrow B' \equiv B$$

Genuine scores

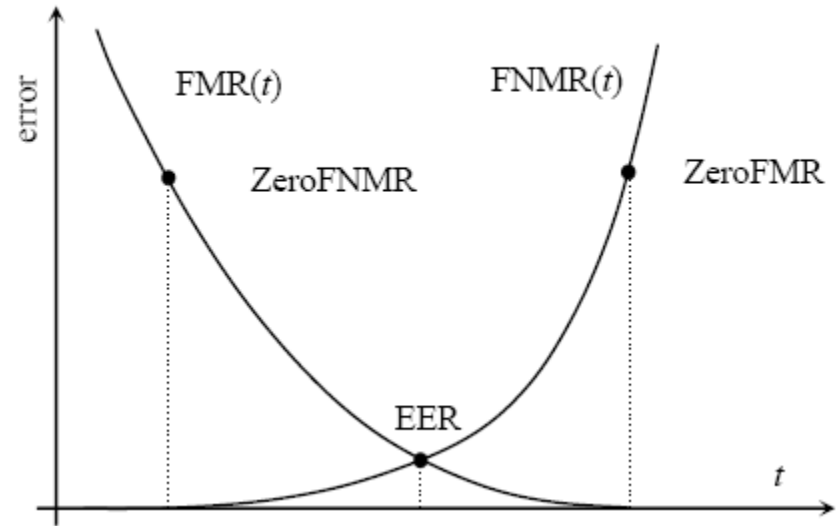
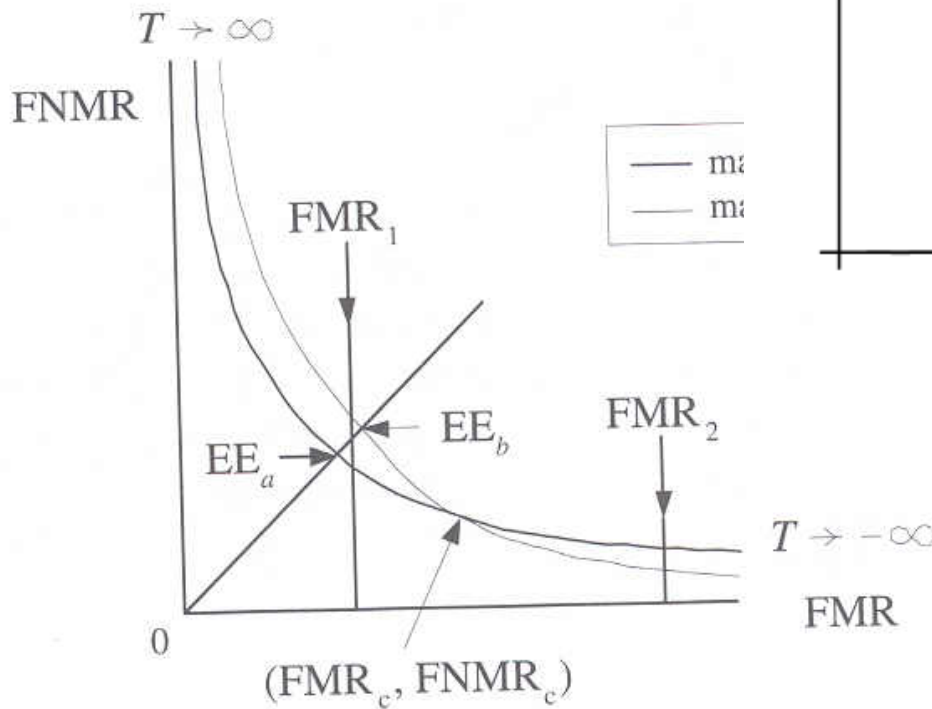
$$\text{FNMR}(T) = \int_{s=-\infty}^T p_m(s) ds$$

$$\text{FMR}(T) = \int_{s=T}^{\infty} p_n(s) ds$$

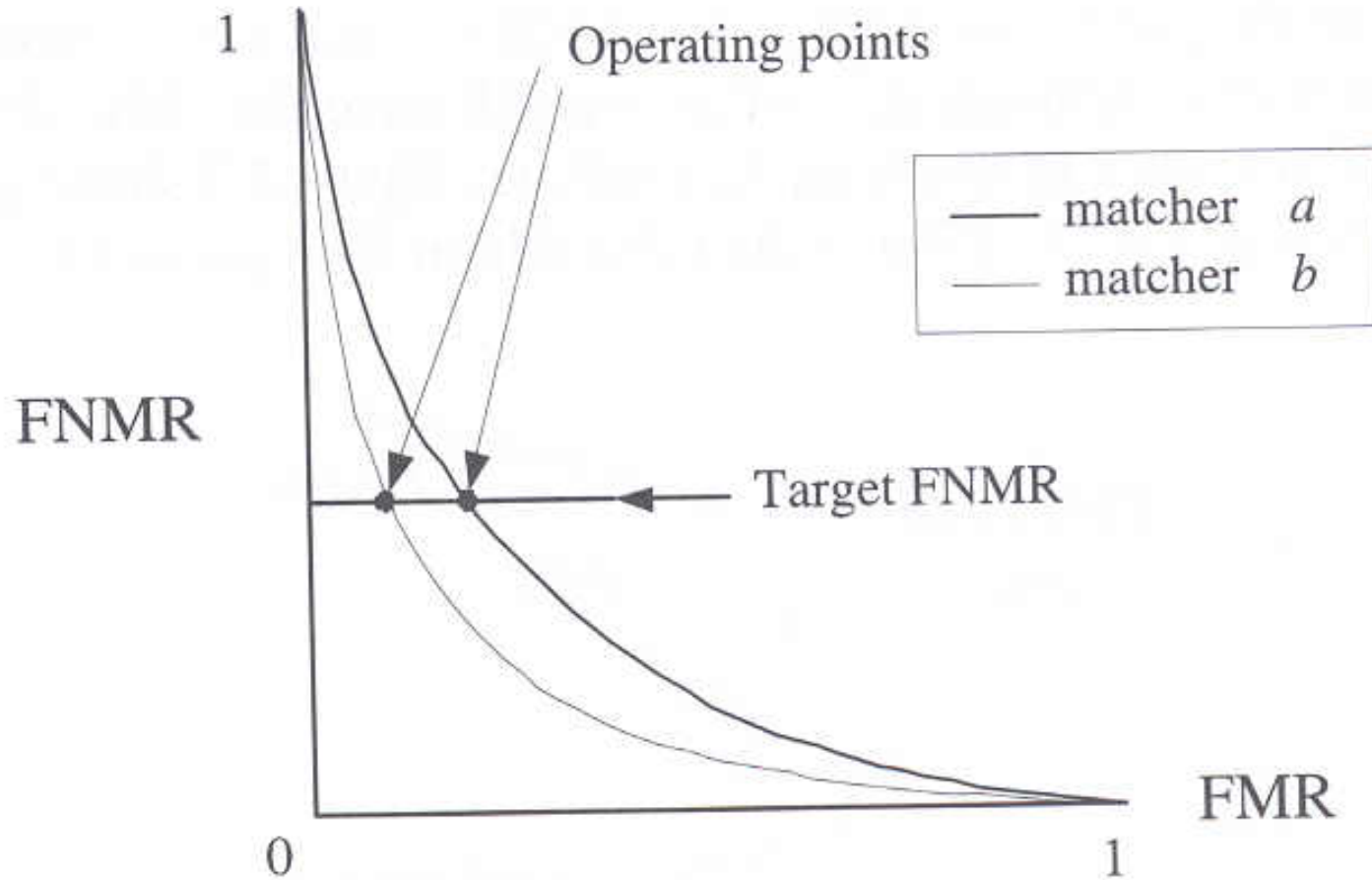
The Equal Error Rate



-ROC:



Using the ROC Curve



Matcher *b* is always better than matcher *a* since for every possible FNMR, its FMR is lower

ROC curve – example on DB1

- 2800 genuine pairs, 4950 imposters pairs

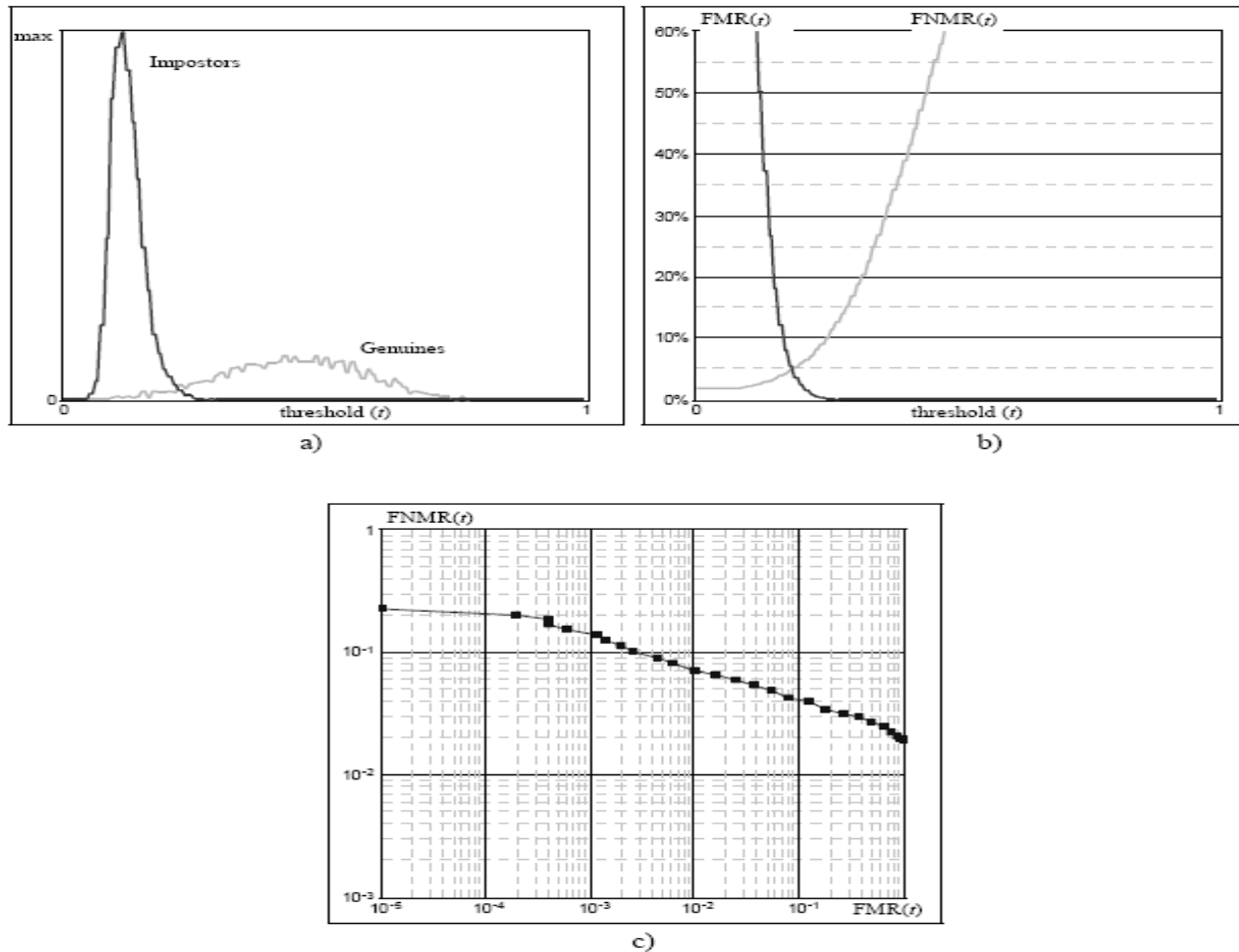


Figure 1.5. Evaluation of a fingerprint verification algorithm over FVC2002 database DB1 (Maio et al., 2002b): a) genuine and impostor distributions were computed from 2800 genuine pairs and 4950 impostor pairs, respectively; b) $FMR(t)$ and $FNMR(t)$ are derived from the score distributions in a); c) DET curve is derived from the $FMR(t)$ and $FNMR(t)$ curves in b).



FVC 2004 results

- <http://bias.csr.unibo.it/fvc2004/>
- <http://www.nist.gov/srd/biomet.htm>

Algorithm	EER(%)	Avg Enroll Time (sec)	Avg Match Time (sec)	Avg Model Size (KB)
Bioscrypt Inc.	2.07	0.08	1.48	24
Sonda Ltd	2.10	2.07	2.07	1.3
Chinese Academy of Sciences	2.30	0.35	0.67	16.4
Gevarius	2.45	0.69	0.71	2.0
Jan Lunter	2.90	1.01	1.19	3.1

- Database:
 - DB1: optical sensor "V300" by CrossMatch
 - DB2: optical sensor "U.are.U 4000" by Digital Persona
 - DB3: thermal sweeping sensor "FingerChip FCD4B14CB" by Atmel
 - DB4: synthetic fingerprints

FVC COMPARISION

NIST Fingerprint Vendor Technology Evaluation

– <http://fpvte.nist.gov/>

–NIST Proprietary Fingerprint Template (PFT) Testing

– <http://fingerprint.nist.gov/SDK/>

	DB1	DB2	DB3	DB4
FVC2000	2.30%	1.39%	4.34%	3.38%
FVC2002	0.20%	0.17%	0.63%	0.16%
FVC2004	1.61%	2.32%	1.34%	0.81%
FVC2006	5.88%	0.05%	1.59%	0.39%

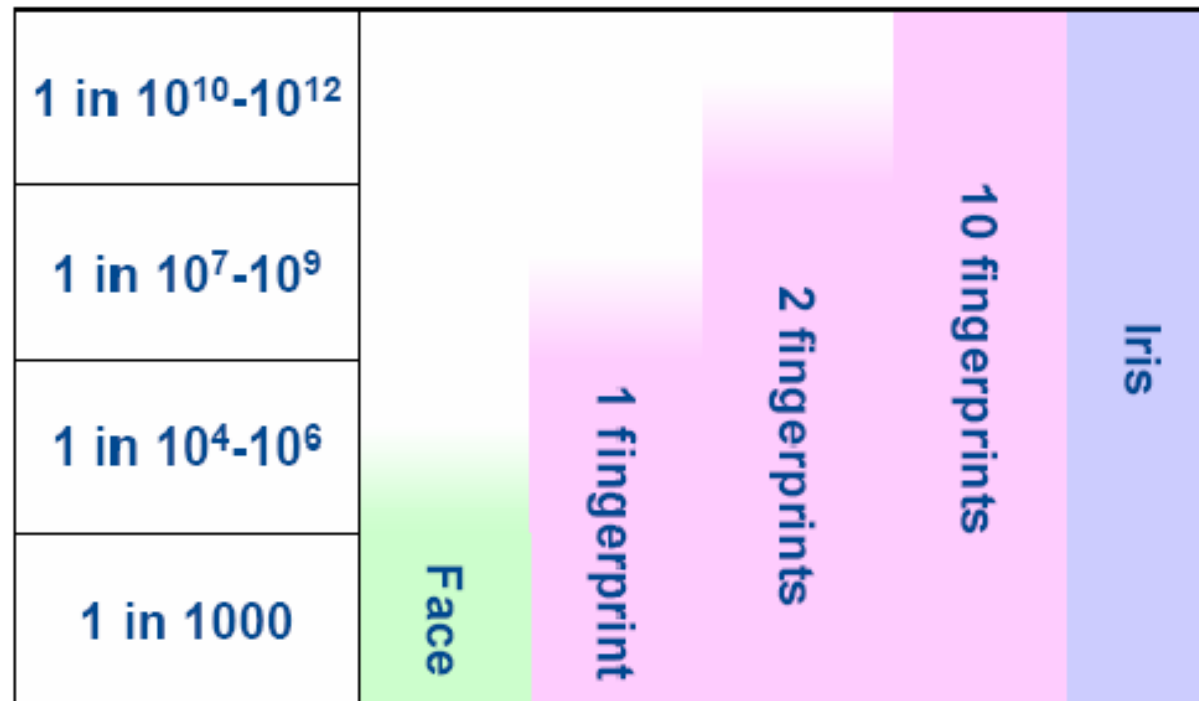
Table 4.3. Average accuracy (EER) of the three best performing algorithms over the different FVC databases. A direct comparison across the different competitions is not possible due to the use of databases of unequal difficulty.

Accuracy and scalability



FRR lower than

Suitable biometrics



Mansfield 2004



Convenience vs Security



- The higher the FRR, the less convenient an application is because more subjects are incorrectly recognized and therefore subject to denial of service or the exception handling process

$$\textit{Convenience} = 1 - \textit{FRR}$$

- Similarly, the FAR is often used as some measure of security of a verification system

$$\textit{Security} = 1 - \textit{FAR}$$

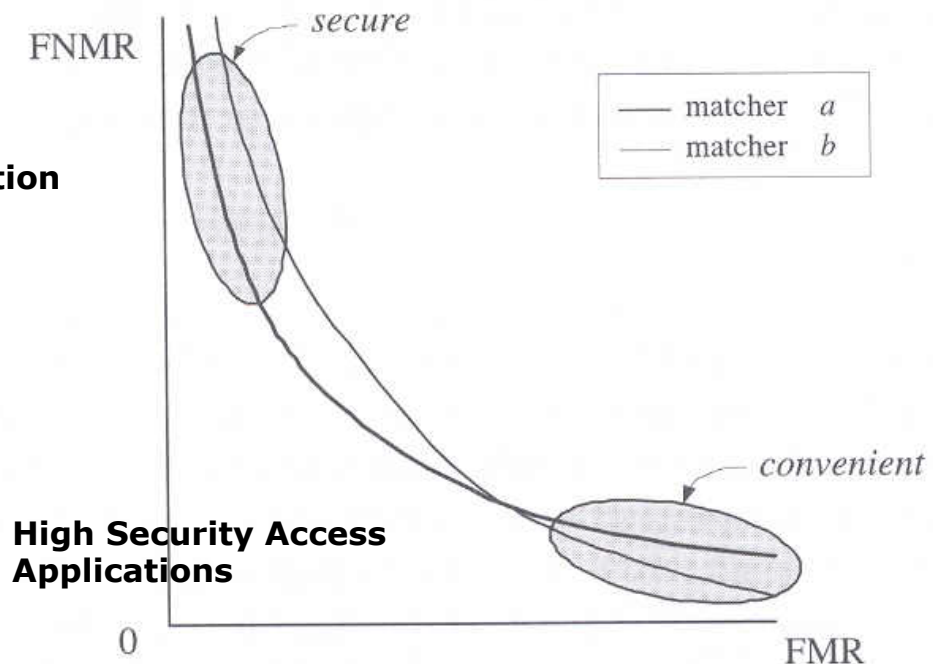
Convenience vs Security

- Convenience of a Biometric
- Convenience of Implementation

$$\text{Convenience} = 1 - \text{FRR}$$

$$\text{Security} = 1 - \text{FAR}$$

Forensic application



Errors specific to biometrics



- The **Failure to Acquire (FTA)** rate is the percentage of the target population that does not possess a particular biometric, i.e. does not deliver a usable biometric sample (e.g. the fingerprint of a brick layer (the ridges have been worn away))
- The **Failure to Enroll (FTE)** rate is the proportion of the population that somehow cannot be enrolled because of limitations of the technology or procedural problems.





Synthetic fingerprint generation

Daniel Novák

6.12, 2011, Prague

**Acknowledgments: Xavier Palathingal, Andrzej Drygajlo,
Handbook of Fingerprint Recognition**



Synthetic fingerprint generation

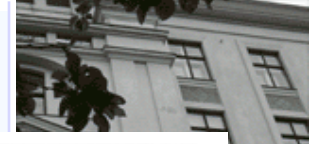


- **Motivation**
 - Accuracy of each algorithm is usually evaluated on relatively small proprietary databases
 - Evaluation on small databases makes the accuracy estimates highly data dependent
 - When the databases are proprietary, the accuracy of various fingerprint matching algorithms cannot be compared directly
- **Synthetic fingerprint generation** can be used to automatically create large databases of fingerprints, thus allowing fingerprint recognition algorithms to be effectively trained, tested, optimized, and compared

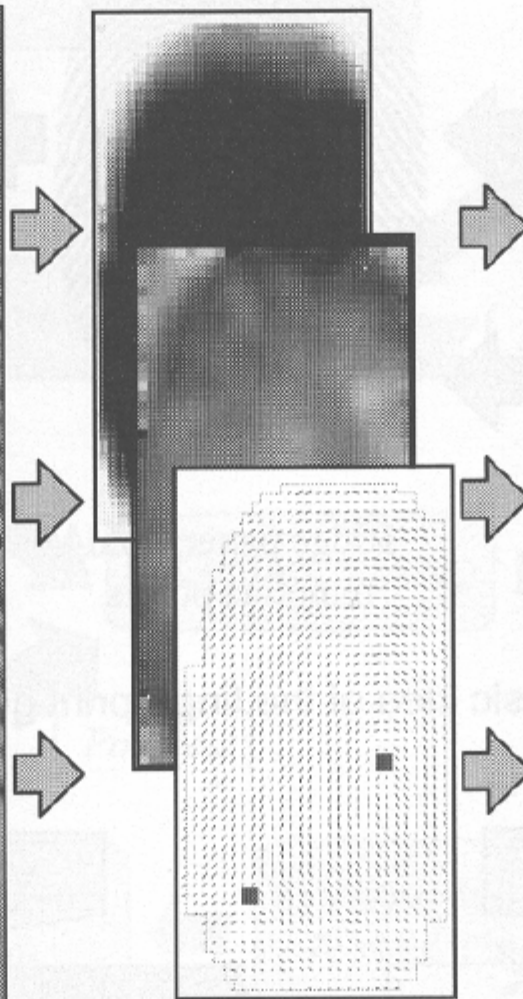
8



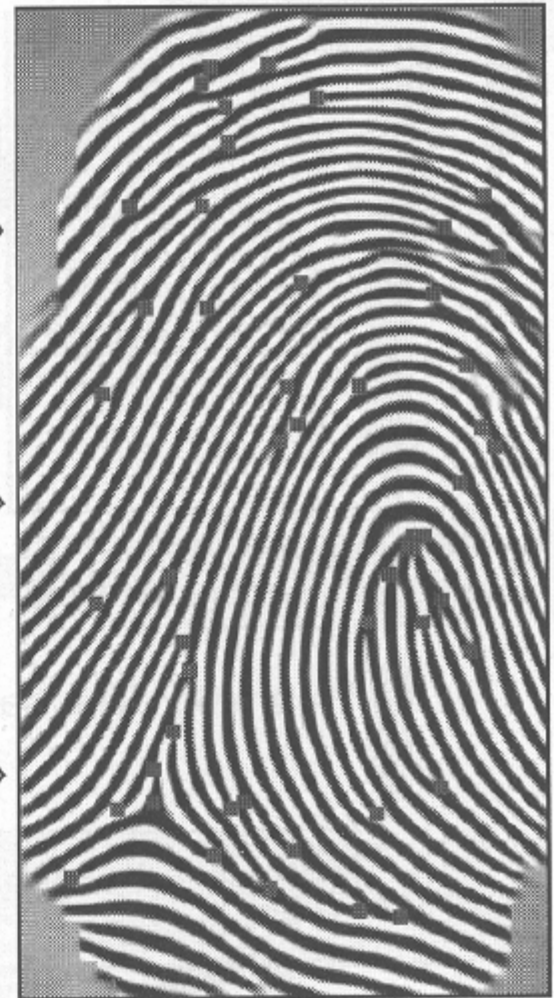
Feature extraction process



Fingerprint image

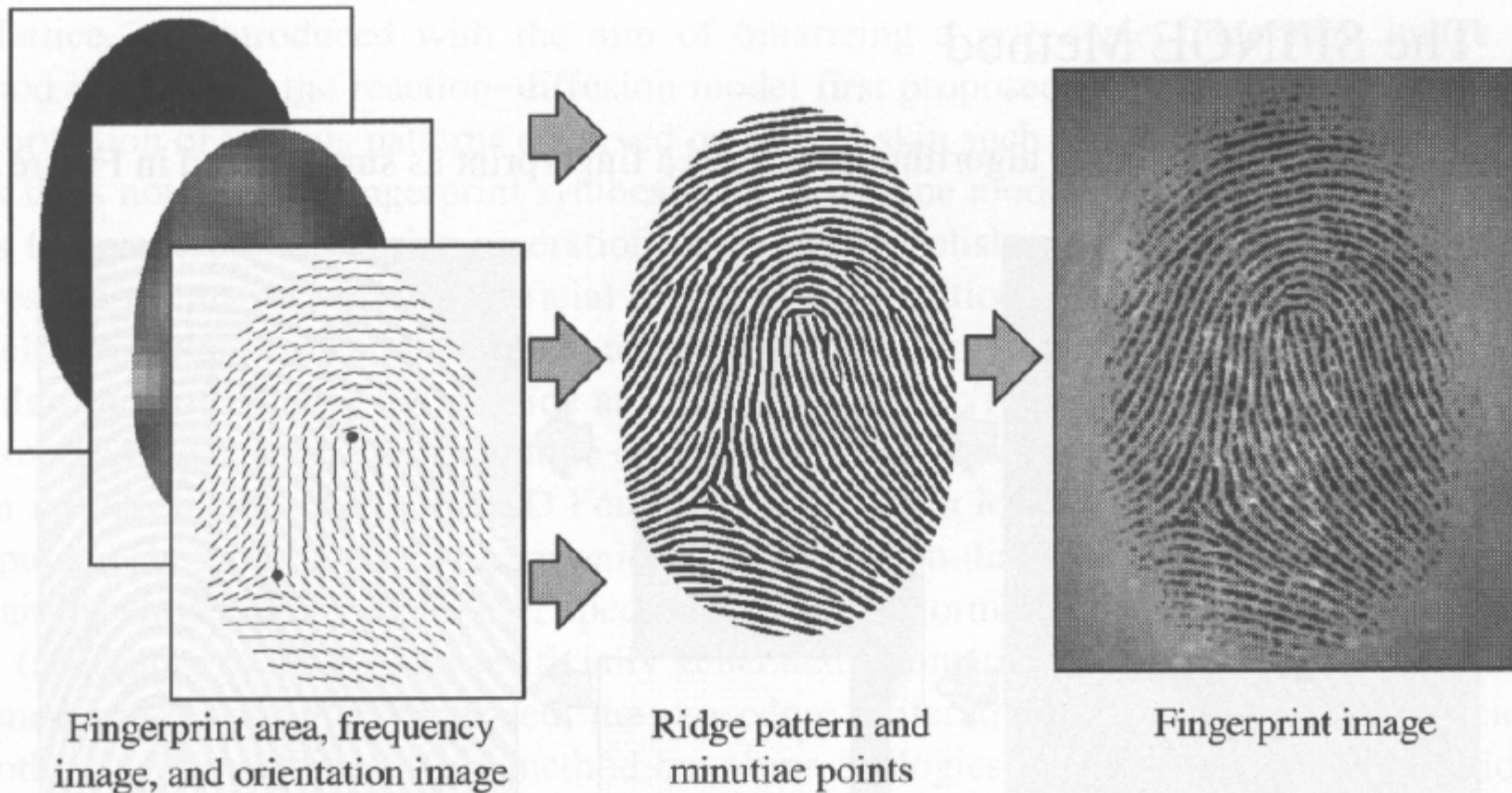


Fingerprint area, frequency image, and orientation image

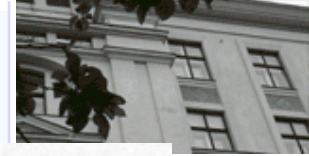


Ridge pattern and minutiae points

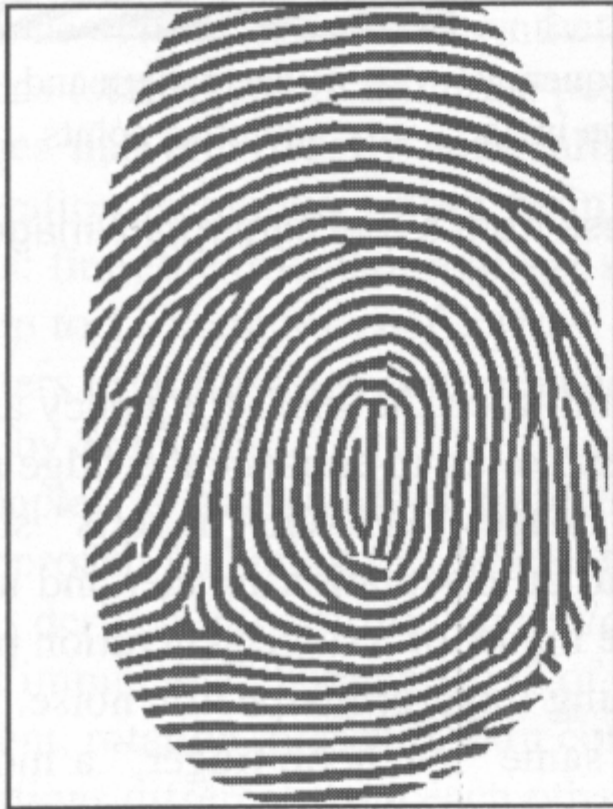
Basic idea



From master to final impression



Individuality data



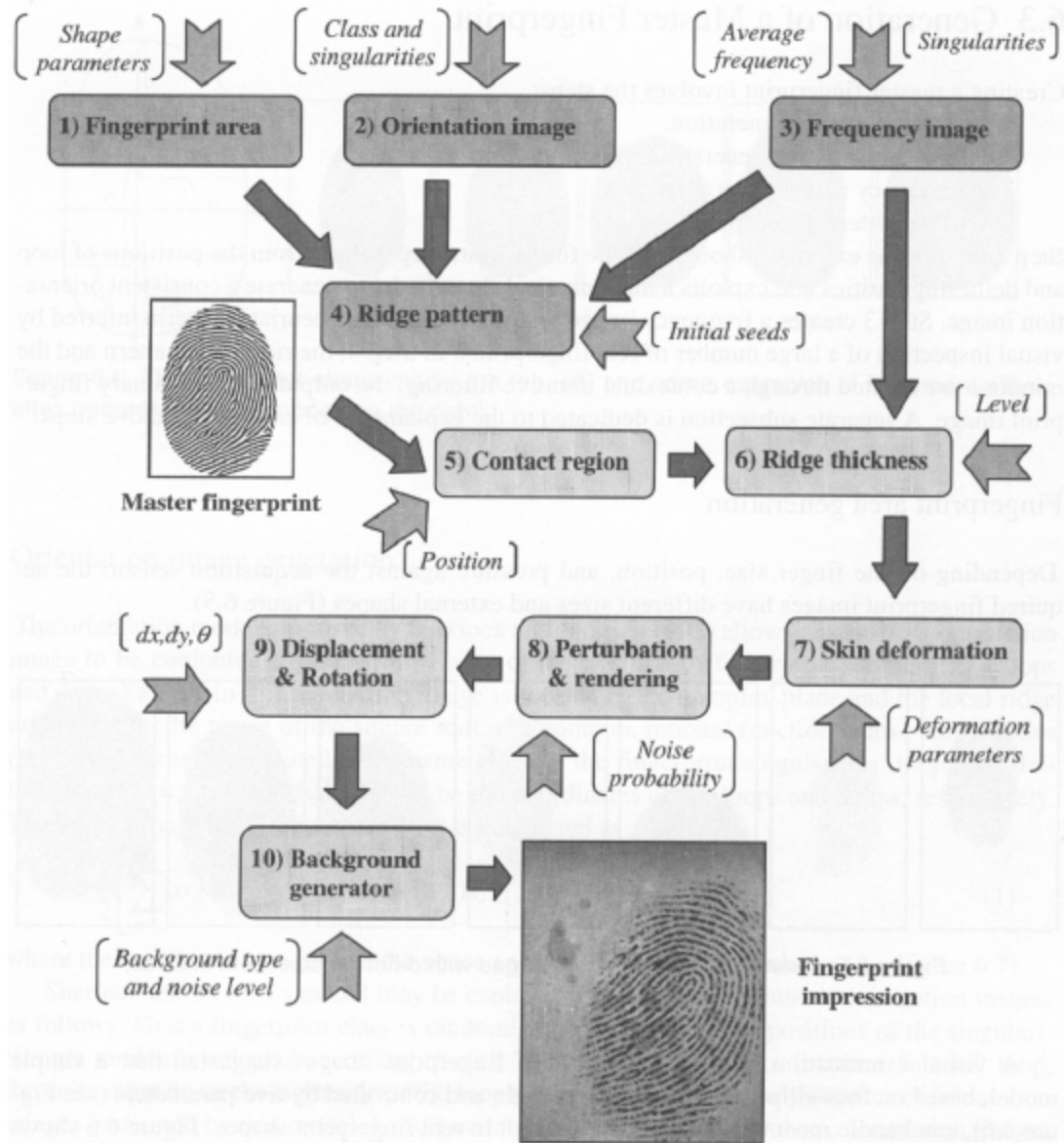
Master fingerprint



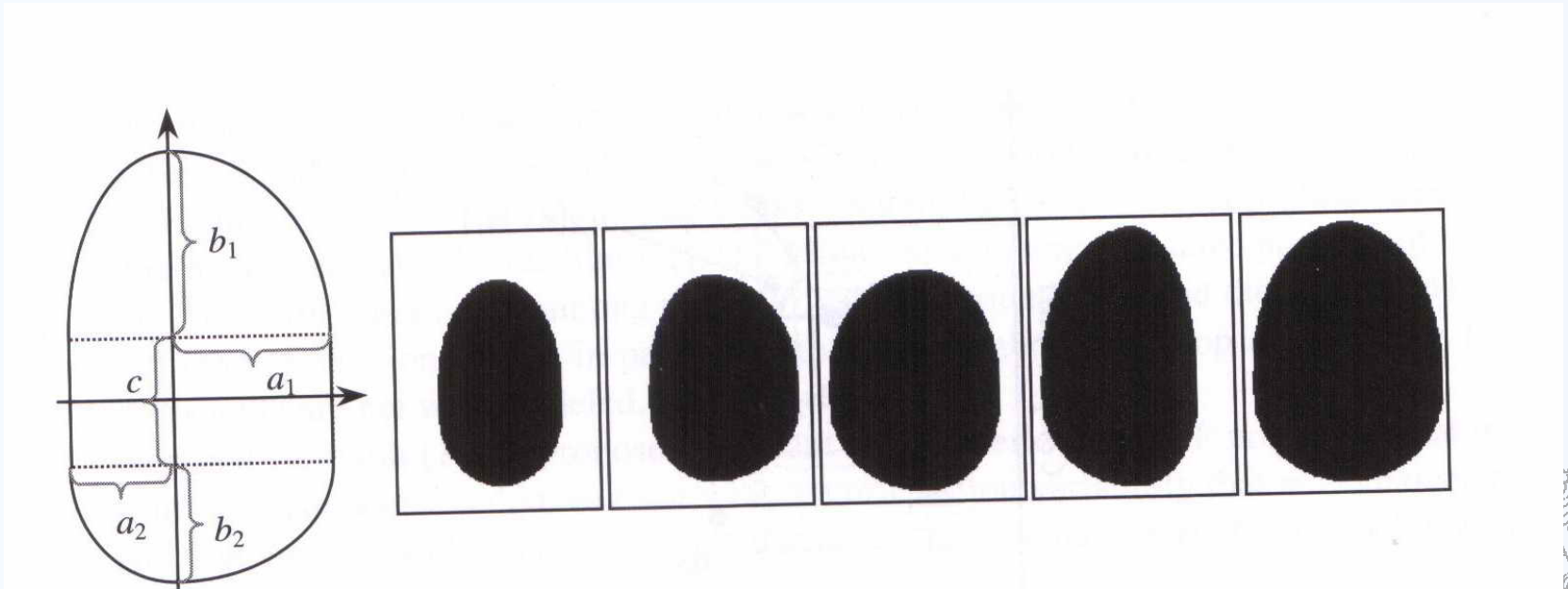
Variability data



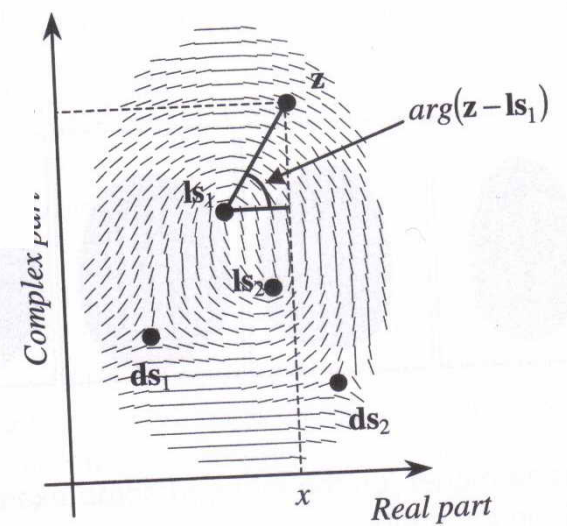
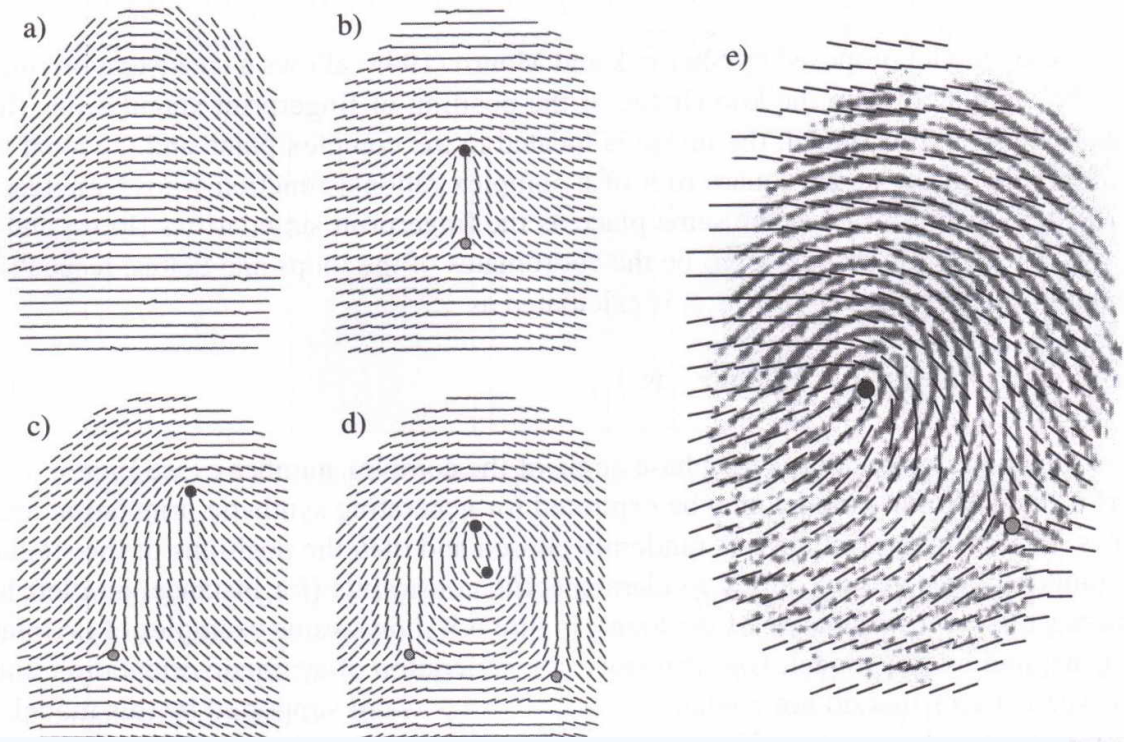
SFINGE



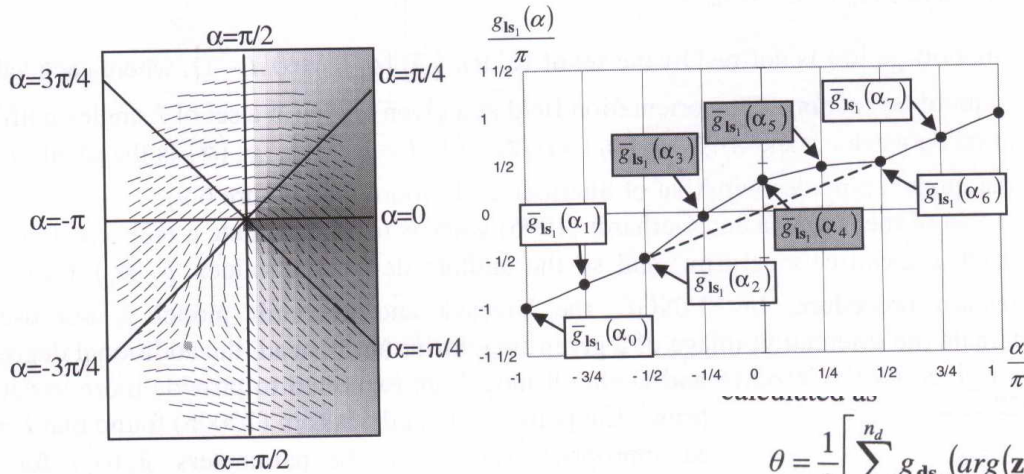
FP area generation



Orientation



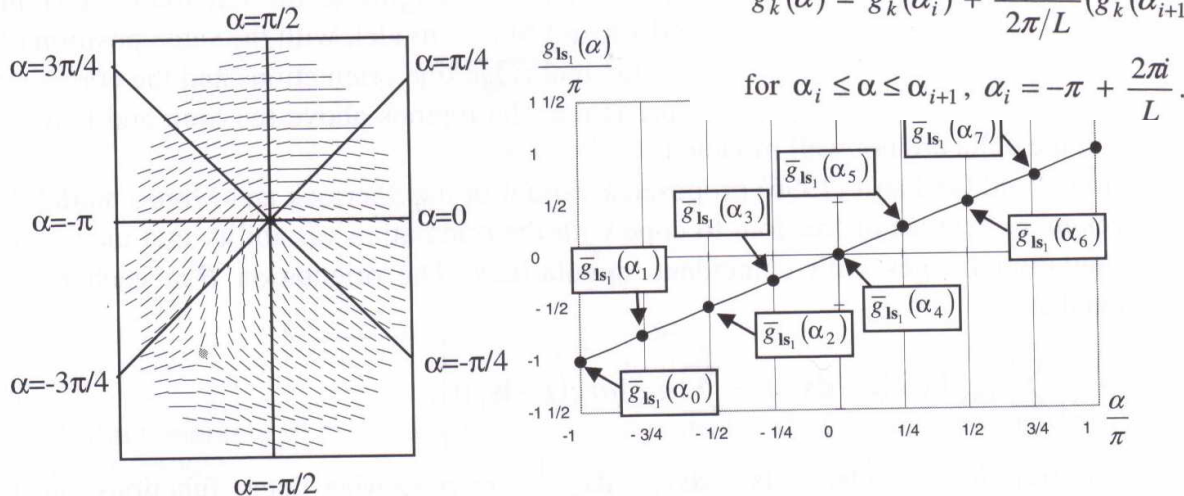
Orientation



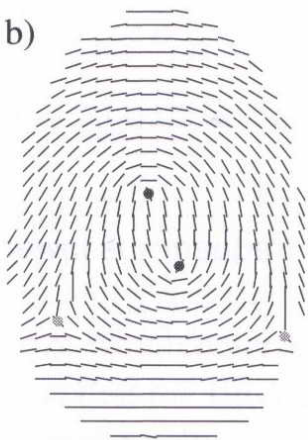
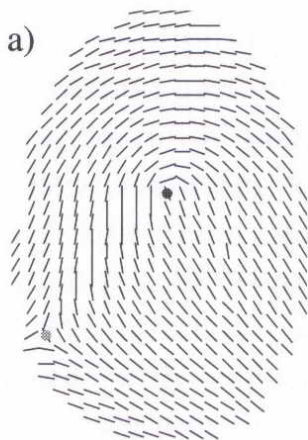
$$\theta = \frac{1}{2} \left[\sum_{i=1}^{n_d} g_{\mathbf{ds}_i}(\arg(\mathbf{z} - \mathbf{ds}_i)) - \sum_{i=1}^{n_c} g_{\mathbf{ls}_i}(\arg(\mathbf{z} - \mathbf{ls}_i)) \right], \quad (2)$$

where $g_k(\alpha)$, for $k \in \{\mathbf{ls}_1, \dots, \mathbf{ls}_{n_c}, \mathbf{ds}_1, \dots, \mathbf{ds}_{n_d}\}$, are piecewise linear functions capable of locally correcting the orientation field with respect to the value given by the Sherlock and Monroe model:

$$g_k(\alpha) = \bar{g}_k(\alpha_i) + \frac{\alpha - \alpha_i}{2\pi/L} (\bar{g}_k(\alpha_{i+1}) - \bar{g}_k(\alpha_i)), \quad (3)$$



Orientation



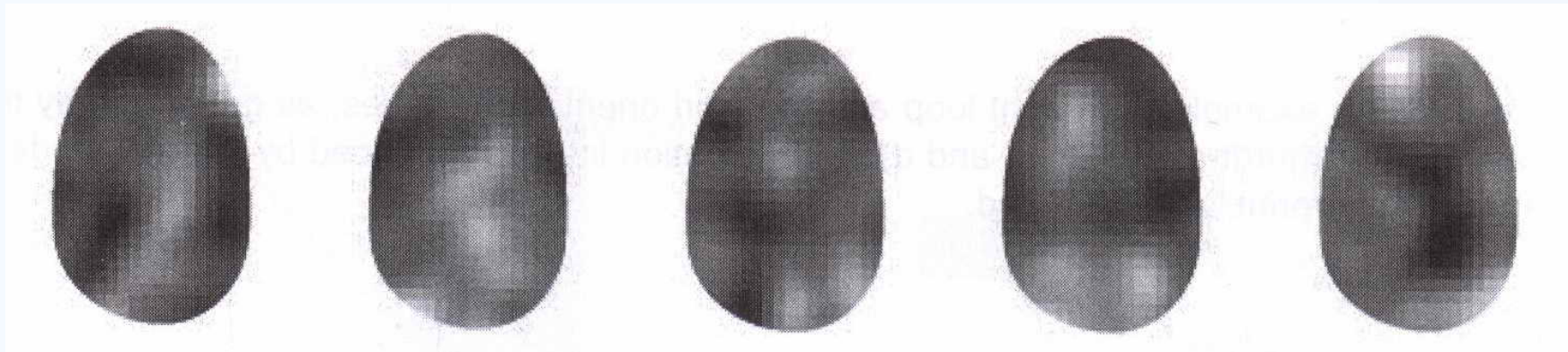
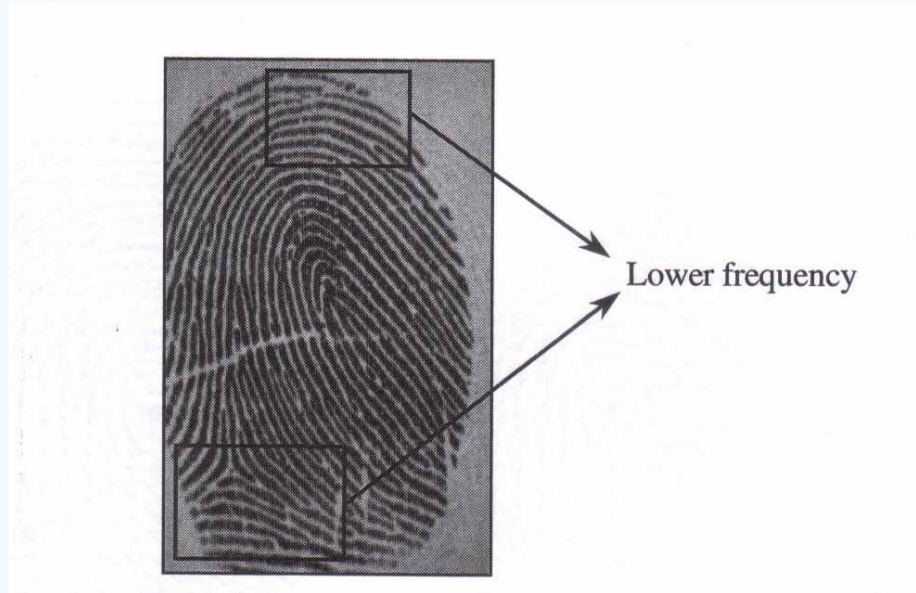
Sherlock and Monro



Vizcaya and Gerhardt



Frequency

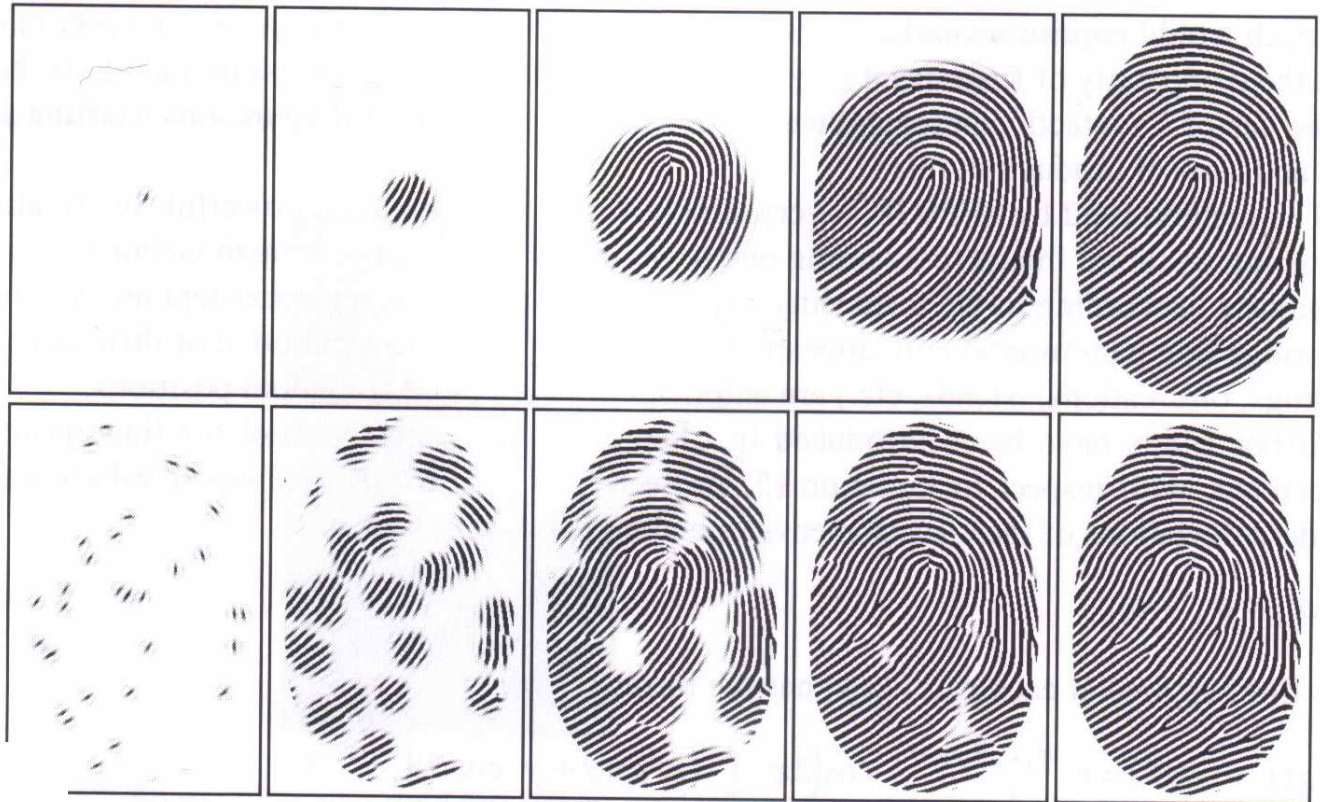


Ridge line

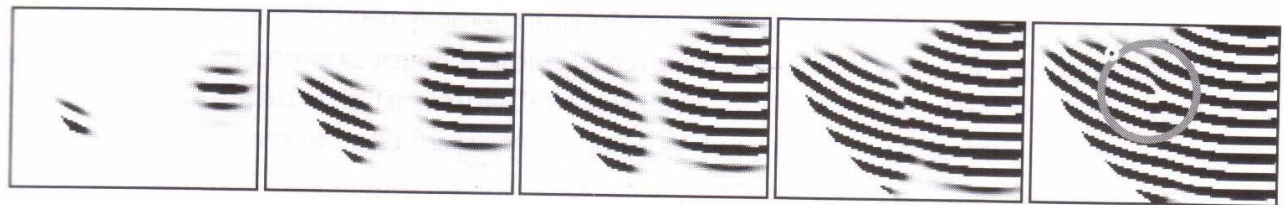


- Gabor filter
- Seeds

$$\sigma_x = \sigma_y = \sigma$$

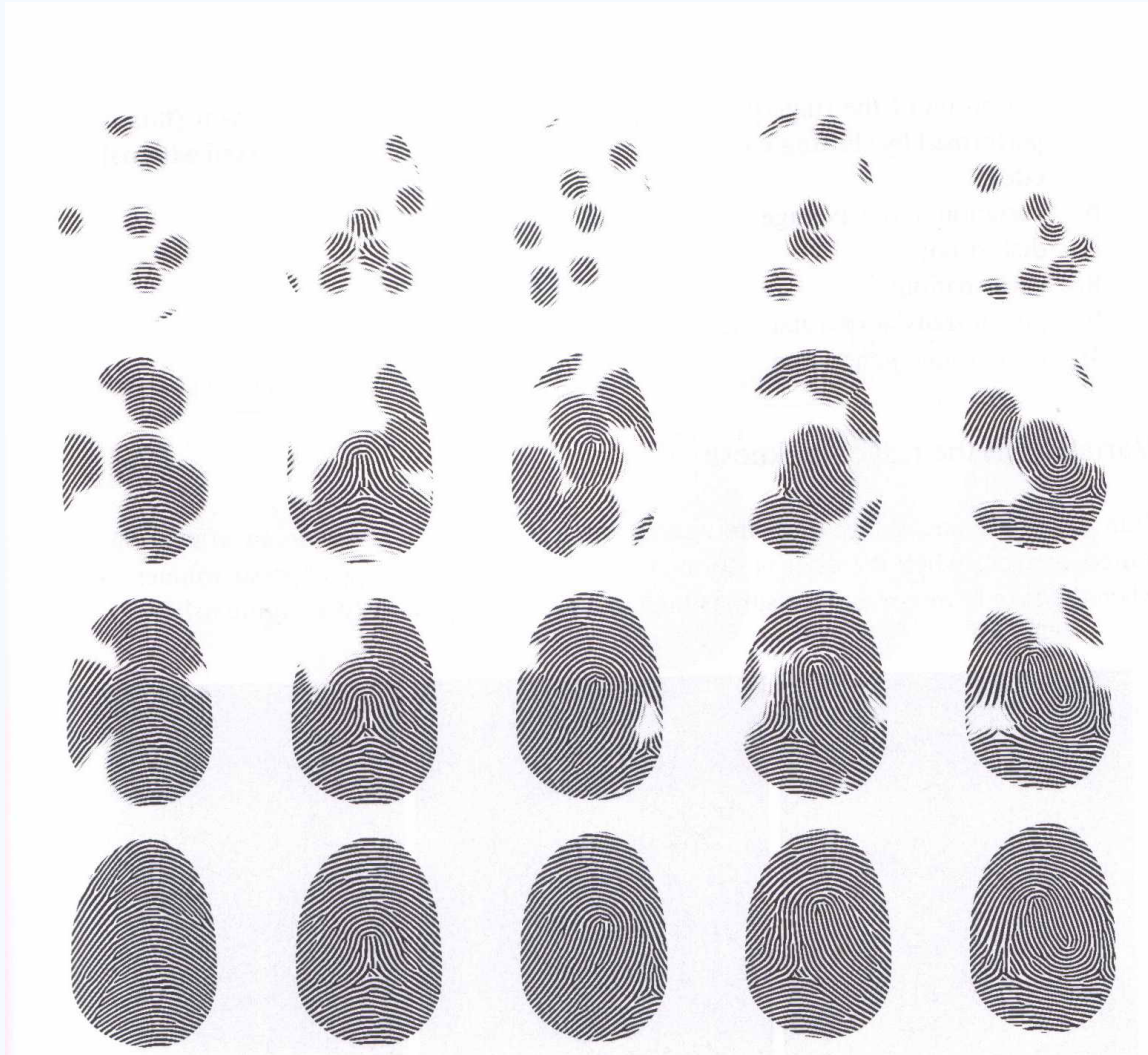


$$e^{-\left(\left(\frac{3}{2f}\right)^2 / 2\sigma^2\right)} = 10^{-3}$$

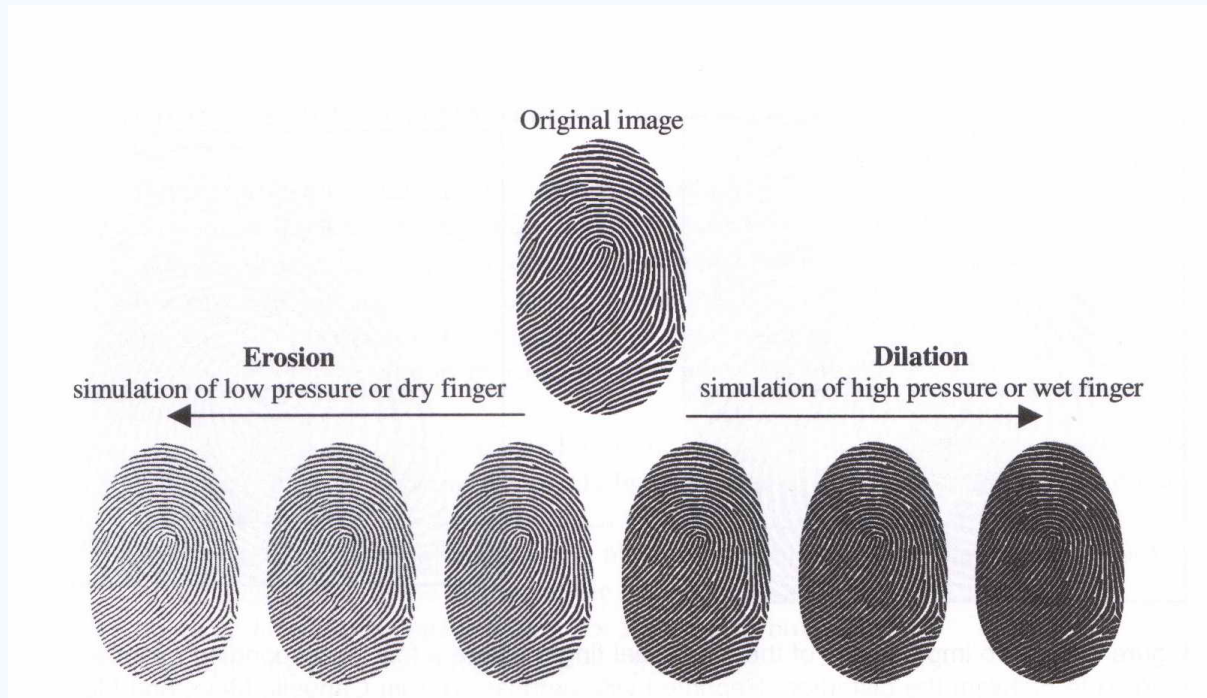


$$g(x, y : \theta, f) = e^{-((x^2 + y^2) / 2\sigma^2)} \cdot \cos[2\pi \cdot f \cdot (x \cdot \sin \theta + y \cdot \cos \theta)],$$

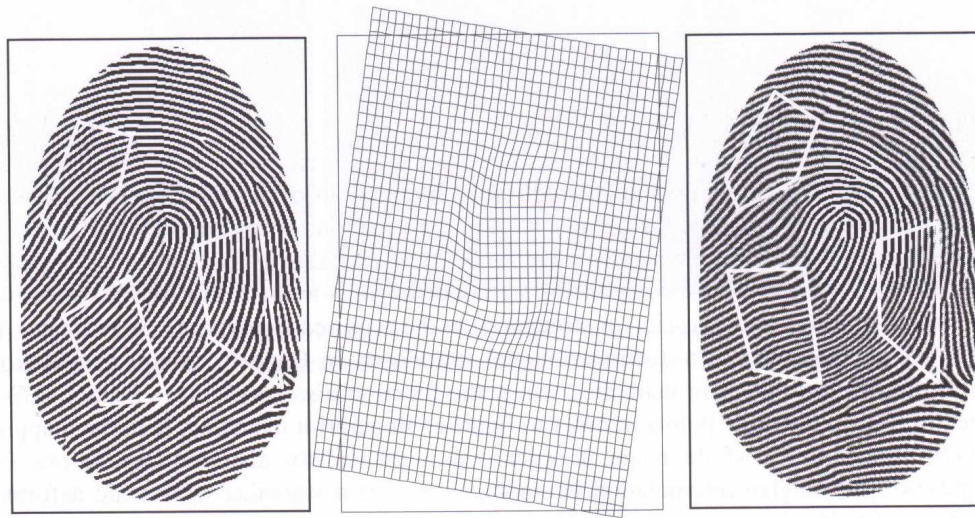
Ridge line



Ridge thickness

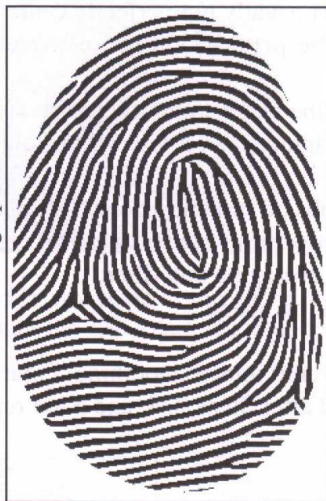


Distortion

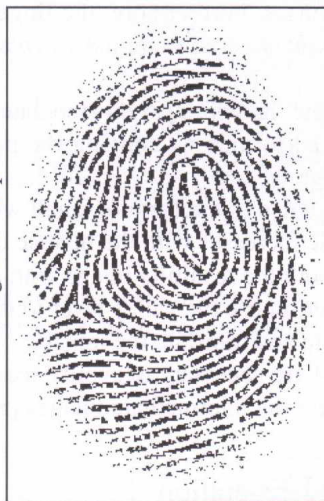


Perturbation & Translation

Master fingerprint



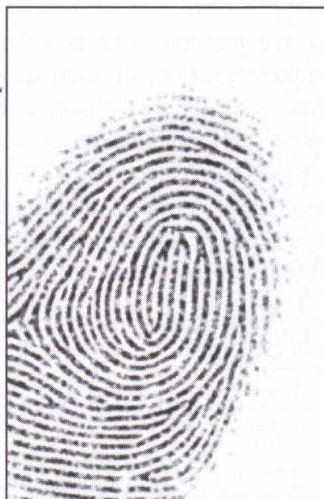
Noising: after Step 2



Noising: after Step 4



Global translation/rotation: after Step 5



Background



- $\bar{\mathbf{b}} = \frac{1}{m} \sum_{\mathbf{b} \in B} \mathbf{b}$ be their mean vector;
- $\mathbf{C} = \frac{1}{m} \sum_{\mathbf{b} \in B} (\mathbf{b} - \bar{\mathbf{b}})(\mathbf{b} - \bar{\mathbf{b}})^T$ be their covariance matrix;
- $\Phi \in \mathcal{R}^{n \times n}$ be the orthonormal matrix that diagonalizes \mathbf{C} ; that is, $\Phi^T \mathbf{C} \Phi = \Lambda$,
 $\Lambda = \text{Diag}(\lambda_1, \lambda_2, \dots, \lambda_n)$, $\Phi = [\varphi_1, \varphi_2, \dots, \varphi_n]$,
where λ_i and φ_i , $i = 1..n$ are the eigenvalues and the eigenvectors of \mathbf{C} , respectively.

1. a k -dimensional vector $\mathbf{y} = [y_1, y_2, \dots, y_k]$ is randomly generated according to k normal distributions: $y_j = N(0, \lambda_j^{1/2})$, $j = 1..k$;
2. the corresponding n -dimensional vector \mathbf{b} is obtained as: $\mathbf{b} = \Phi_k \mathbf{y} + \bar{\mathbf{b}}$.

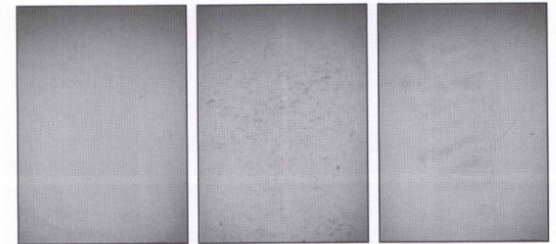
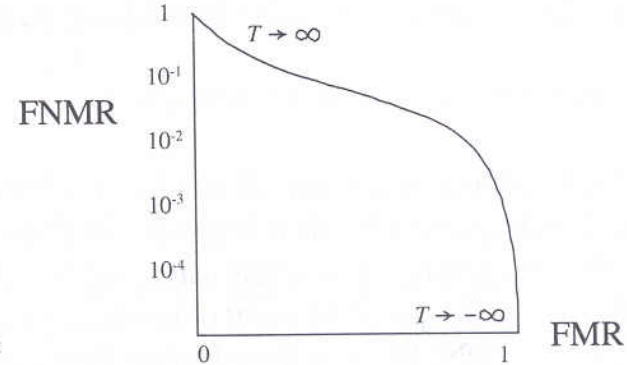
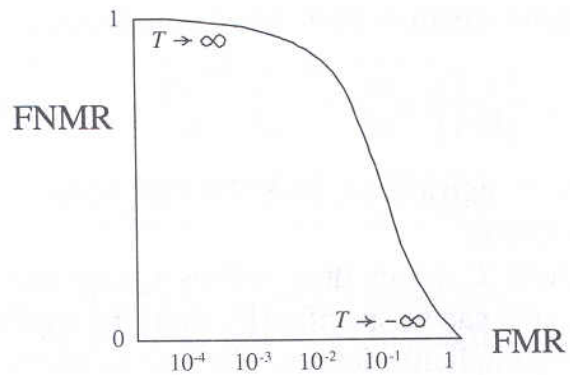


Figure 6.22. Examples of background-only images (acquired from an optical scanner) used for training the background generator.

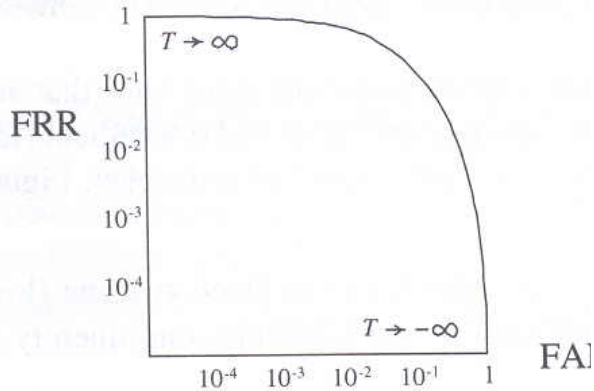


Figure 6.23. Three synthetic images with backgrounds generated according to the model (the parameters used for training are $m = 65$ and $k = 8$).

Variations of ROCs



Semi-log plots



Log-log plot

