

Problem solving by search II

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Outline

- ▶ Graph search
- ▶ Heuristics (how to search faster)
- ▶ Greedy
- ▶ A*. A-star search.

Recap: Search

A tree search recap

```
function TREE_SEARCH(problem) return a solution or failure
  initialize the frontier the initial state of the problem
  loop
    if the frontier is empty then return failure
    else choose a node from frontier and remove from frontier
    end if
    if the node contains a goal state then return the solution
    end if
    Expand the node and add the resulting nodes to frontier
  end loop
end function
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A Maze, what could possibly go wrong?

Analyze the demo run. What happened? Why did it take that long?

	0	1	2	3	4	
0	0.00	0.00	0.00	0.00	0.00	0
1	0.00	0.00	0.00	0.00	0.00	1
2	0.00	0.00	0.00	0.00	0.00	2
3	0.00	0.00	0.00	0.00	0.00	3
4	0.00	0.00	0.00	0.00	0.00	4
	0	1	2	3	4	

Tree search the maze

```
function TREE_SEARCH(env) return a  
solution or failure  
  initialize the frontier  
  while frontier do  
    node = frontier.pop()  
    if goal in node then  
      break  
    end if  
    nodes = env.expand(node.state)  
    Add nodes to frontier  
  end while  
end function
```

	0	1	2	3	4	
0	0.00	0.00	0.00	0.00	0.00	0
1	0.00	0.00	0.00	0.00	0.00	1
2	0.00	0.00	0.00	0.00	0.00	2
3	0.00	0.00	0.00	0.00	0.00	3
4	0.00	0.00	0.00	0.00	0.00	4
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Make a frontier and expand columns on a paper and follow the algorithm by putting and removing (scratching out) nodes from the list.

A graph search

function GRAPH_SEARCH(env) **return** a solution or failure

 init **frontier** by the start state

initialize the explored set to be empty

while frontier **do**

 node = frontier.pop()

if goal in node **then** break

end if

 nodes = env.expand(node.state)

add node to explored

for all nodes **do**

if *node not in explored (or in frontier)* **then**

 add nodes to frontier

end if

end for

end while

end function

Think about what is node and what state. What is main difference? How are they connected? Where do they appear? What is node/state in the maze problem?

The main idea: Do not expand a **state** twice.



Do not forget: node is not the same as state!

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Do not forget: *node* is not the same as *state*!

The BFS graph search

```
function BFS_GRAPH_SEARCH(env) return a solution or failure
  node ← env.observe()
  frontier ← FIFOqueue(node)
  explored ← set()
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    node ← frontier.pop()
    explored.add(node.state)           ▷ adding state not node!
    child_nodes ← env.expand(node.state)
    for all child_nodes do
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Why adding/checking state and note node in expanded data structure?
Can I do the simple presence check for all kind of graph search algorithms?

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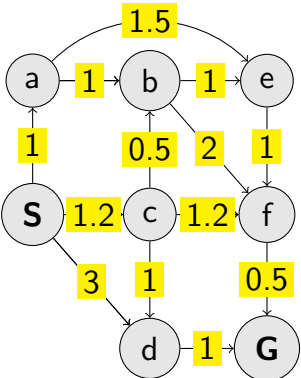
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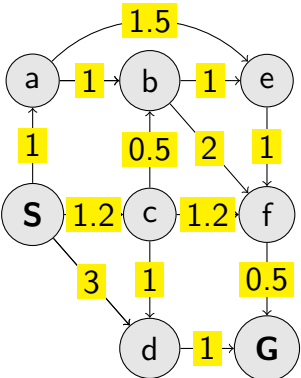
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What about actual costs graph search?



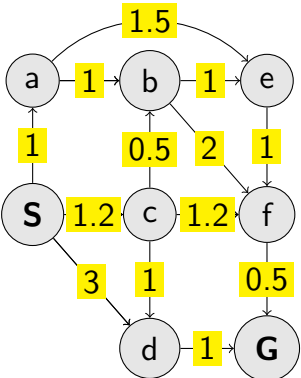
When following the algorithm (animation) use the paper list of frontier and expanded

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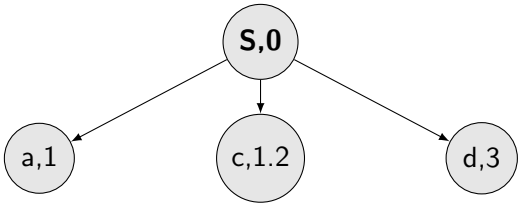
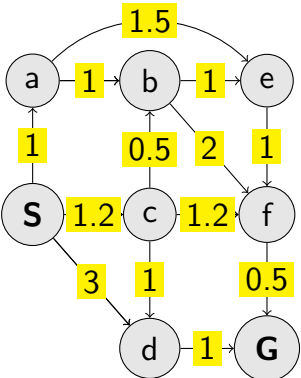
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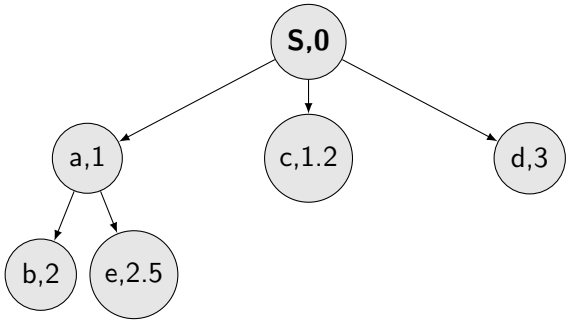
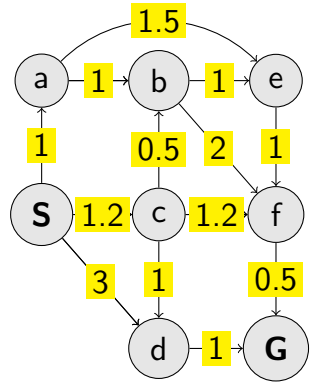
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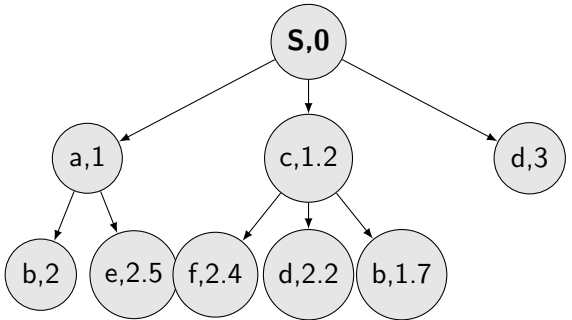
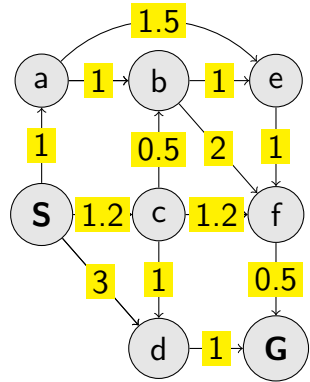
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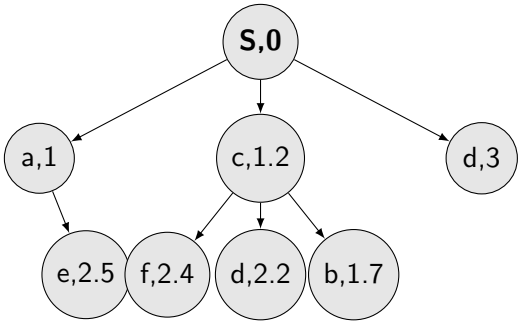
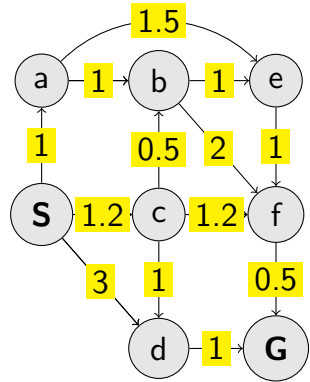
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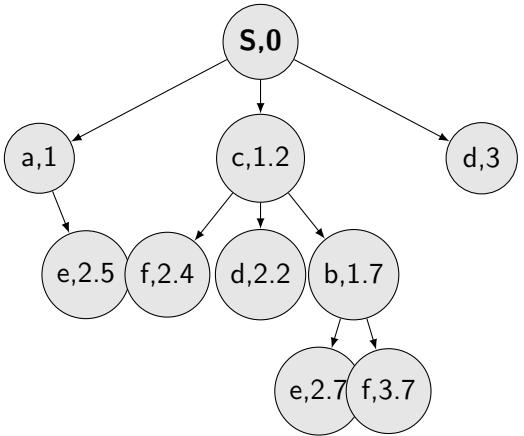
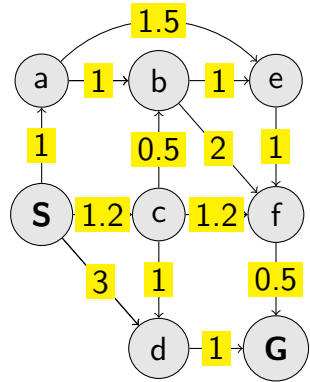
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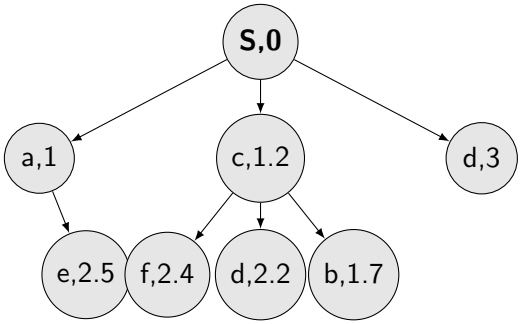
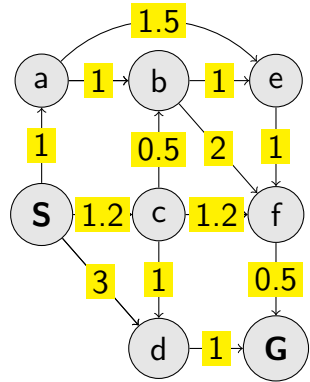
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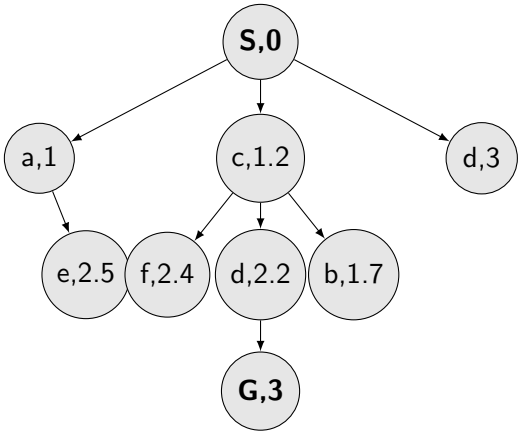
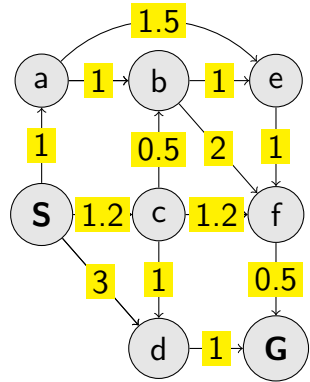
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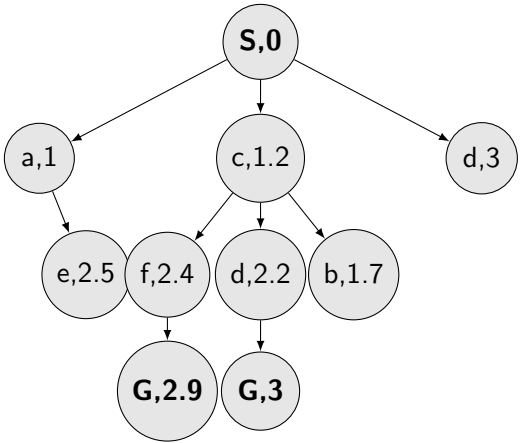
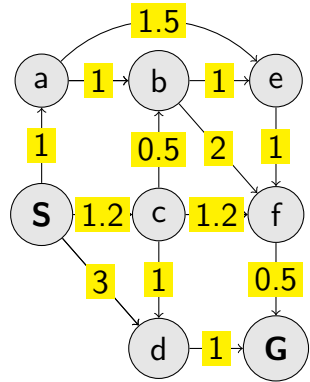
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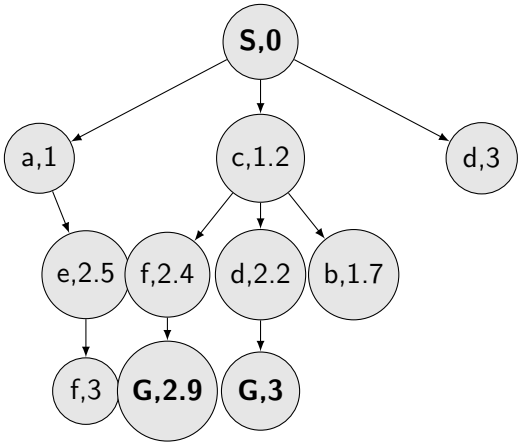
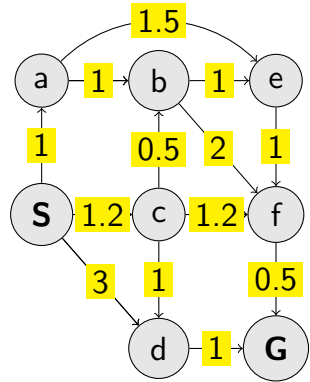
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function UCS_GRAPH_SEARCH(env) return a solution or failure
  node ← env.observe()
  frontier ← priority_queue(node)           ▷ path_cost for ordering
  explored ← set()
  while frontier not empty do
    node ← frontier.pop()
    if node contains Goal then return node           ▷ check here!
    end if
    explored.add(node.state)
    child_nodes ← env.expand(node.state)
    for all child_nodes do
      if child_node.state not in explored or in frontier then
        frontier.insert(child_node)
      else if child_node.state in frontier with higher cost then
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Does the algorithm always find the best (cheapest) path? Are there any requirements for the path optimality function?

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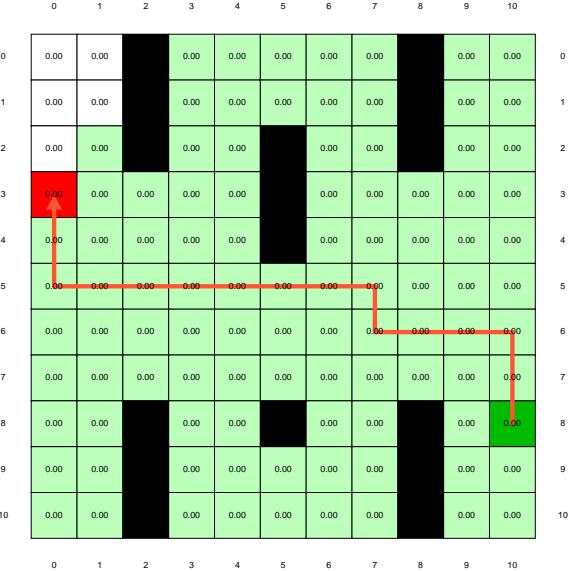
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    child_nodes ← env.expand(node.state)
    for all child_nodes do
      if child_node.state not in explored or in frontier then
        frontier.insert(child_node)
      else if child_node.state in frontier with higher cost then
        replace that with the child_node
      end if
    end for
  end while
```

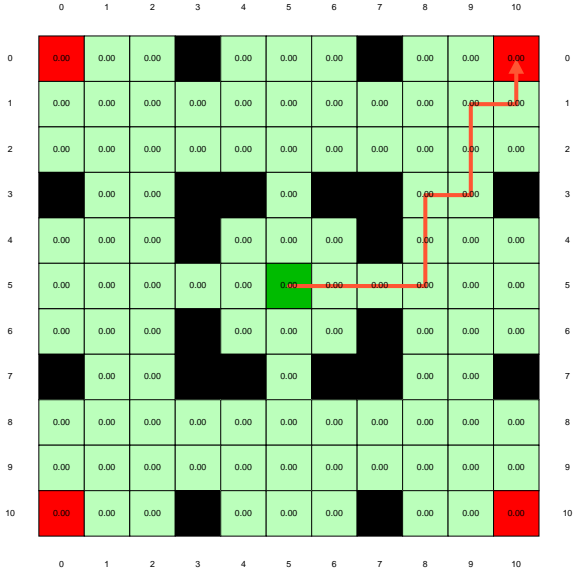
Does the algorithm always find the best (cheapest) path? Are there any requirements for the path optimality function?

Few examples of search strategies so far



Run the demos.

What is wrong with UCS and other strategies?



Run the demo.

Node selection, take argmin $f(n)$

- ▶ DFS: $f(n) = -n.depth$
- ▶ BFS: $f(n) = n.depth$
- ▶ UCS: $f(n) = n.path_cost$

The good: frontier as a priority queue The bad: All the $f(n)$ correspond to the cost from n to the start - only backward cost.

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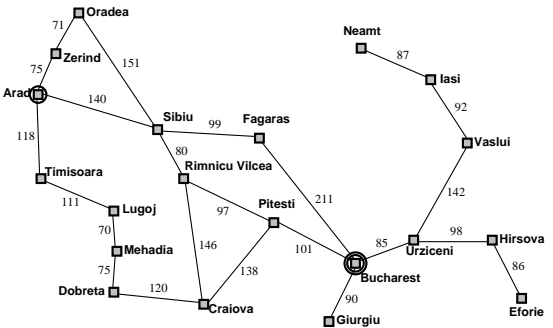
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Heuristics

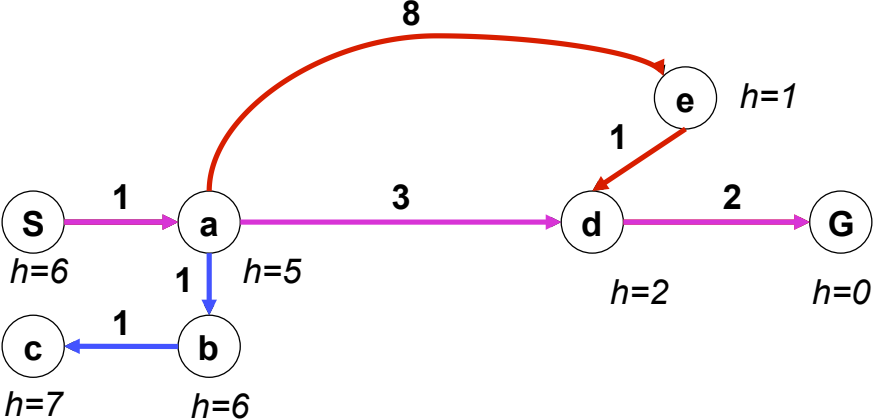
- ▶ A function that estimates how close a state to the goal.
- ▶ Designed for a particular problem.
- ▶ Examples:
- ▶ We will use $h(n)$ - heuristic value of node n

Example of hueristics



Arad	366	Mehadia	241
Bucharest	0	Neamt	234
Craiova	160	Oradea	380
Drobeta	242	Pitesti	100
Eforie	161	Rimnicu Vilcea	193
Fagaras	176	Sibiu	253
Giurgiu	77	Timisoara	329
Hirsova	151	Urziceni	80
Iasi	226	Vaslui	199
Lugoj	244	Zerind	374

Greedy, take the node argmin $h(n)$

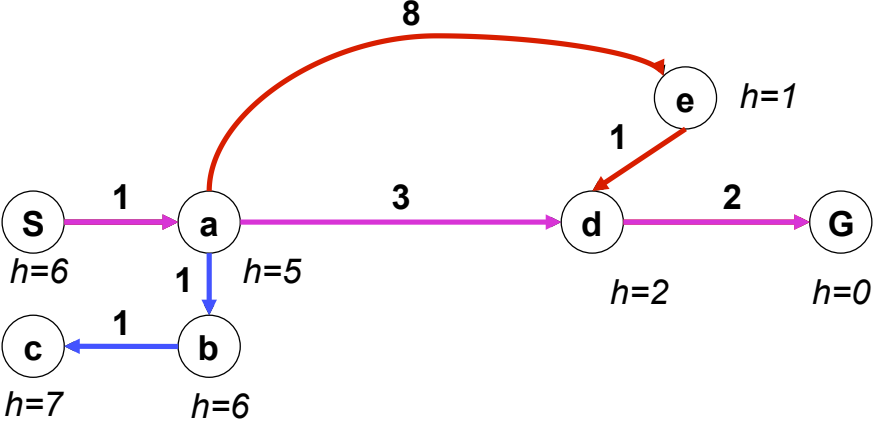


1

What is wrong (and nice) with the Greedy?

¹Graph example: Ted Grenager

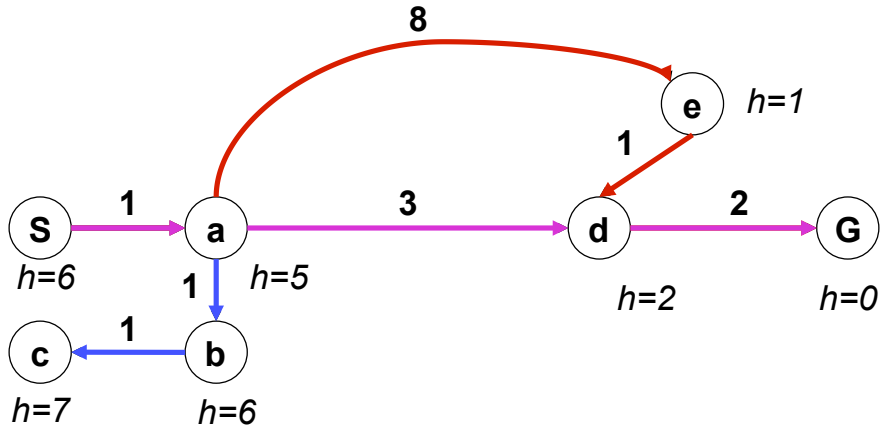
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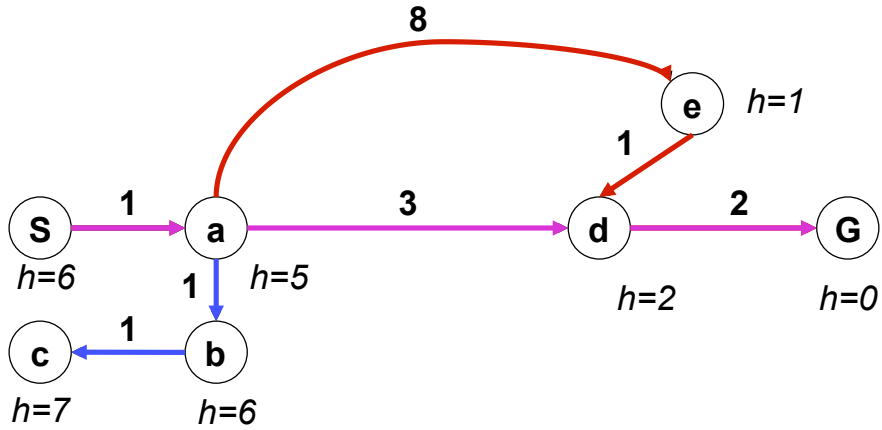
A* combines UCS and Greedy



UCS orders by backward (path) cost $g(n)$
Greedy uses heuristics (goal proximity) $h(n)$

A* orders nodes by: $f(n) = g(n) + h(n)$

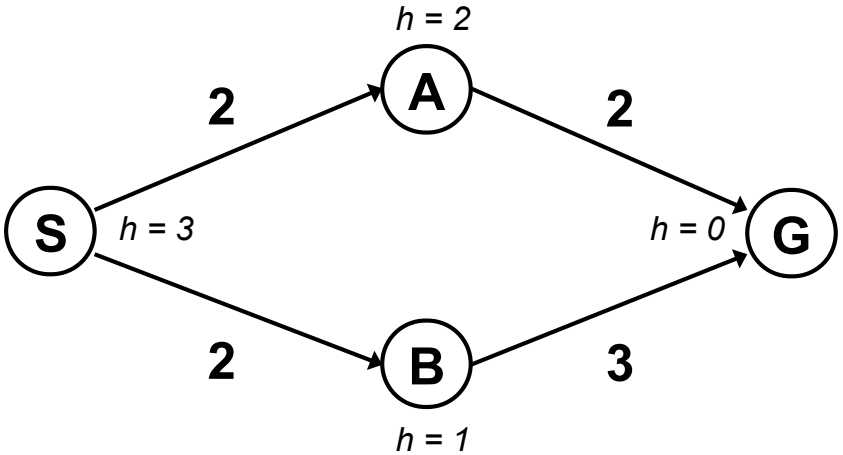
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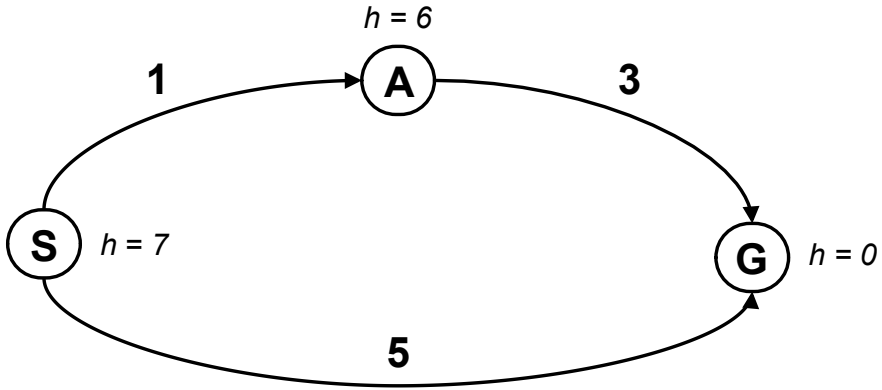
When to stop A*



2

²Graph example: Dan Klein and Pieter Abbeel

Is A* optimal?

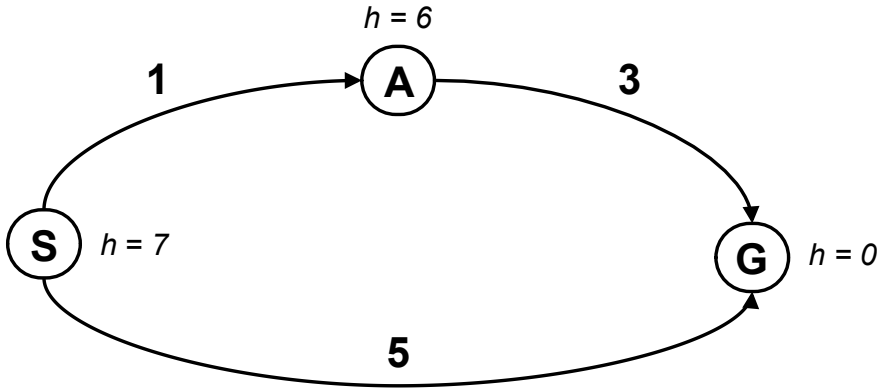


3

What is the problem?

³Graph example: Dan Klein and Pieter Abbeel

Is A* optimal?



3

What is the problem?

³Graph example: Dan Klein and Pieter Abbeel

Admissible heuristics

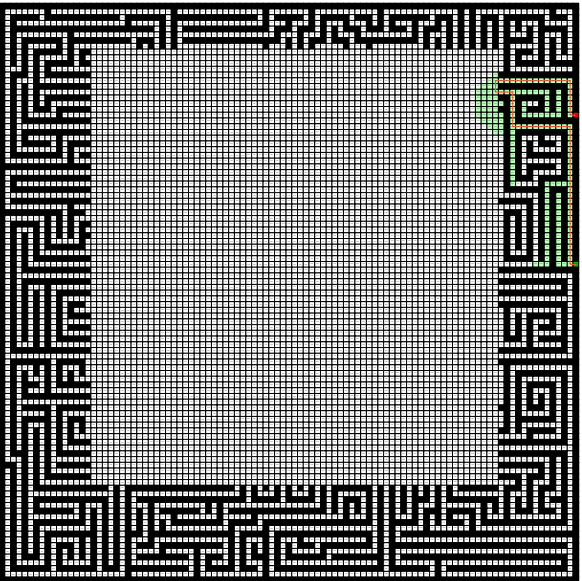
A heuristic function h is admissible if:

$$0 \leq h(n) \leq h^*(n)$$

where $h^*(n)$ is the true cost of going from n to the nearest goal.

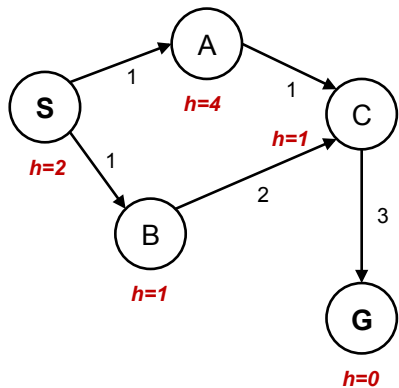
Optimality of A* tree search

Properties - does heuristic matter?



A* graph search

```
function GRAPH_SEARCH(env)
  frontier.insert(startnode)
  explored = set()
  while frontier do
    node = frontier.pop()
    if goal in node then break
    end if
    nodes = env.expand(node.state)
    explored.add(node)
    for all nodes do
      if node not in explored then
        frontier.insert(node)
      end if
    end for
  end while
end function
```

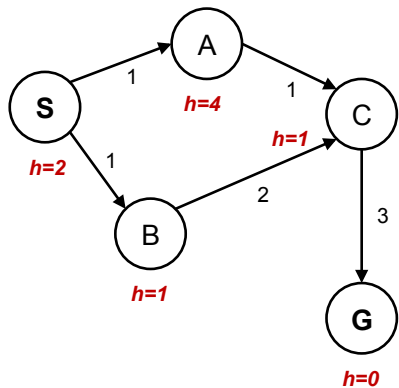


Graph example: Dan Klein and Pieter Abbeel

What went wrong?

A* graph search

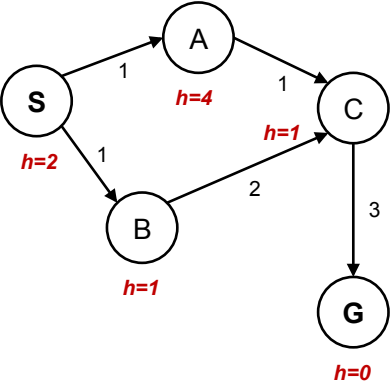
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Graph example: Dan Klein and Pieter Abbeel

What went wrong?

Consistent heuristics

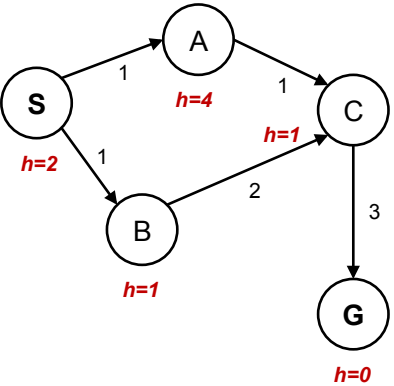


Admissible h :
 $h(A) \leq \text{true cost } A \rightarrow G$

Consistent h :
 $h(A) - h(C) \leq \text{true cost } A \rightarrow C$

f along a path never decreases!

Consistent heuristics

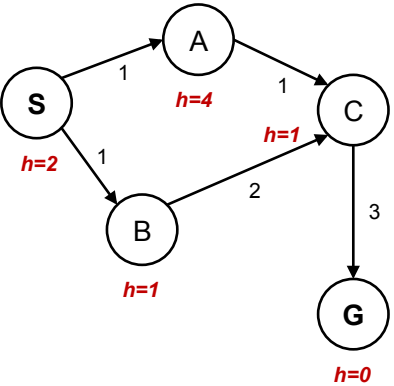


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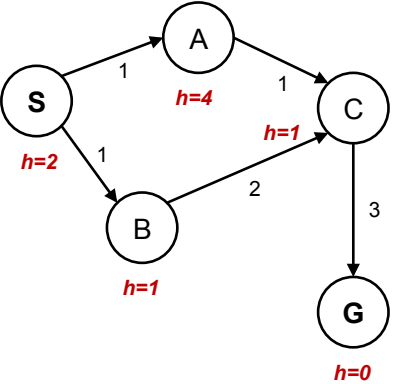
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Optimality of A*

- ▶ admissible h for tree search
- ▶ consistent h for graph search
- ▶ What about UCS?
- ▶ Are all consistent heuristics also admissible?
 $h(A) - h(C) \leq \text{cost}(A \rightarrow C)$

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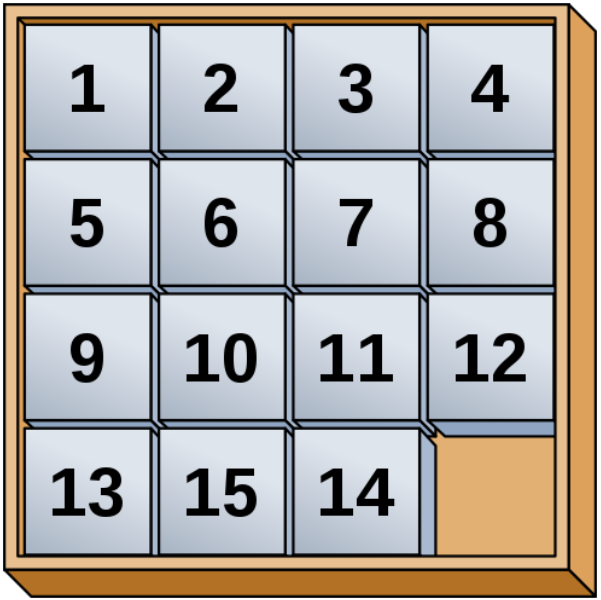
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How to find a heuristics?



Which heuristics is the best?