

# Constraint-Handling in Evolutionary Algorithms

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Substantial part of this material is based on slides for tutorial  
'Constraint-Handling Techniques used with Evolutionary Algorithms'  
presented at GECCO 2011 by Carlos A. Coello Coello and  
the technical report Carlos A. Coello Coello: A Survey of Constraint Handling Techniques used with Evolutionary Algorithms.  
See <http://dl.acm.org/citation.cfm?doid=2001858.2002130> and  
<http://citeseer.ist.psu.edu/viewdoc/download?doi=10.1.1.43.9288&rep=rep1&type=pdf>



<http://cw.felk.cvut.cz/doku.php/courses/a0m33eoa/start>













































































# Stochastic Ranking + ES

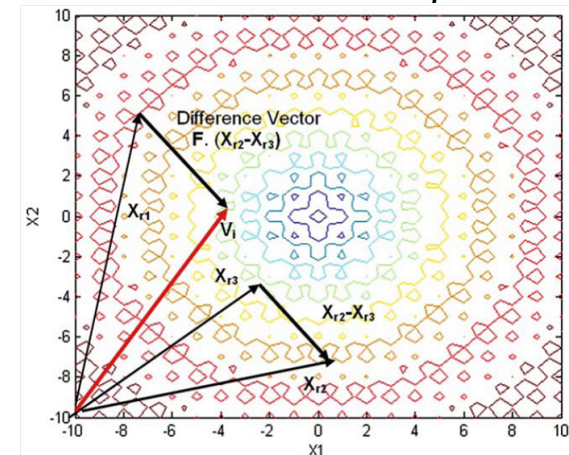
## Stochastic ranking coupled to evolution strategy

- SR used to rank solutions in the parental population.
- *Differential variation* used to better adjust the search direction (lines 8-10), performed once per a parent. Normally the search is biased toward a grid aligned with the coordinate system; Adapting the full covariance matrix would help as well (and better), but it is too costly.
- *Exponential smoothing* used to reduce fluctuations on standard deviations  $\sigma'_k$  (line 14).

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1 Initialize:  $\sigma'_k := (\bar{\mathbf{x}}_k - \underline{\mathbf{x}}_k) / \sqrt{n}$ ,  $\mathbf{x}'_k = \mathbf{x}_k + (\bar{\mathbf{x}}_k - \underline{\mathbf{x}}_k) \mathbf{U}_k(0, 1)$ 
2 while termination criteria not satisfied do
3   evaluate:  $f(\mathbf{x}'_k)$ ,  $\mathbf{g}^+(\mathbf{x}'_k)$ ,  $k = 1 \dots, \lambda$ 
4   rank the  $\lambda$  points and copy the best  $\mu$  in their ranked order:
5    $(\mathbf{x}_i, \sigma_i) \leftarrow (\mathbf{x}'_{i;\lambda}, \sigma'_{i;\lambda})$ ,  $i = 1, \dots, \mu$ 
6   for  $k := 1$  to  $\lambda$  do
7      $i \leftarrow \text{mod}(k - 1, \mu) + 1$ 
8     if  $(k < \mu)$  do (differential variation)
9        $\sigma'_k \leftarrow \sigma_i$ 
10       $\mathbf{x}'_k \leftarrow \mathbf{x}_i + \gamma(\mathbf{x}_1 - \mathbf{x}_{i+1})$ 
11     else (standard mutation)
12       $\sigma'_{k,j} \leftarrow \sigma_{i,j} \exp(\tau' N(0, 1) + \tau N_j(0, 1))$ ,  $j = 1, \dots, n$ 
13       $\mathbf{x}'_k \leftarrow \mathbf{x}_i + \sigma'_k \mathbf{N}(0, 1)$ 
14       $\sigma'_k \leftarrow \sigma_i + \alpha(\sigma'_k - \sigma_i)$ 
15   od
16 od
17 od
  
```

Differential variation operator





















# Random Keys for the Network Design Problems

## Constructing the tree network from the NetKey vector

1. Let  $i = 0$ ,  $G$  be an empty graph with  $n$  nodes, and  $\vec{r}_i^s$  the sequence with length  $l = n(n-1)/2$  that could be constructed from the NetKey vector  $\vec{r}_i$ . All possible links of  $G$  are numbered from 1 to  $l$ .
2. Let  $j$  be the number at the  $i$ th position of  $\vec{r}_i^s$ .
3. If the insertion of the link with number  $j$  in  $G$  would not create a cycle, then insert the link with number  $j$  in  $G$ .
4. Stop, if there are  $n - 1$  links in  $G$ .
5. Increment  $i$  and continue with step 2.

Ex.:

position	1	2	3	4	5	6	7	8	9	10
NetKey	0.55	0.73	0.09	0.23	0.40	0.82	0.65	0.85	0.75	0.90
link	A-B	A-C	A-D	A-E	B-C	B-D	B-E	C-D	C-E	D-E

