One dimensional searching

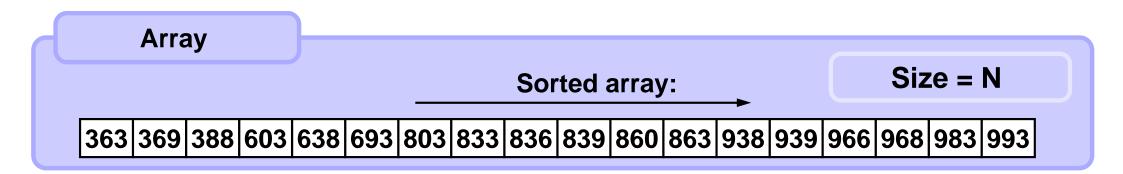
Searching in an array

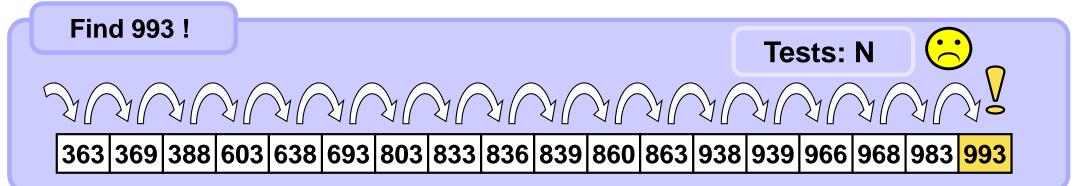
naive search, binary search, interpolation search

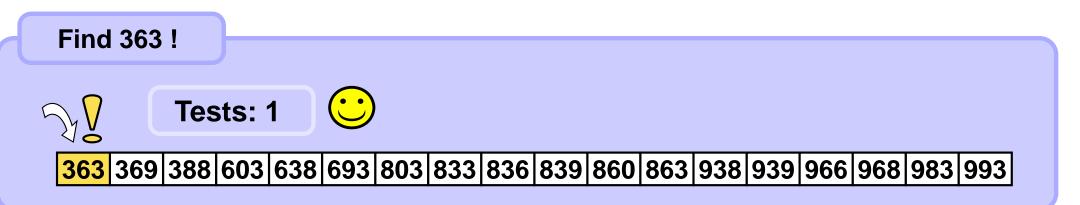
Binary search tree (BST)

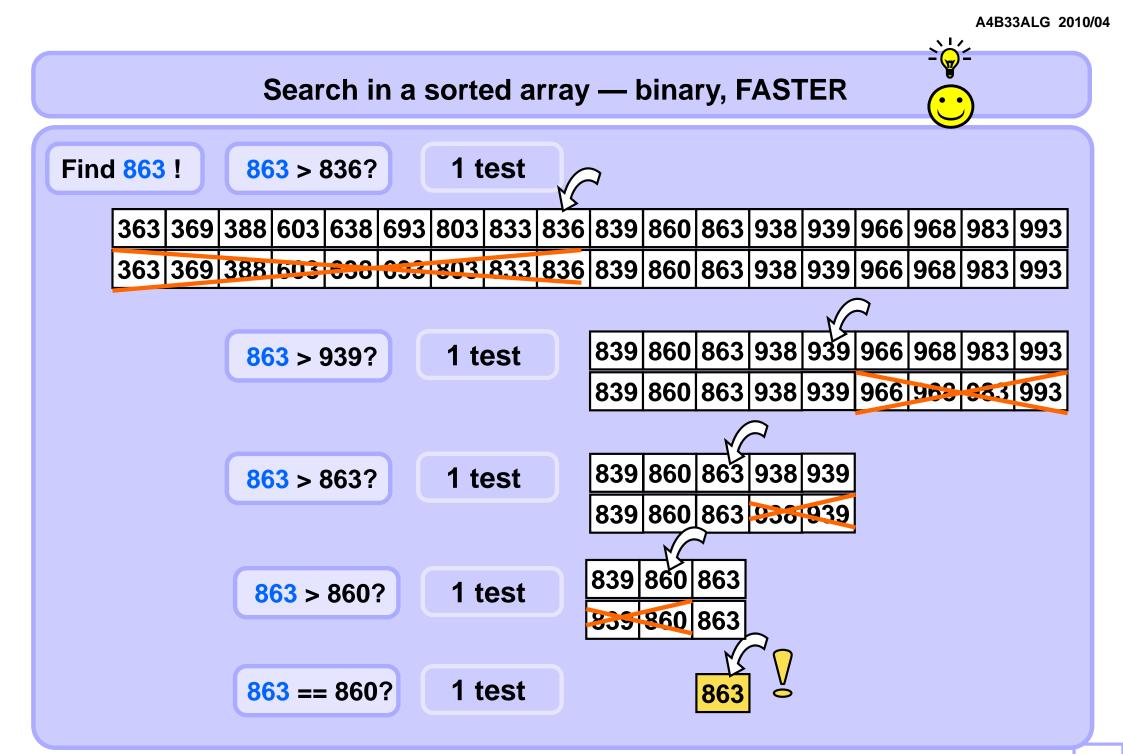
operations Find, Insert, Delete

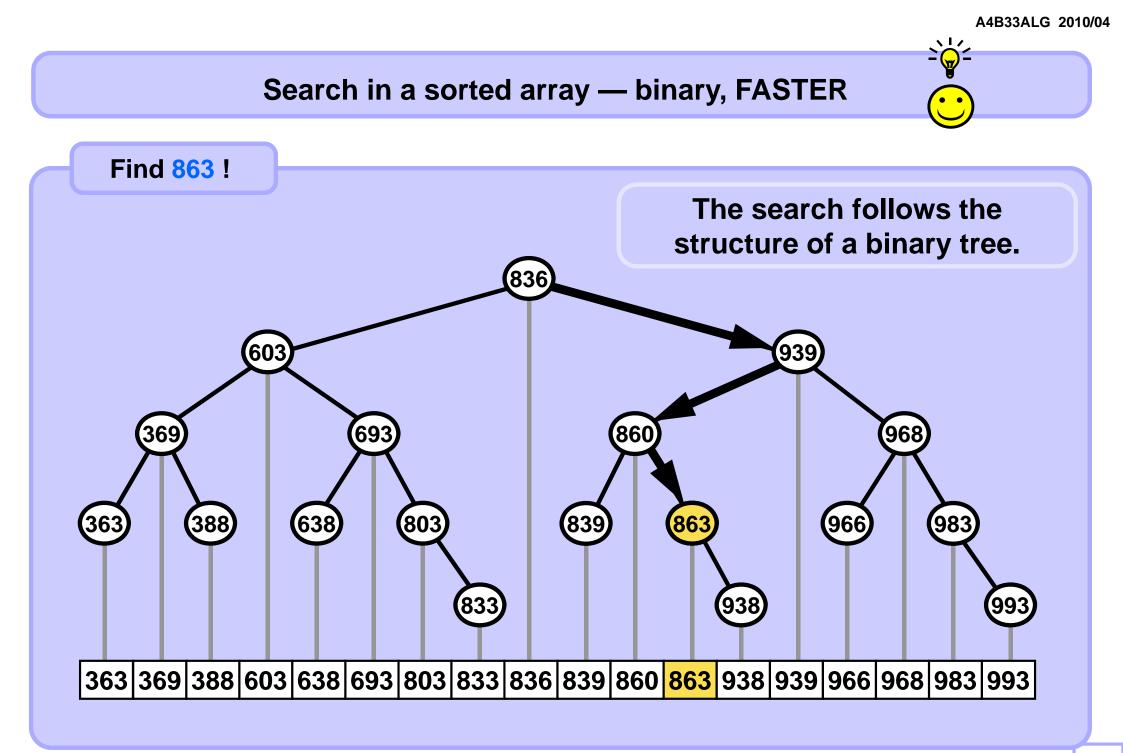
Naive search in a sorted array — linear, SLOW.



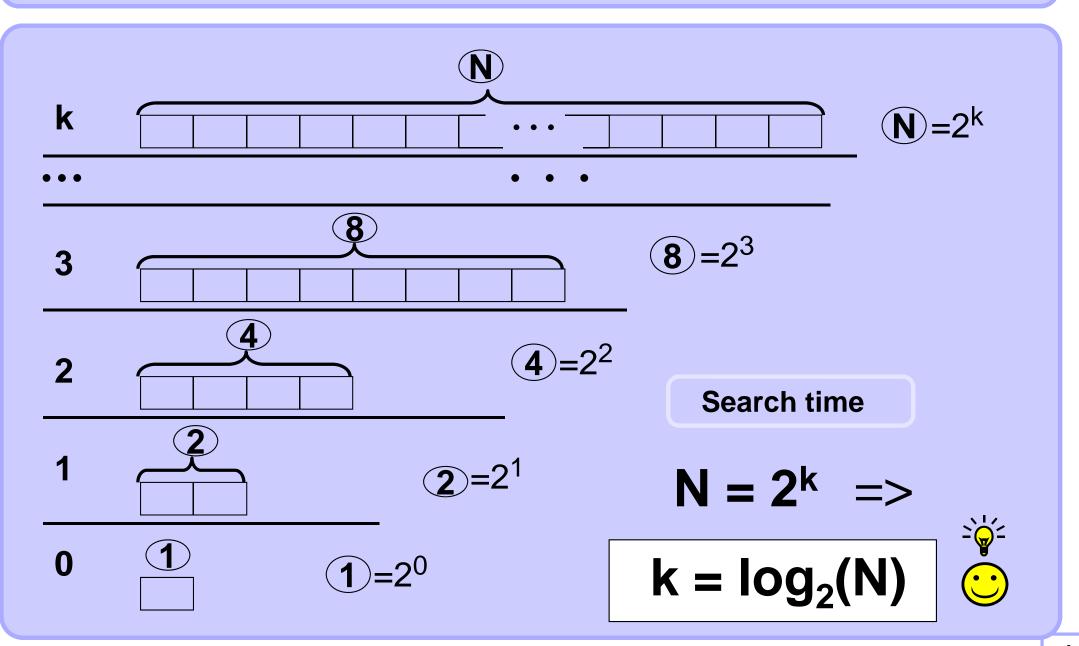


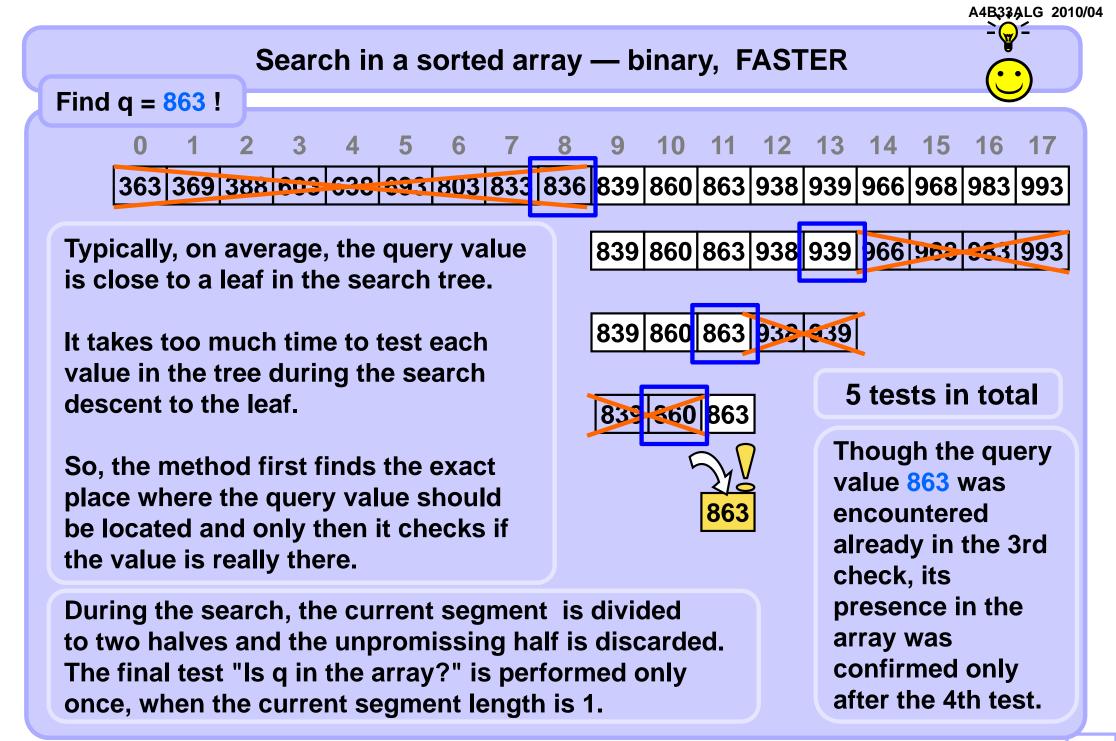






Search in a sorted array — binary, FASTER

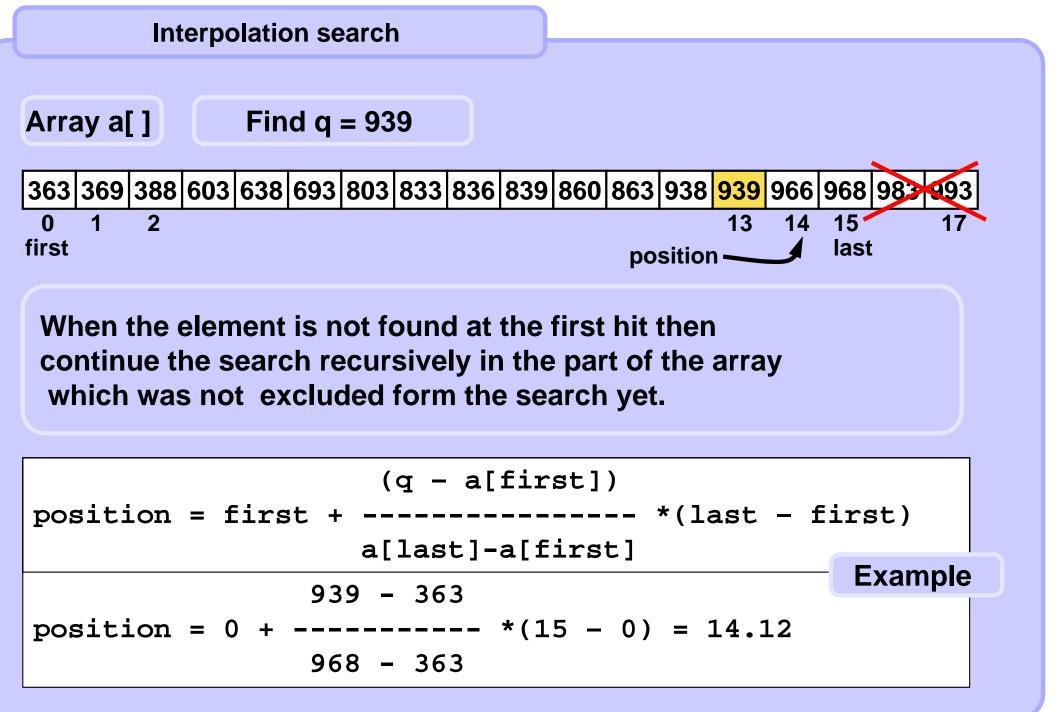


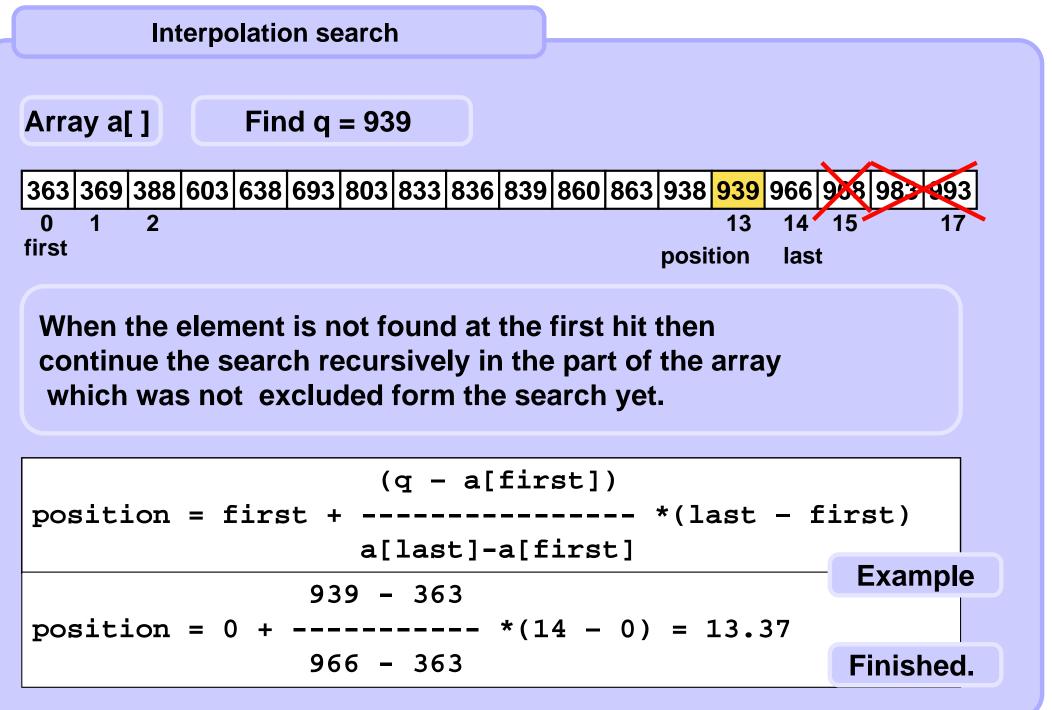


Binary search -- fast variant

Bug? : When low + high > INT_MAX in some languages overflow appears https://research.googleblog.com/2006/06/extra-extra-read-all-about-it-nearly.html

Int	erpol	atior	n se	arch	١										
Array a[]		Find	d q =	= 93	9										
363 369 388	603 6	638 6	693	803	833	836	839	860	863	938	939	966	968	983	993
0 1 2 first											13	р	15 ositic	on	17 last
When the v				-									t hol	In	
When the v distrubuted The position	d ove	er th	e ra	ange mer	e the nt sh	e int noul	erpo d ro	olatio ugh	on s ly co	earc	ch m	night		-	ue.
distrubute	d ove on of	er th the	e ra ele	ange mer (e the nt sh q -	e int noul a[erpo d ro fir	olatio ugh st]	on s ly co)	earc orre	ch m spoi	nd to	o its	val	ue.



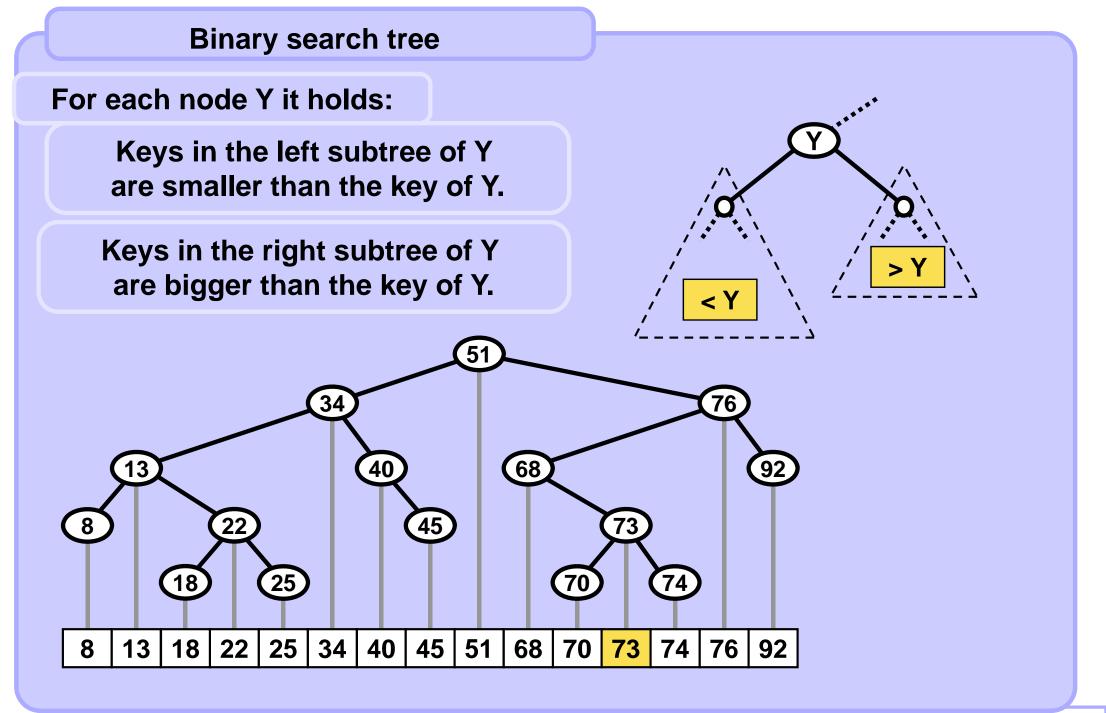


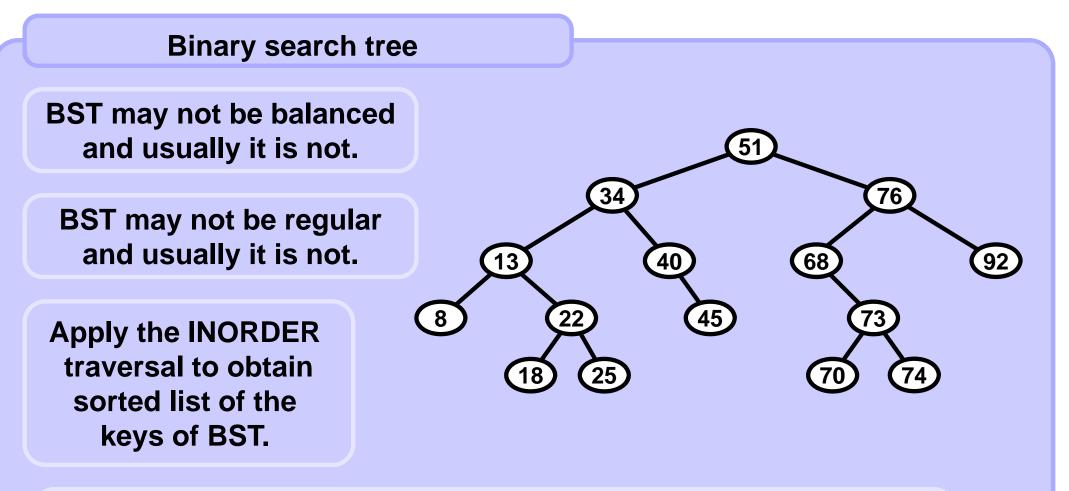
Interpolation search

```
def interpol( arr, q): # q is the query
 first = 0; last = len(arr)-1
while True:
     if first == last :
        if arr[first] == q: return pos
        else:
                         return -1
    pos = first + round( (q-arr[first])/
                    (arr[last]-arr[first]) *(last-first) )
     if arr[pos] == q: return pos
     if arr[pos] < q: first = pos+1 # check left side</pre>
                 last = pos-1 # check right side
    else:
```

Search in a sorted array — speed comparison

Array	Linear search	Interpolation search	Binary search
size N	average case	average case	all cases
10	5.5	1.60	4
30	15.5	2.12	5
100	50.5	2.56	7
300	150.5	2.89	9
1 000	500.5	3.18	10
3 000	1 500.5	3.41	12
10 000	5 000.5	3.63	14
30 000	15 000.5	3.80	15
100 000	50 000.5	3.96	17
300 000	150 000.5	4.11	19
1 000 000	500 000.5	4.24	20
Asymptotic complexity	Obviously ⊕(n)	Random uniform distribution $log_2(log_2(N)) \in \Theta(log(log(N)))$	Due to the binary tree structure ☉(log(n))



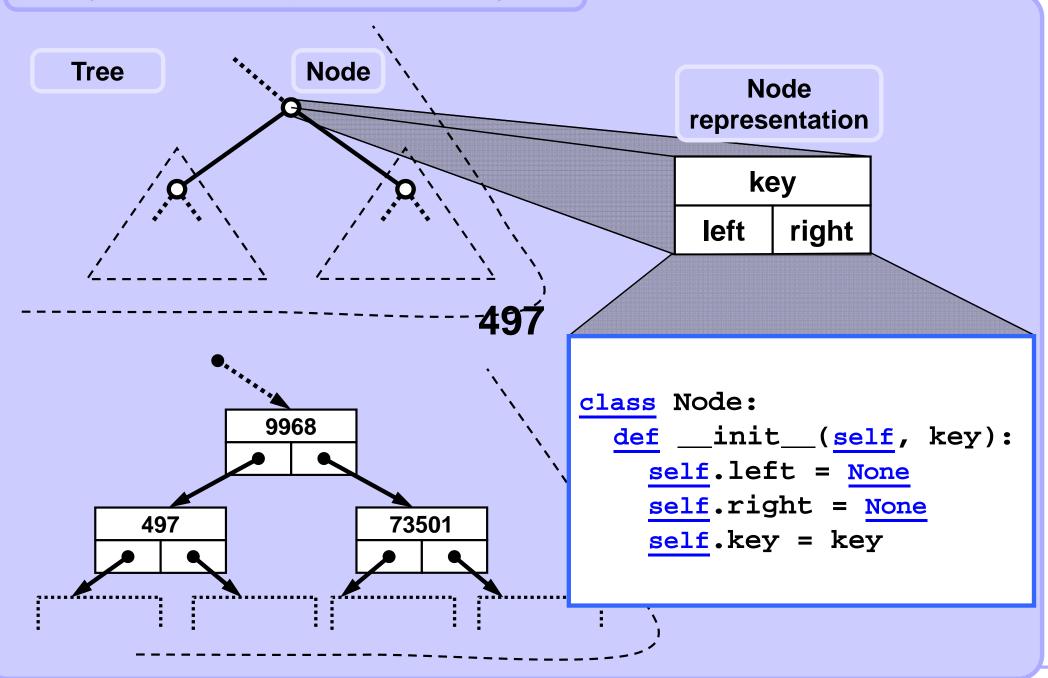


BST is flexible due to operations:

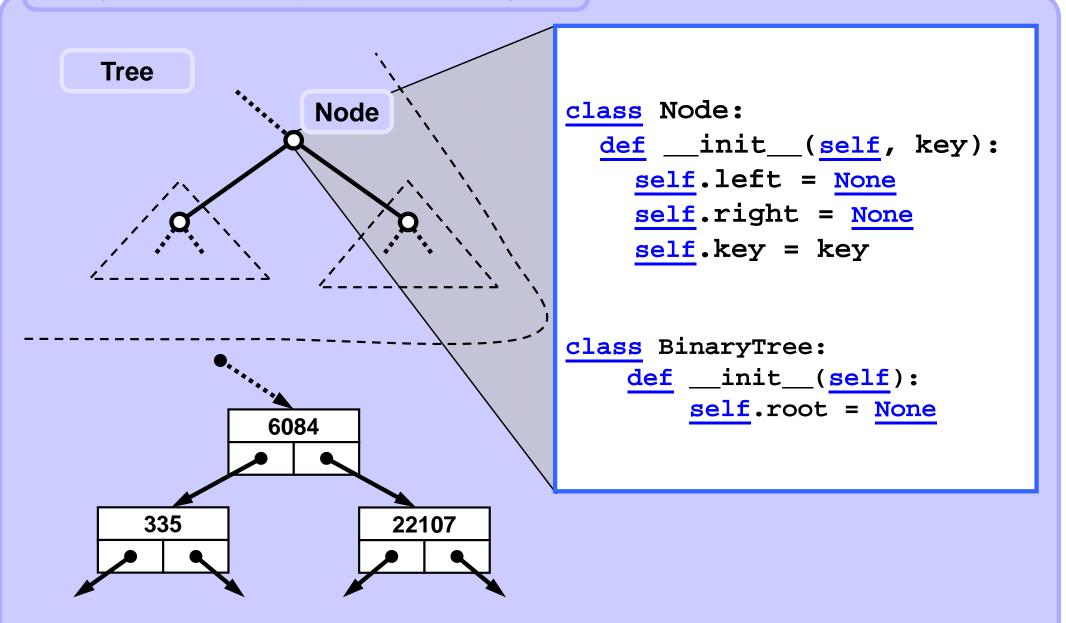
Find – return the pointer to the node with the given key (or null). Insert – insert a node with the given key. Delete – (find and) remove the node with the given key.

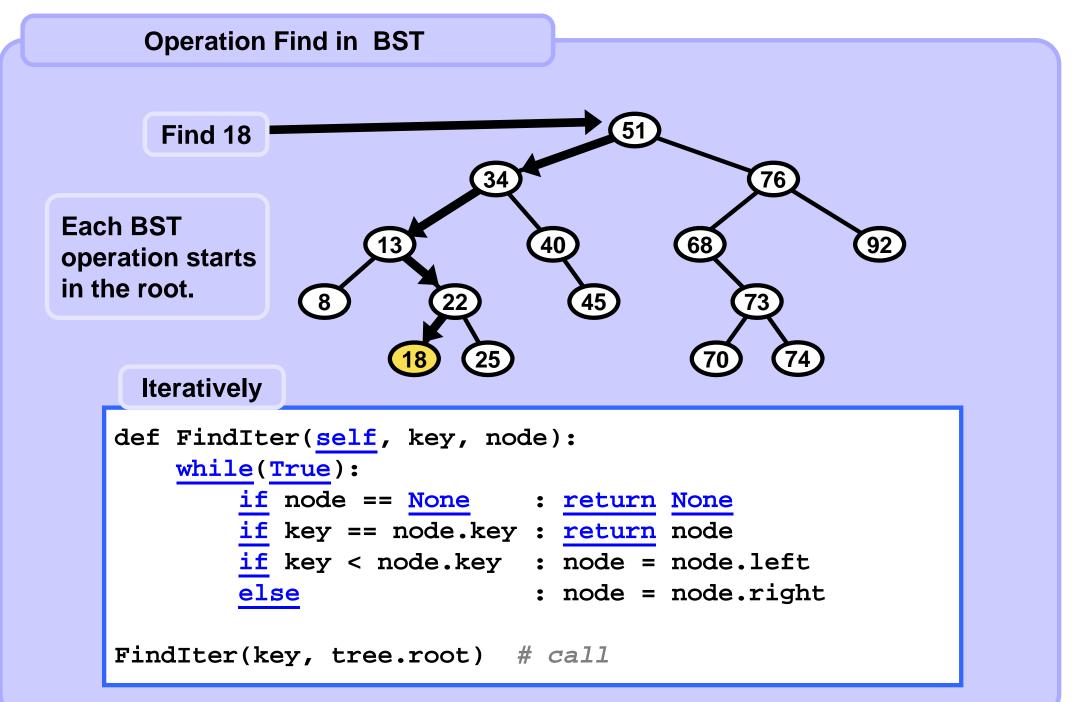
A4B33ALG 2010/04



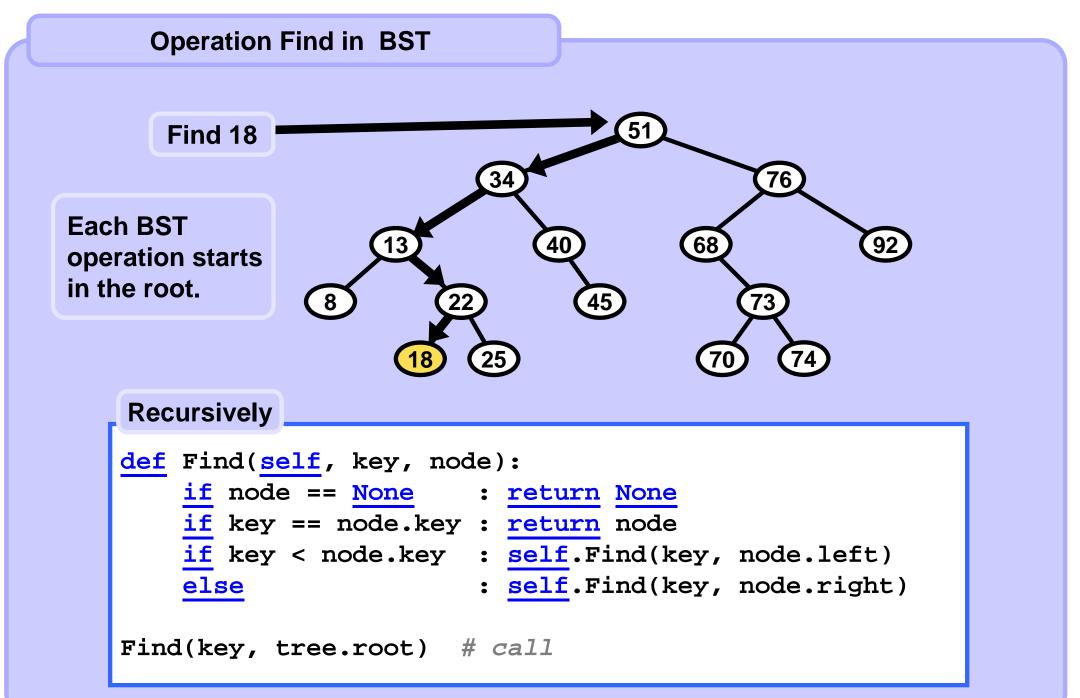


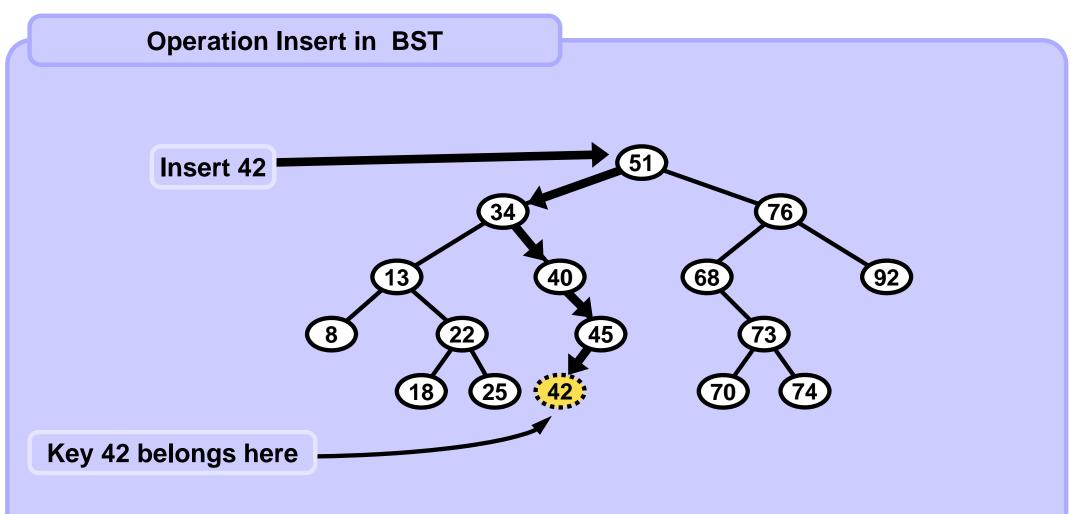
Binary search tree implementation -- Python





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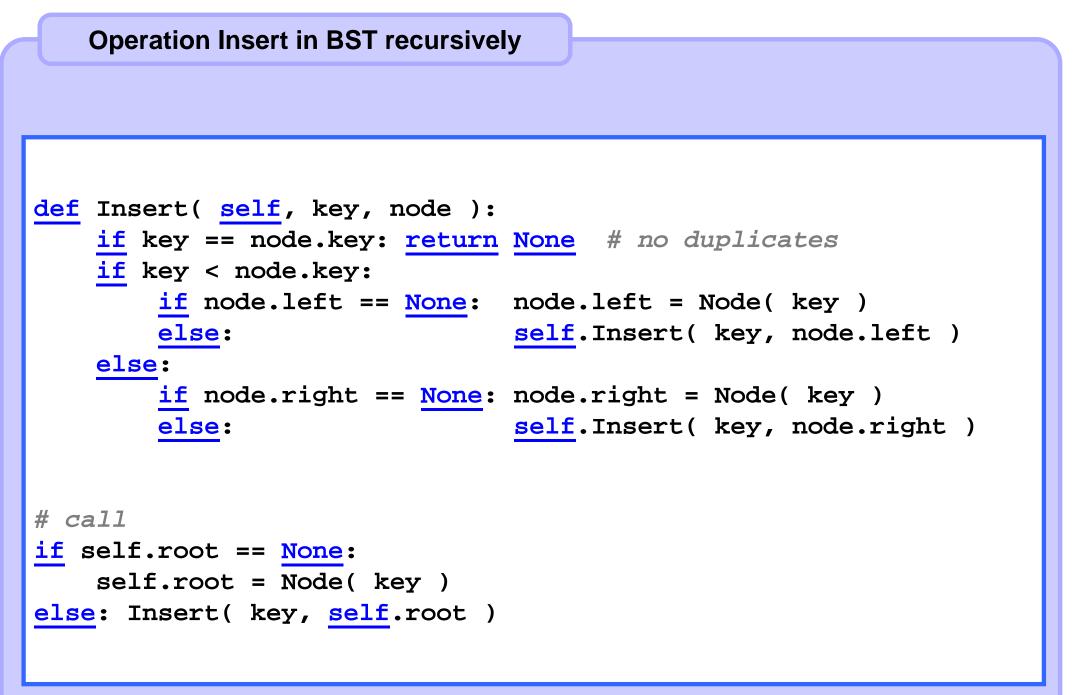


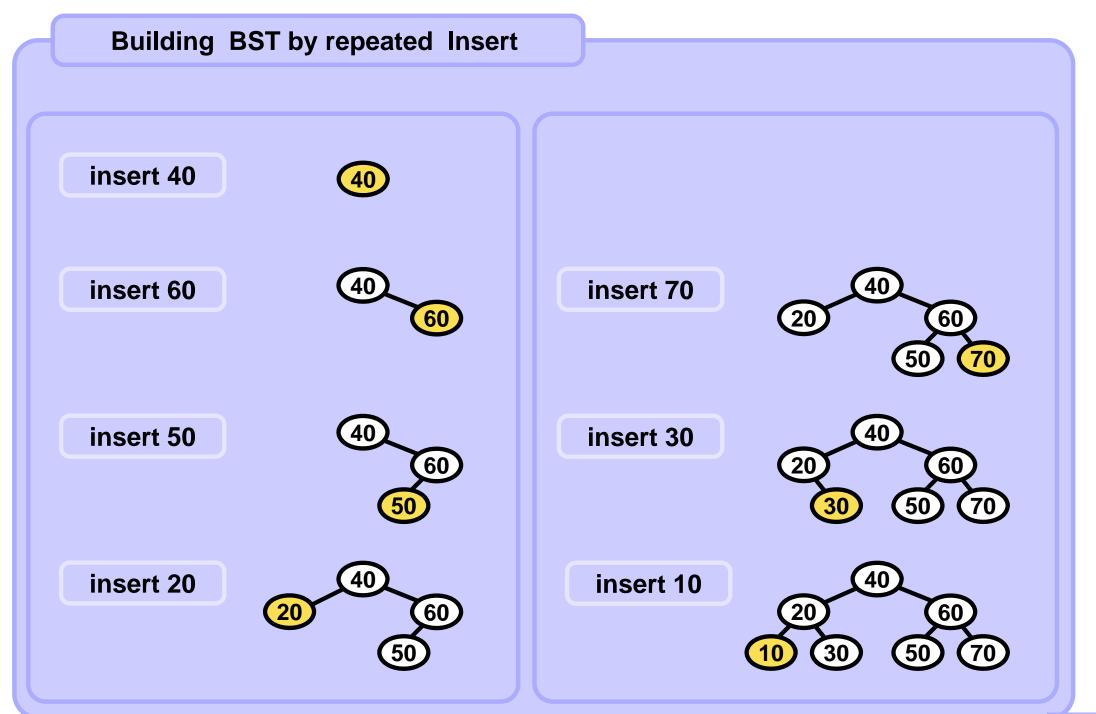


Insert

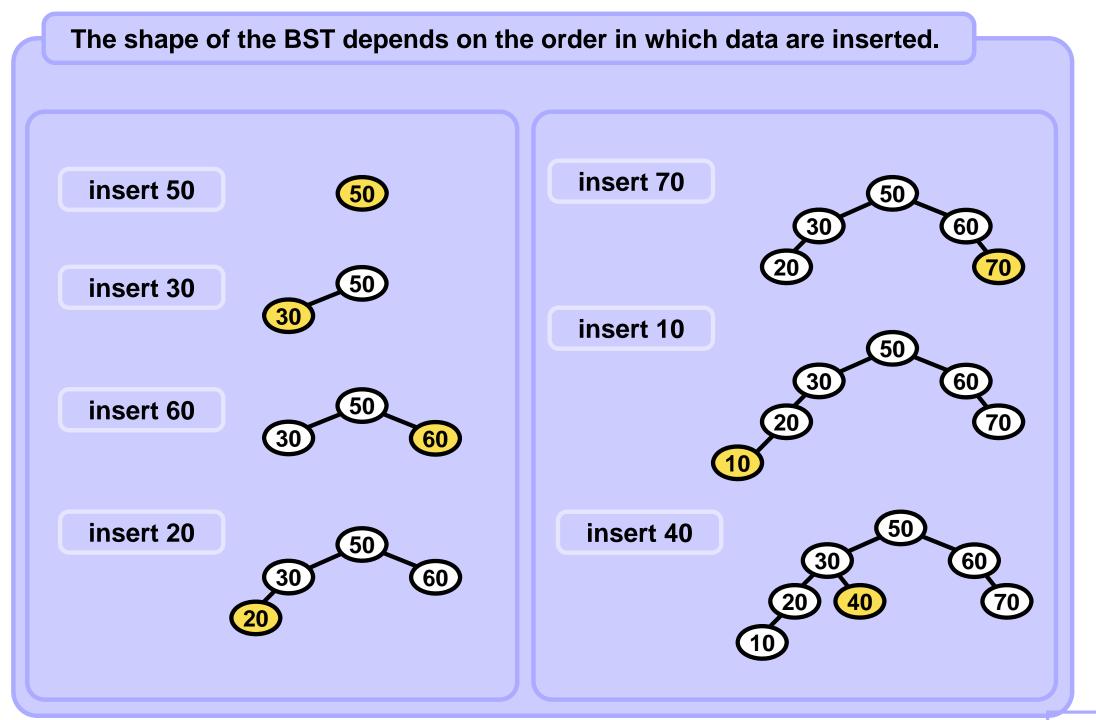
- 1. Find the place (like in Find) for the leaf where the key belongs.
- 2. Create this leaf and connect it to the tree.

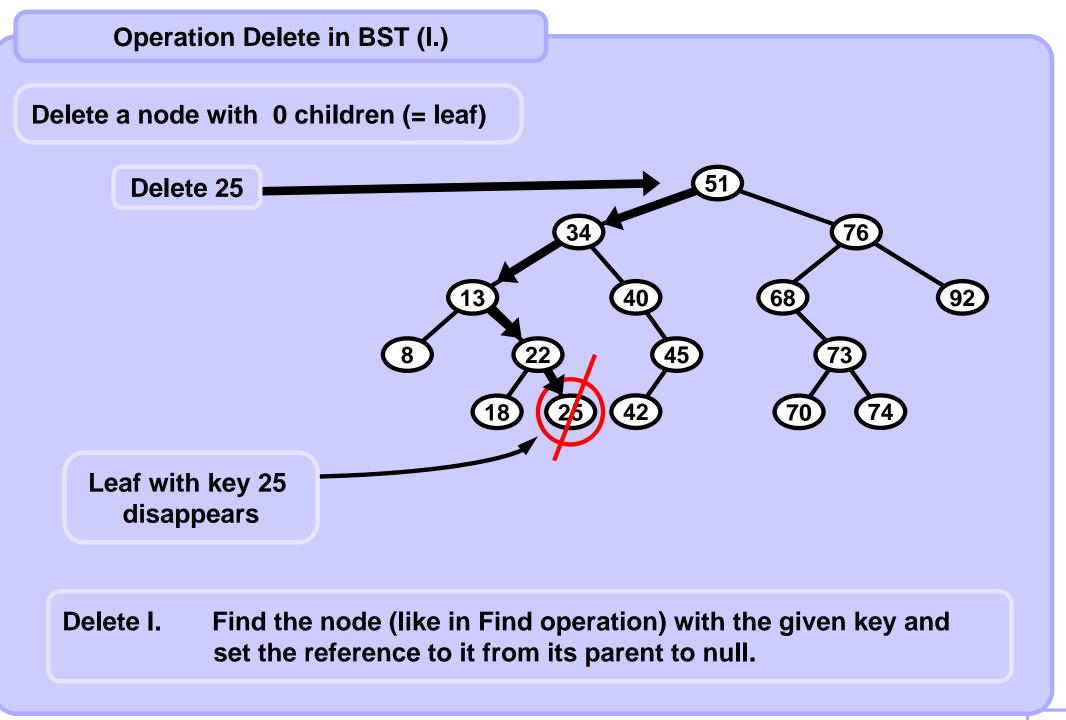
```
def InsertIter( self, key ):
                                     # empty tree
 if self.root == None:
     self.root = Node( key );
     return self.root
 node = self.root
 while True:
     if key == node.key: return None # no duplicates!
     if key < node.key:</pre>
         if node.left == None:
             node.left = Node( key )
             return node.left
         else: node = node.left
     else:
         if node.right == None:
             node.right = Node( key )
             return node.right
         else: node = node.right
```

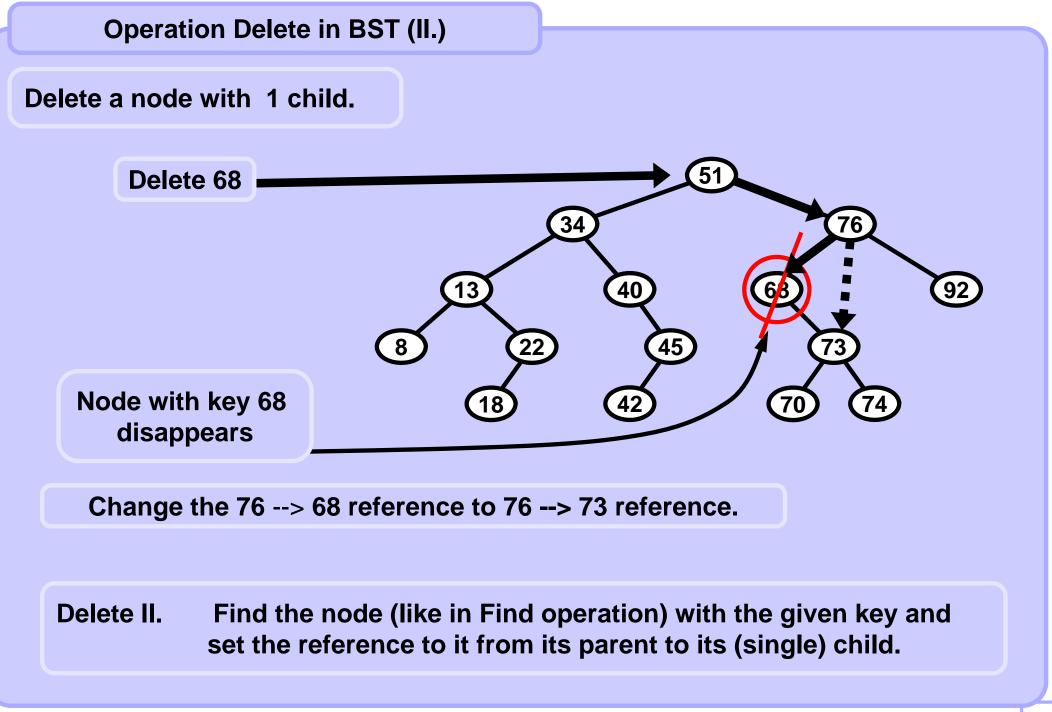




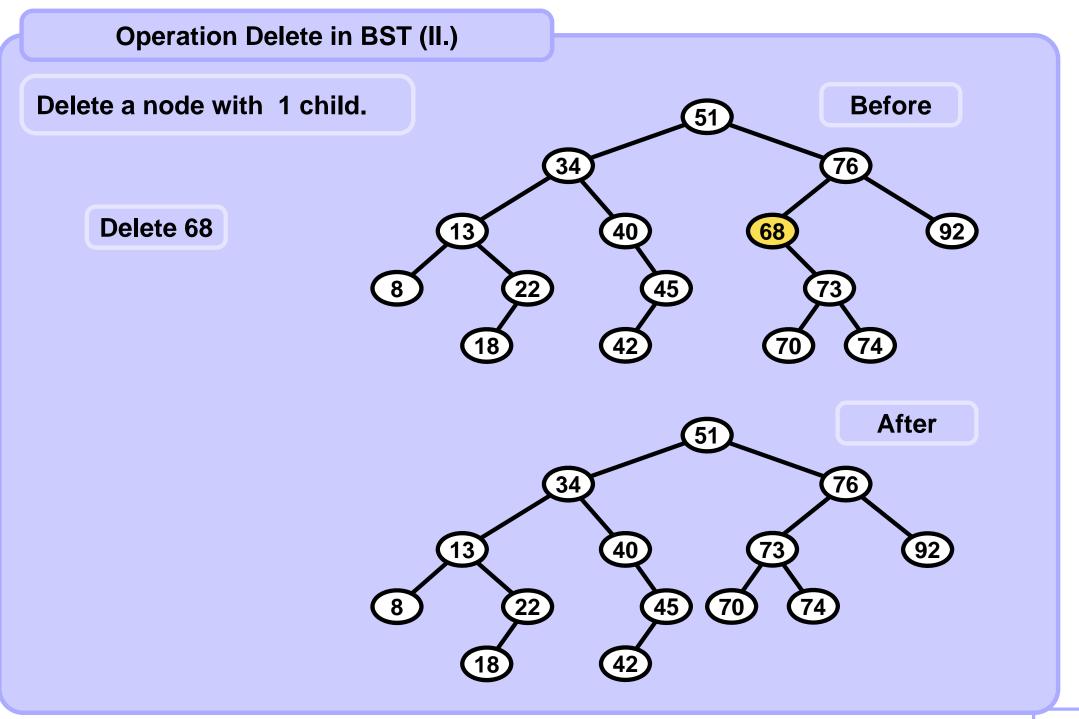
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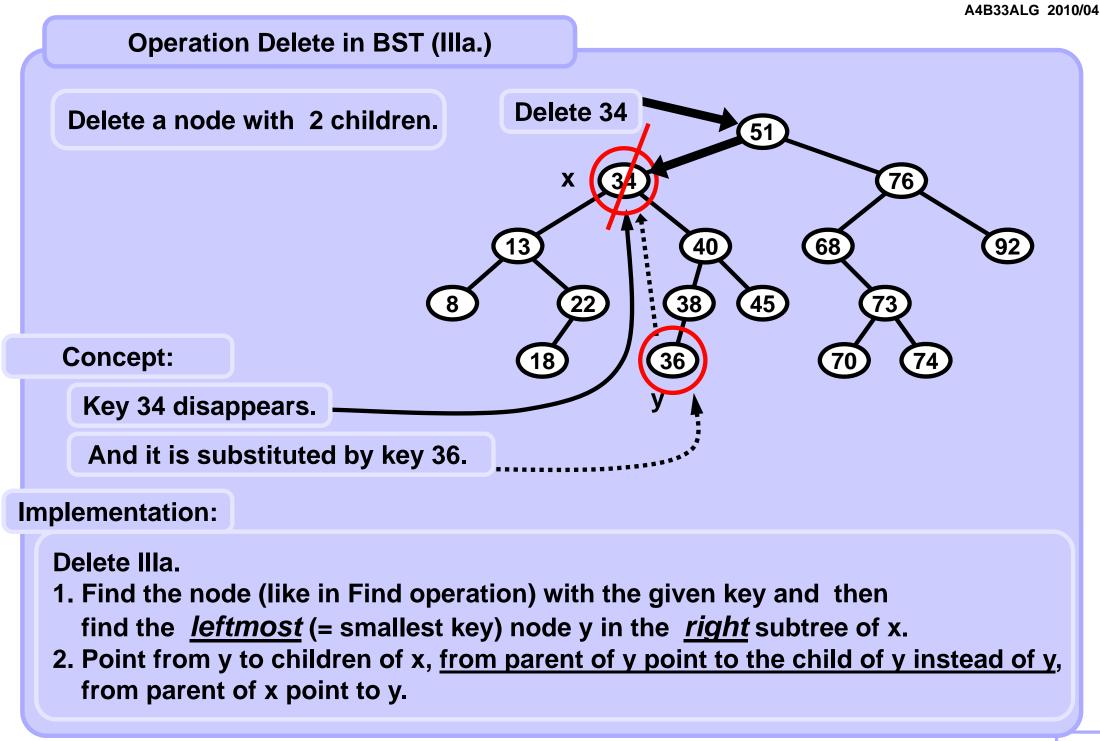


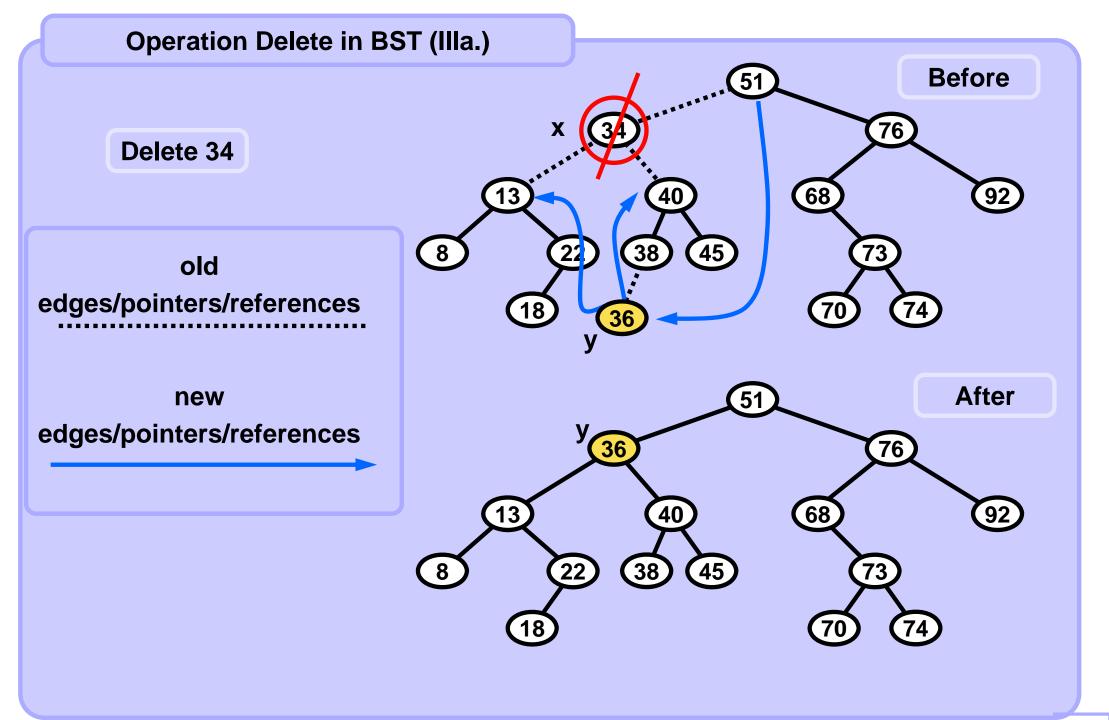


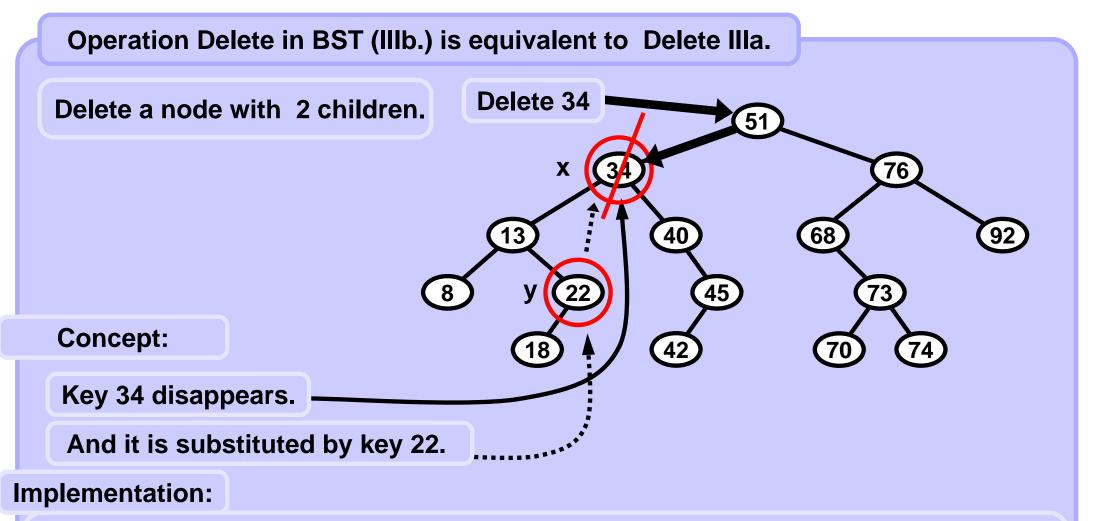


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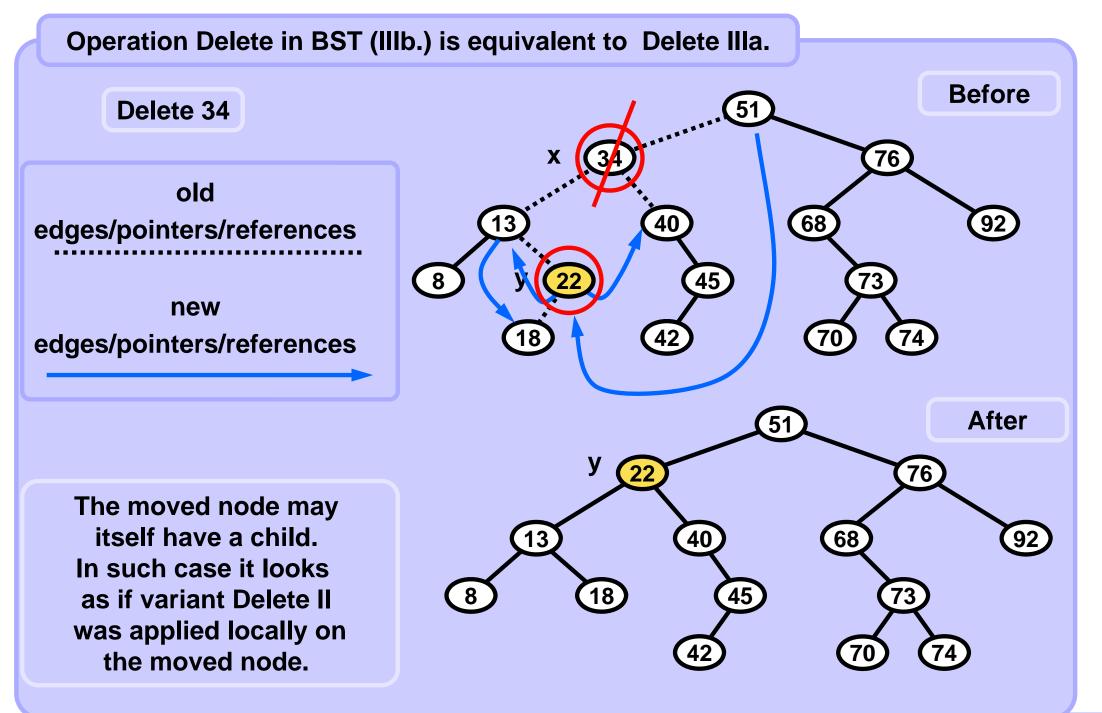


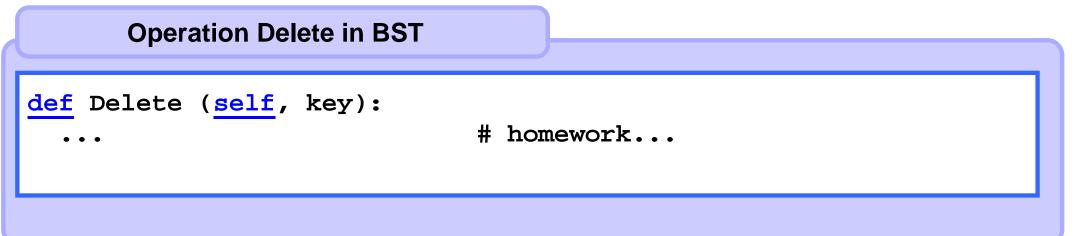




Delete IIIb.

- 1. Find the node (like in Find operation) with the given key and then find the *rightmost* (= smallest key) node y in the *left* subtree of x.
- 2. Point from y to children of x, from parent of y point to the child of y instead of y, from parent of x point to y.





Asymptotic	c complexities of operations Find, In	sert, Delete in BST				
	BST with n nodes					
Operation	Balanced not guaranteed, must be induced by additional conditions	Not balanced (expected general case)				
Find	O (log(n))	O (n)				
Insert	O (log(n))	O (n)				
Delete	O (log(n))	O (n)				