

# Abstractions

PAH (Planning and Games)

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# Abstractions

- General approach to computing heuristic estimates
- *Abstract* multiple states into one to make the problem smaller
  - But preserve the transition behaviour
- Easy to be admissible

# Quiz

- To give **admissible** estimates, an abstraction  $T'$  of transition system  $T$  does not have to satisfy:
  1. if  $s$  is the init state in  $T$ , then  $a(s)$  is the init state in  $T'$
  2.  $a(s)$  is a goal state in  $T'$  if and only if  $s$  is a goal state in  $T$
  3. if  $T$  has a transition from  $s$  to  $t$ , then  $T'$  has a transition from  $a(s)$  to  $a(t)$

Answer:

2. If  $s$  is a goal state in  $T$ , **then**  $a(s)$  is a goal state in  $T'$ .

# Quiz

- Which combination of several abstractions is always **admissible**?:
  1. sum
  2. multiplication
  3. maximum

Answer:

**3.** maximum

# Quiz

- Let  $\Pi$  be an FDR planning task, and let  $A$  be an abstraction of  $T(\Pi)$  with abstraction mapping  $\alpha$ . Then  $h^{A,\alpha}$  is:
  1. safe, goal-aware, admissible and consistent
  2. safe, goal-aware, not admissible and not consistent
  3. only admissible

Answer:

1. safe, goal-aware, admissible and consistent

# Quiz

- Let  $\alpha_1 \dots \alpha_k$  be abstraction mappings on  $T$ .
- We say that  $\alpha_1 \dots \alpha_k$  are **orthogonal** if for all transitions  $\langle s, l, t \rangle$  of  $T$  :
  1.  $\alpha_i(s) \neq \alpha_j(t)$  for all  $i \neq j$
  2.  $\alpha_i(s) \neq \alpha_i(t)$  for at least one  $i \in [k]$
  3.  $\alpha_i(s) \neq \alpha_i(t)$  for at most one  $i \in [k]$

Answer:

3.  $\alpha_i(s) \neq \alpha_i(t)$  for **at most** one  $i \in [k]$

# Quiz

- Let  $\alpha_1 \dots \alpha_k$  be **orthogonal** abstraction mappings on T.
- Then  $\sum_{i \in [k]} h^{A, \alpha_i}$  is:
  1. safe, goal-aware, admissible and consistent
  2. safe, goal-aware, not admissible and not consistent
  3. only admissible

Answer:

1. safe, goal-aware, admissible and consistent

# Quiz

- Let  $h^{A,\alpha}$  and  $h^{A,\beta}$  be abstraction heuristics for the same planning task  $\Pi$  such that  $\langle A,\alpha \rangle$  is a **refinement** of  $\langle B,\beta \rangle$ .
- Then:
  1.  $h^{A,\alpha} == h^{A,\beta}$  for all states  $s$  of  $\Pi$ .
  2.  $h^{A,\alpha} \leq h^{A,\beta}$  for all states  $s$  of  $\Pi$ .
  3.  $h^{A,\alpha} \geq h^{A,\beta}$  for all states  $s$  of  $\Pi$ .

Answer:

3.  $h^{A,\alpha} \geq h^{A,\beta}$  for all states  $s$  of  $\Pi$ .