

Problem solving by search

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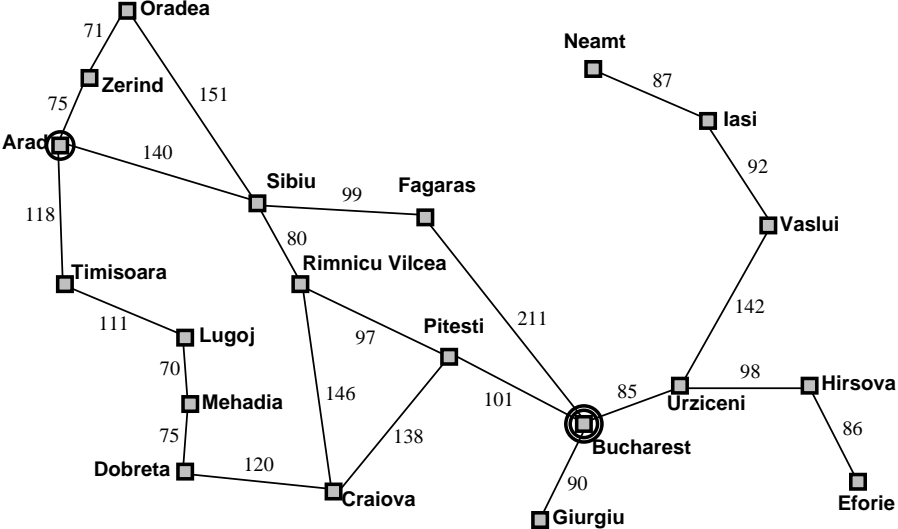
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Outline

- ▶ Search problem.
- ▶ State space graphs.
- ▶ Search trees.
- ▶ Strategies, which tree branches to choose?
- ▶ Strategy/Algorithm properties?
- ▶ Programming infrastructure

Example: Romania



Example: Romania

Goal:

be in Bucharest

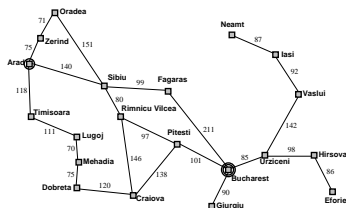
Problem formulation:

states: position in a city (cities)

actions: drive between cities

Solution:

Sequence of cities (path)



Example: The 8-puzzle

7	2	4
5		6
8	3	1

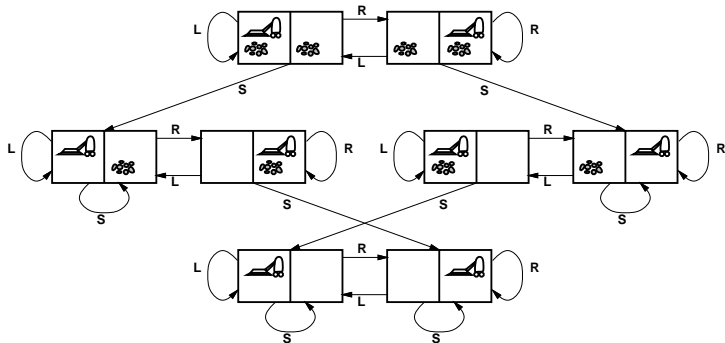
Start State

1	2	3
4	5	6
7	8	

Goal State

states?
actions?
solution?
cost?

Example: Vacuum cleaner



states?
actions?
solution?
cost?

A Search Problem

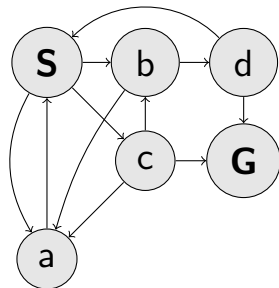
- ▶ **State space** (including Start/Initial state): position, board configuration,
- ▶ **Actions**: drive to, Up, Down, Left ...
- ▶ **Transition model**: Given state and action return state (and **cost**)
- ▶ **Goal test**: Are we done?

State Space Graphs

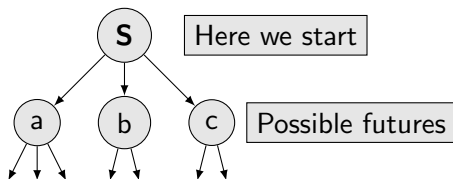
State space graph: a representation of a search problem

- ▶ Nodes are abstracted world configurations
- ▶ Arcs represent action results
- ▶ Goal test is a set of goal nodes

Each state occurs only *once* in a state (search) space.



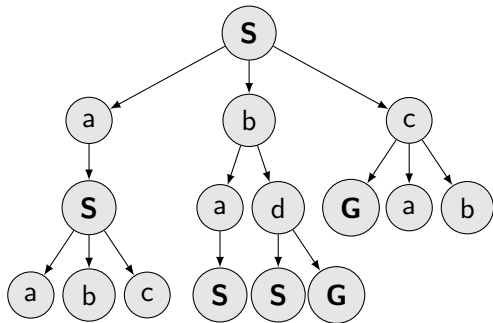
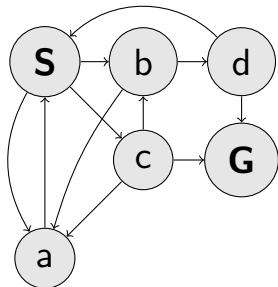
Search Trees



- ▶ A “what if” tree of plans and their outcomes
- ▶ Start node is the root
- ▶ Children are successors
- ▶ Nodes show states, but correspond to *plans* that achieve those states

What does the last item mean, actually?

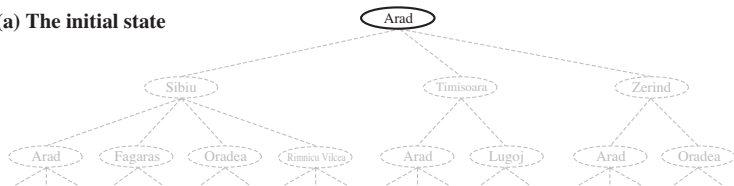
State Space Graphs vs. Search Trees



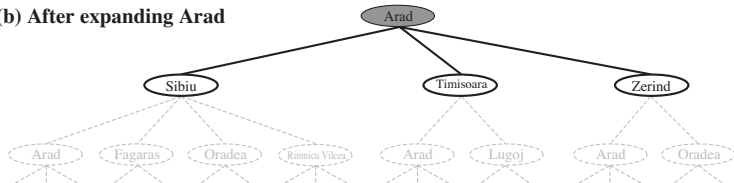
How big is the search tree?

Search tree for Romania

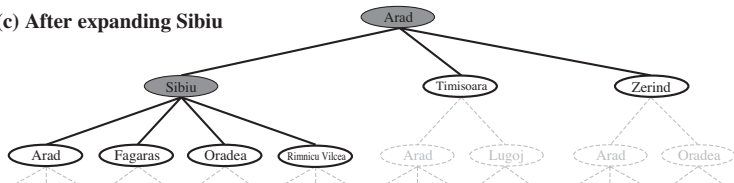
(a) The initial state



(b) After expanding Arad

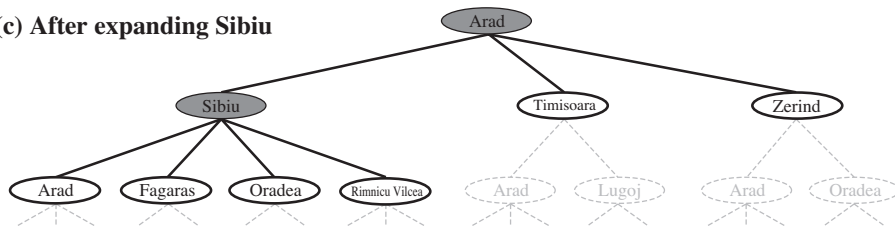


(c) After expanding Sibiu



Search elements

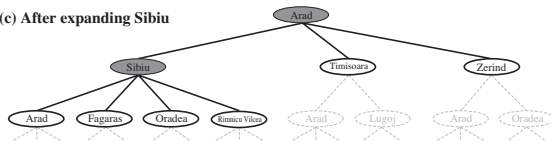
(c) After expanding Sibiu



- ▶ Expand **plans** - possible ways (**tree nodes**).
- ▶ Manage/Maintain **fringe** (or **frontier**) of plans under consideration.
- ▶ Expand new nodes *wisely(?)*.

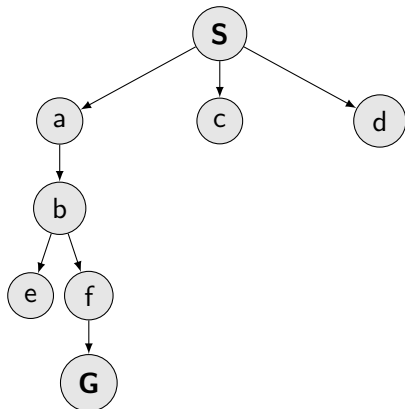
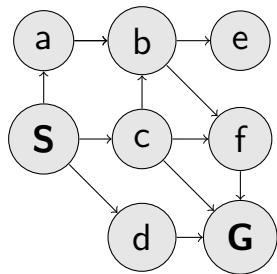
Tree search algorithm

(c) After expanding Sibiu



```
function TREE_SEARCH(problem) return a solution or failure
  initialize by using the initial state of the problem
  loop
    if no candidates for expansion then return failure
    else choose a leaf node for expansion
    end if
    if the node contains a goal state then return the solution
    end if
    Expand the node and add the resulting nodes to the tree
  end loop
end function
```

Example of a tree search



Which nodes to *explore*?

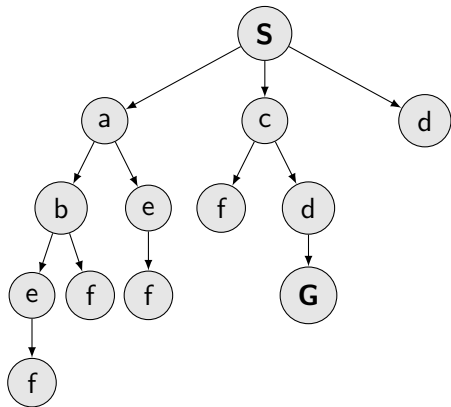
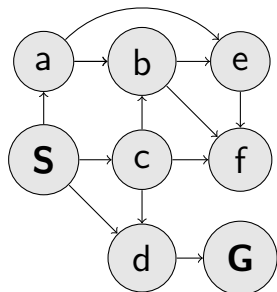
What are the properties of a strategy/algorithm?

Search (algorithm) properties

- ▶ **Complete?** Guaranteed to find a solution (if exists)?
- ▶ **Optimal?** Guaranteed to find the least cost path?
- ▶ **Time complexity?** How many steps - an operation with a node?
- ▶ **Space complexity?** How many nodes to remember?

How many nodes in a tree? What are tree parameters?

Depth-First Search (DFS)

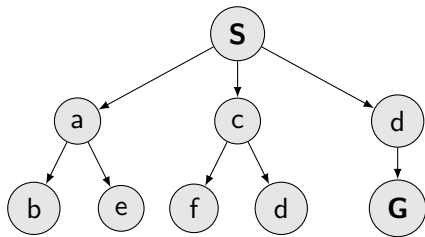
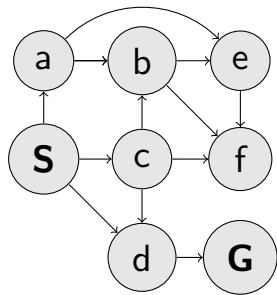


What are the DFS properties?

DFS properties

- ▶ Complete?
- ▶ Optimal?
- ▶ Time complexity?
- ▶ Space complexity?

Breadth-First Search (BFS)

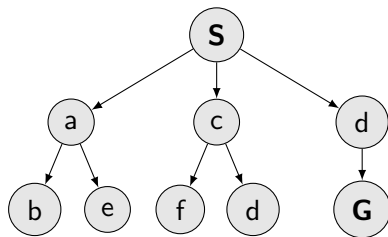
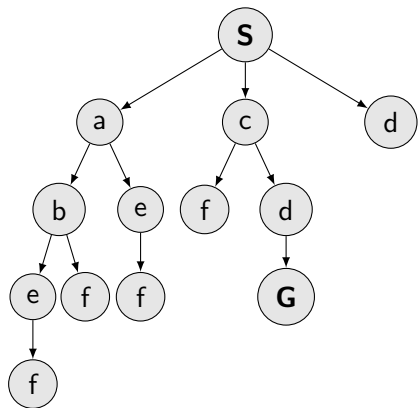


What are the BFS properties?

BFS properties

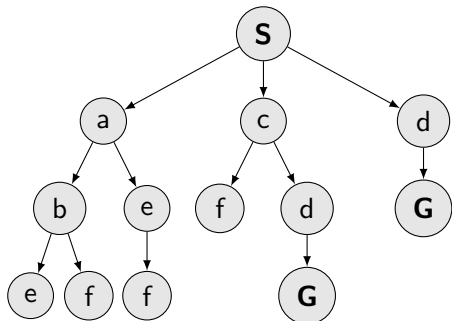
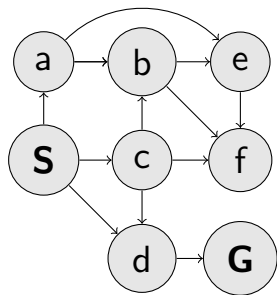
- ▶ Complete?
- ▶ Optimal?
- ▶ Time complexity?
- ▶ Space complexity?

DFS vs BFS



DFS with limited depth, $\text{maxdepth}=2$

Do not follow nodes with $\text{depth} > \text{maxdepth}$

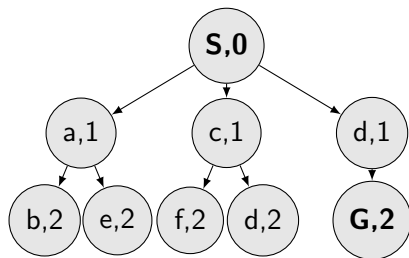
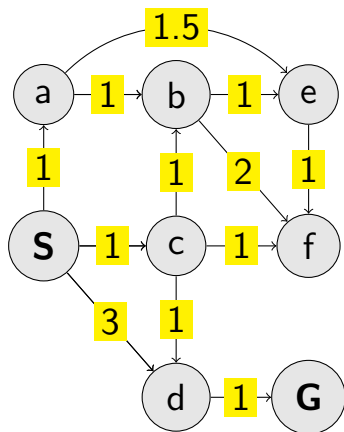


Iterative deepening DFS (ID-DFS)

- ▶ Start with `maxdepth = 1`
- ▶ Perform DFS with limited depth. Report success or failure.
- ▶ If failure, forget everything, increase `maxdepth` and repeat DFS

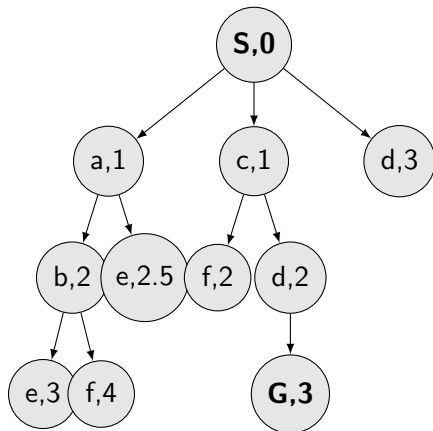
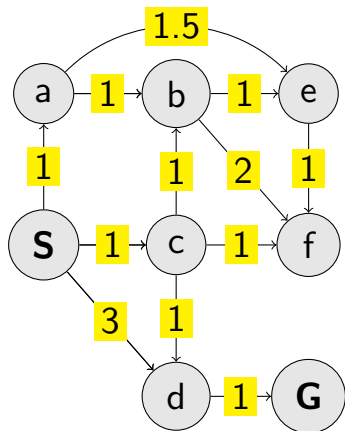
Is it not a terrible waste to forget everything between steps?

Cost sensitive search



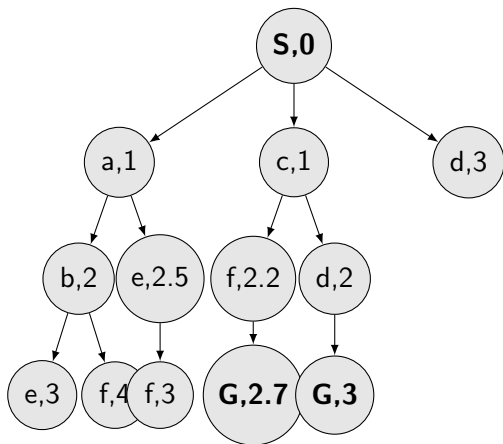
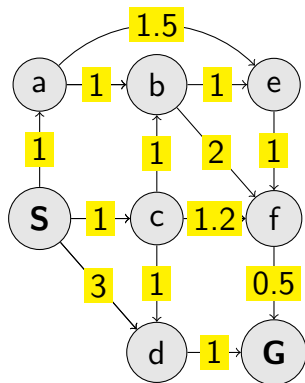
- ▶ In BFS, DFS, node \pm depth was the node-value.
- ▶ How was the depth actually computed?
- ▶ How to evaluate nodes with path cost?

Uniform Cost Search (UCS)

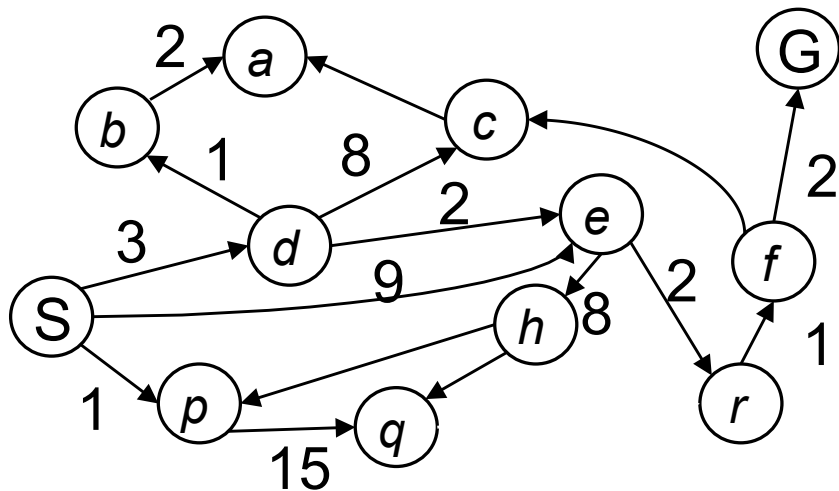


When to **check the goal** (and stop) the search? When visiting or expanding the node?

When to stop, when visiting or expanding?



Example: Graph with costs



UCS properties

Programming a Tree Search

Infrastructure for (tree) search algorithms

What should a `tree node n` now?

- ▶ `n.state`
- ▶ `n.parent`
- ▶ `n.pathcost`

Perhaps we may add something later, if needed ...

How to organize nodes?

The Python examples are just suggestions, ...

- ▶ A dynamically linked structure (`list()`).
- ▶ Add a node (`list.insert(node)`).
- ▶ Take a node and remove from the structure (`node=list.pop()`).
- ▶ Check the Python modules `heapq`¹ and `queue`² for inspiration.

¹<https://docs.python.org/3.5/library/heapq.html>

²<https://docs.python.org/3.5/library/queue.html>

What is the solution?

- ▶ We stop when **Goal** is reached.
- ▶ How do we construct the **path**?