

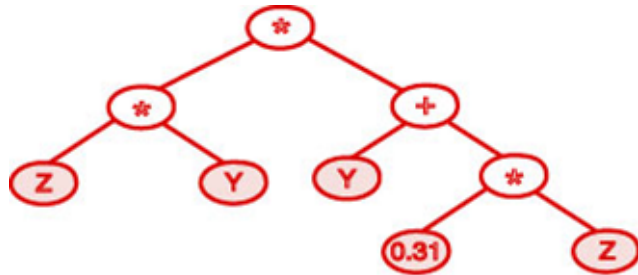
Genetic Programming

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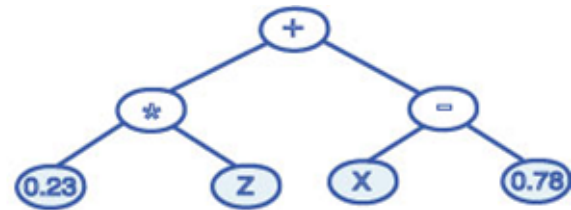


<http://cw.felk.cvut.cz/doku.php/courses/a0m33eoa/start>

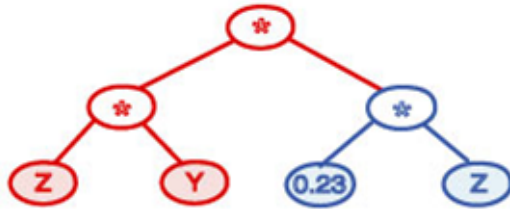
GP: Standard Crossover



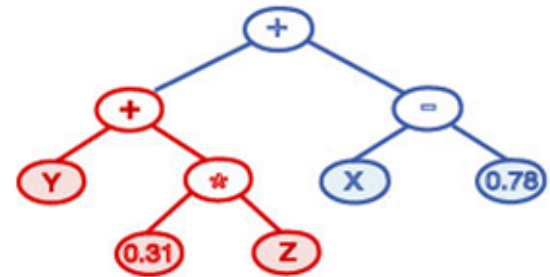
Parent 1: $Z * Y * (Y + 0.31 * Z)$



Parent 2: $0.23 * Z + X - 0.78$



Child 1: $0.23 * Y * Z^2$



Child 2: $Y + 0.31 * Z + X - 0.78$

Example of GP in Action: Trigonometric Identity cont.

1. run, 13th generation

$$(-(-1(*(\sin x)(\sin x))))(*(\sin x)(\sin x))$$

which equals (after editing) to $1 - 2 * \sin^2 x$

2. run, 34th generation

$$(-1(*(*(\sin x)(\sin x))2))$$

which is just another way of writing the same expression.

3. run, 30th generation

$$\begin{aligned} &(\sin \quad (-(-2(* x 2)) \\ &\quad (\sin(\sin(\sin(\sin(\sin(\sin(*(\sin \quad (\sin 1)) \\ &\quad \quad \quad \quad \quad \quad \quad (\sin 1)) \\ &)))))))))) \end{aligned}$$

The expression on the second and third row returns a value almost equal to $\pi/2$ so the discovered identity is

$$\cos(2x) = \sin(\pi/2 - 2x).$$

GP: Constant Creation

In many problems exact real-valued constants are required to be present in the correct solution (evolved program tree) \implies GP must have the ability to create arbitrary real-valued constant.

Ephemeral random constant \mathfrak{R} – a special terminal.

- Initialization – whenever the ephemeral random constant \mathfrak{R} is chosen for any endpoint of the tree during the creation of the initial population, a random number of a specified data type in a specified range is generated and attached to the tree at that point.

Each occurrence of this terminal symbol invokes a generation of a unique value.

- Once these values are generated and inserted into initial program trees, these constants remain fixed.
- The numerous different random constants will become embedded in various subtrees in evolving trees.

Other constants can be further evolved by crossing the existing subtrees, such a process being driven by the goal of achieving the highest fitness.

The pressure of fitness function determines both the directions and the magnitudes of the adjustments in numerical constants.

GP Initialization: Probabilistic Tree-Creation Method 1

PTC1 is a modification of GROW that

- allows the user to define probabilities of appearance of functions within the tree,
- gives user a control over expected desired expected tree size, and guarantees that, on average, trees will be of that size.
- does not give the user any control over the variance in tree sizes.

Given:

- maximum depth bound D
- function set F consisting of N and T
- computed probability of choosing a nonterminal p
- probabilities q_t and q_n for each $t \in T$ and $n \in N$
- arities b_n of all nonterminals $n \in N$
- **probability p of choosing a nonterminal over a terminal given the expected tree size E_{tree} calculated according to**

$$p = \frac{1 - \frac{1}{E_{tree}}}{\sum_{n \in N} q_n b_n}$$

	PTC1(depth d)
	Returns: a tree of depth $\leq D - d$
1	if($d = D$) return a terminal from T (by q_t probabilities)
2	else if(rand $< p$)
3	choose a nonterminal n from N (by q_n probabilities)
4	for each argument a of n
5	fill a with PTC1($d + 1$)
6	return n
7	else return a terminal from T (by q_t probabilities)

Probabilistic Tree-Creation Method PCT1: Proof of p

- The expected number of nodes at depth d is $E_d = g^d$, for $g \geq 0$ (the expected number of children to a newly generated node).
- E_{tree} is the sum of E_d over all levels of the tree, that is

$$E_{tree} = \sum_{d=0}^{\infty} E_d = \sum_{d=0}^{\infty} g^d$$

From the geometric series, for $g \geq 0$

$$E_{tree} = \begin{cases} \frac{1}{1-g}, & \text{if } g < 1 \\ \infty, & \text{if } g \geq 1. \end{cases}$$

Probabilistic Tree-Creation Method PCT1: Proof of p

- From

$$E_{tree} = \frac{1}{1 - pb}$$

we get

$$p = \frac{1 - \frac{1}{E_{tree}}}{b}$$

GP: Selection

Commonly used are the fitness proportionate roulette wheel selection or the tournament selection.

Greedy over-selection is recommended for complex problems that require large populations (> 1000) – the motivation is to increase efficiency by increasing the chance of being selected to the fitter individuals in the population

- rank population by fitness and divide it into two groups:
 - group I: the fittest individuals that together accounting for $c = x\%$ of the sum of fitness values in the population,
 - group II: remaining less fit individuals.
- 80% of the time an individual is selected from group I in proportion to its fitness; 20% of the time, an individual is selected from group II.
- For population size = 1000, 2000, 4000, 8000, $x = 32\%$, 16%, 8%, 4%.
%’s come from rule of thumb.

GP: Crossover Operators

Standard crossover operators used in GP, like standard 1-point crossover, are designed to ensure just the syntactic closure property.

- On the one hand, they produce syntactically valid children from syntactically valid parent.
- On the other hand, the only semantic guidance of the search is from the fitness measured by the difference of behavior of evolving programs and the target programs.

This is very different from real programmers' practice where any change to a program should pay heavy attention to the change in semantics of the program.

To remedy this deficiency in GP genetic operators making use of the semantic information has been introduced:

- **Semantically Driven Crossover (SDC)**

[Beadle08] Beadle, L., Johnson, C.G.: Semantically Driven Crossover in Genetic Programming, 2008.

- **Semantic Aware Crossover (SAC)**

[Nguyen09] Nguyen, Q.U. et al.: Semantic Aware Crossover for Genetic Programming: The Case for Real-Valued Function Regression, 2009.

Automatically Defined Functions: Motivation

Hierarchical problem-solving (“divide and conquer”) may be advantageous in solving large and complex problems because the solution to an overall problem may be found by decomposing it into smaller and more tractable subproblems in such a way that the solutions to the subproblems are reused many times in assembling the solution to the overall problem.

Automatically Defined Functions (Koza94) – idea similar to reusable code represented by subroutines in programming languages.

- Subroutines are reused with different instantiation of dummy variables.
- Reuse eliminates the need to “reinvent the wheel” on each occasion when a particular sequence of steps may be useful.
- Reuse makes it possible to exploit a problem’s modularities, symmetries and regularities.
- Code encapsulation – protection from crossover and mutation.
- Simplification – less complex code, easier to evolve.
- Efficiency – acceleration of the problem-solving process (i.e. the evolution).

[Koza94] Genetic Programming II: Automatic Discovery of Reusable Programs, 1994

GP with ADFs: Even-4-Parity Function

An example of solution with 74 nodes.

```
(LIST3 (NAND (OR (AND (NOR ARG0 ARG1) (NOR (AND ARG1
ARG1) ARG1)) (NOR (NAND ARG0 ARG0) (NAND ARG1
ARG1))) (NAND (NOR (NOR ARG1 ARG1) (AND (OR
(NAND ARG0 ARG0) (NOR ARG1 ARG0)) ARG0)) (AND
(OR ARG0 ARG0) (NOR (OR (AND (NOR ARG0 ARG1)
(NAND ARG1 ARG1)) (NOR (NAND ARG0 ARG0) (NAND
ARG1 ARG1))) ARG1))))
(OR (AND ARG2 (NAND ARG0 ARG2)) (NOR ARG1 ARG1))
(ADFO (ADFO D0 D2) (NAND (OR D3 D1) (NAND D1
D3)))).
```


Reading

- Poli, R., Langdon, W., McPhee, N.F.: *A Field Guide to Genetic Programming*, 2008, <http://www.gp-field-guide.org.uk/>
- Koza, J.: *Genetic Programming: On the Programming of Computers by Means of Natural Selection*, MIT Press, 1992.

