A0B17MTB – Matlab

Part #1

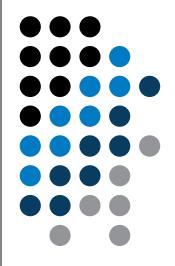


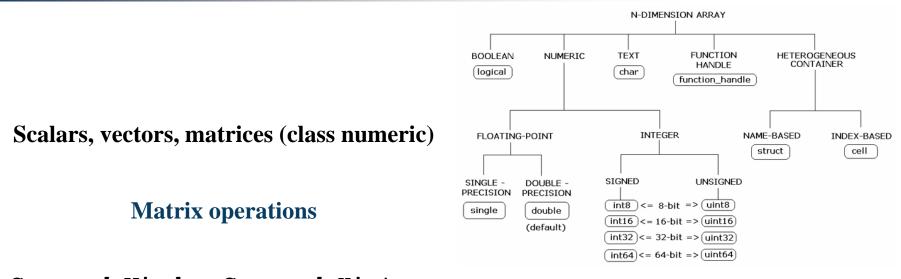
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Command Window, Command History

Saving and loading variables

Exercises



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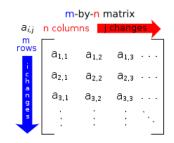
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Data types

Matrices in Matlab

- matrix is a basic data structure in Matlab
- there are following types depending on size :
 - 1×1 (scalar)
 - $M \times 1$, or $1 \times N$ (vector)
 - M×N (matrix)
 - array (multidimensional matrices) $M \times N \times P \times Q \times R \times ...$

- can be complex
- can contain text as well (beware the length)





Matrix creation

- following techniques are available:
 - element-by-element entering (suitable for small matrices only)
 - colon notation ,,: " to define elements of a series
 - generation by built-in functions
 - generation of matrices in m-files
 - import and export from/to external files (.mat, .txt, .xls)



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Matrix construction element-by-element

- test following commands to construct matrices by element enumeration
 - suitable for small matrices only

>> a1 = -1
>> a2 = [-1] % brackets are redundant

$$a_1 = a_2 = -1$$

$$\mathbf{v}_{1} = \begin{pmatrix} -1 & 0 & 1 \\ 0 \\ 1 \end{pmatrix}$$

$$>> v1 = \begin{bmatrix} -1 & 0 & 1 \\ >> v2 = \begin{bmatrix} -1 & 0 & 1 \\ 2 & 2 & 2 \end{bmatrix}$$

$$>> M1 = \begin{bmatrix} -1 & 0 & 1 \\ 2 & -1 & 2 & 2 \end{bmatrix}$$

$$>> M2 = \begin{bmatrix} -1 & 0 & 1 \\ 2 & 0 & 2 \end{bmatrix}$$

$$>> M3 = \begin{bmatrix} -1 & -2 \\ 2 & 0 & 2 \end{bmatrix}, \quad \mathbf{M}_{2} = \begin{pmatrix} -1 & -2 \\ 0 & 0 \\ 1 & 2 \end{bmatrix}, \quad \mathbf{M}_{3} = \begin{pmatrix} -1 & -2 \\ 0 & 0 \end{bmatrix}$$



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Matrix construction element-by-element

90 s

- construct following matrices:
 - matrix values are defined inside square brackets []
 - semicolon ,,; " separates individual rows of a matrix

$$\mathbf{A} = \begin{pmatrix} -1 & 1 \\ 1 & -2 \end{pmatrix} \qquad \mathbf{B} = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$



Data types

120 s

• semicolon placed at the end of a command suppresses display of the output in Command Window

• when more than one command on the same line, coma is used to separate each command

• note: it is possible to copy and paste code including ">>"

 $\mathbf{c} = \begin{pmatrix} 1 & 0 & 0 \end{pmatrix} \qquad \mathbf{d} = \begin{vmatrix} 0 \\ 0 \end{vmatrix}$



• "row" vs. "column" vector

Matrix construction

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Workspace browser

- new variables
- deleting / modification of existing variables
- saving / loading
- size, elements of variables
 - other information can be added
- fast data plotting option

 all operations can be carried out using Matlab functions that we learn later, e.g. min, max, size, length

| Workspace -+ - <th< th=""><th></th><th></th><th></th><th></th><th></th><th></th><th>X 5 D</th></th<> | | | | | | | X 5 D |
|--|--|-------------|----------|---------------|------------|-----------------|-------|
| Name Value Size Min Max I [-1,1;1,-2] 2x2 -2 1 B [1,2,3;4,5,6;7,8,9] 3x3 1 9 a 1 1x1 1 1 b 5 1x1 5 5 c [1,0,0] 1x3 0 1 d [0;0;1] 3x1 0 1 | | | | Charden Ray | | | |
| es A [-1,1;1,-2] 2x2 -2 1 B [1,2,3;4,5,6;7,8,9] 3x3 1 9 a 1 1x1 1 1 b 5 1x1 5 5 c [1,0,0] 1x3 0 1 d [0;0;1] 3x1 0 1 | | | | Stack: Bas | - | | |
| a 1 1x1 1 1 b 5 1x1 5 5 c [1,0,0] 1x3 0 1 d [0;0;1] 3x1 0 1 | | | | | | | |
| a 1 1x1 1 1 b 5 1x1 5 5 c [1,0,0] 1x3 0 1 d [0;0;1] 3x1 0 1 | es | | | | | | |
| b 5 1x1 5 5 c [1,0,0] 1x3 0 1 d [0;0;1] 3x1 0 1 | .00 | | | ;4,5,6;7,8,9] | | | |
| c [1,0,0] 1x3 0 1 d [0;0;1] 3x1 0 1 | | | | | | | |
| d [0;0;1] 3x1 0 1 | | | | | | | |
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| | X 🗈 💼 | A 3 3 | | | | | 1) 🔻 |
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| 1 2 3 4 5 6 7 | X Image: Comparison of the second secon | A 2 1 | | | | | 1) 🔻 |
| 1 2 3 4 5 6 7 -1 1 | 2x2 double> | A 2 1 | | | | | 1) 🔻 |
| 1 2 3 4 5 6 7 -1 1 | X Image: Comparison of the second secon | A 2 1 | | | | | 1) 🔻 |
| 1 2 3 4 5 6 7 -1 1 | X Image: Comparison of the second secon | A 2 1 | | | | | 1) 🔻 |



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Program flow

Workspace browser

- Workspace now contains variables A, B, a, b, c, d (from previous slides)
 - all variables in the base workspace are displayed
- variable ans contains the last result
 - can be used for calculation
 - overwritten by each command input!

>> 2*2, ans^2

- try to edit variables A, a
 - by a Matlab command directly
 - by change of value in Workspace browser
- try to delete variables B, c

| Workspace | lu-t | | |
|-----------|---------------------|-----|-----|
| Name 🛆 | Value | Min | Max |
| A | [-1 1;1 -2] | -2 | 1 |
| H B | [1 2 3;4 5 6;7 8 9] | 1 | 9 |
| 🕂 a | 1 | 1 | 1 |
| 🕂 b | 5 | 5 | 5 |
| 🕂 c | [100] | 0 | 1 |
| 🕂 d | [0;0;1] | 0 | 1 |
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Basic math operators

- of several types:
 - arithmetic
 - matrix
 - vector
 - relational
 - logical
 - and other (to be mentioned later...)

- other operations using Matlab functions
 - complex conjugate,
 - sum, determinant, square root
 - and hundreds of other functions ...

- subtraction
- * multiplication
- ^ power
- ' transpose
- \land left matrix division
- / right matrix division
- . dot notation



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Operator Precedence in Matlab

- according to the following table
 - see Matlab \rightarrow Language Fundamentals \rightarrow Operators and Elementary Operations \rightarrow Arithmetic

| | 1 | parentheses | () | | | | | |
|--------------------|----|---|-----|-----|----|-------------|----|----|
| rity | 2 | transpose, power | Ţ | . ' | ^ | • ^ | | |
| higher priority | 3 | unary plus, unary minus, logical negation | + | - | ~ | | | |
| | 4 | multiplication, division | * | •* | / | \setminus | ./ | .\ |
| | 5 | addition, subtraction | + | - | | | | |
| | 6 | colon operator | : | | | | | |
| | 7 | relational operators | < | > | <= | >= | == | ~= |
| | 8 | logical AND (element-wise) | æ | | | | | |
| /er rity | 9 | logical OR (element-wise) | I | | | | | |
| lower priority | 10 | logical AND (short-circuit) | & & | | | | | |
| ¥ | 11 | logical OR (short-circuit) | | | | | | |



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Basic math operators

200 s

- type in following commands
 - zero can be omitted with a decimal number beginning with zero (not recommended!)

>> a3 = -2/4 >> a4 = -0.5 >> a5 = -.5

- what is the difference between a3, a4, a5?
- beware the precedence of operators (we see in the next slides):

>> 3*5*6
>> a1 = 15
>> a2 = 10;
>> a2/a3
>> a2/a3*a4
>> a2/(a3*a4)

- explain the difference between a2/a3*a4 and a2/(a3*a4)
- verify the rules of operator precedence from the previous slide



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Lengthy commands in Matlab

120 s

- it is suitable to structure command blocks for clarity:
 - next line: SHIFT+ENTER

>> A = [1 1 1]; B = [2 2 2]; % SHIFT+ENTER C = [2 3 2];

- three dots notation
 - for continuation of the same command on the next line
 - compare results:



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Basic math functions

• math functions in Matlab are generally divided in three groups:

• <u>scalar</u>

- function operates over individual elements of a matrix
- e.g.: sin, sqrt, log, factorial

• <u>vector</u>

- Function operates over individual rows/columns of a matrix
- e.g.: sum, max

• <u>matrix</u>

- function operates over whole matrix
- e.g.: det, trace



Basic math functions #1

600 s

- using Matlab help, calculate following expression: $a\sin^2(\alpha) + a\cos^2(\alpha) a$
 - use numerical values you choose

• verify following logarithmic identity:

$$\log_{10}(a) + \log_{10}(b) - \log_{10}(ab) = 0$$

• find sum of all elements in individual rows of the following matrix

$$\mathbf{T} = \begin{pmatrix} \frac{1}{2} & \frac{1}{3} & \frac{1}{4} & \frac{1}{5} \\ 6 & 7 & 8 & 9 \\ 0.2 & 0.3 & 0.4 & 0.5 \end{pmatrix}$$



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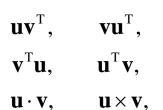
Α

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Basic math functions #2

- assume following vectors \mathbf{u}, \mathbf{v} : $\mathbf{u} = \begin{pmatrix} 1 & 2 & 3 \end{pmatrix}, \mathbf{v} = \begin{pmatrix} 3 & 2 & 1 \end{pmatrix}$
 - calculate



- following functions are needed:
 - transpose (. ') of a matrix
 - dot scalar product
 - cross product
- what is the result of the above mentioned operations?



wikipedia.org



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Basic math functions #3

use following code and round the resulting number to:

- (a) nearest integer
- (b) nearest integer greater than r
- (c) nearest integer lower than r
- (d) zero
- note: one of the functions is called round (e) zero with precision of 2 decimal digits
- find remainder after r is divided by 0.1
 - modulus vs. remainder after division

>> r = 1 + 10 * rand(1)



420 s

Matrix division in Matlab

- matrix operation
- two cases are distinguished: <u>left</u> division ("\" mldivide) and <u>right</u> division ("/" - mrdivide)
 - A is invertible (regular), b is row (column) vector

| $\mathbf{A}\mathbf{x} = \mathbf{b}$ | | $\mathbf{x}\mathbf{A} = \mathbf{b}$ |
|--|---------------------|--|
| | solution to linear | |
| | system of equations | |
| $\mathbf{x} = \mathbf{A}^{-1}\mathbf{b}$ | | $\mathbf{x} = \mathbf{b}\mathbf{A}^{-1}$ |

$$>> x = A \setminus b$$



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500 s

- find the sum of diagonal elements (trace of a matrix) of the matrix T with elements coming from normal distribution with mean equal to 10 and standard deviation equal to 4
 > T = 10 + 4*randn(7, 7);
- find determinant of matrix **U**

$$\mathbf{U} = \begin{pmatrix} 1 & 2 & \frac{17}{81} \\ 0 & 2 & 0 \\ 0 & -2 & -1 \\ & & & \end{pmatrix}$$

• solve the linear system of equations

$$x_{1} + 2x_{2} + 3x_{3} = 6$$

$$4x_{1} + 5x_{2} + 6x_{3} = 15$$

$$7x_{1} + 8x_{2} + x_{3} = 16$$

Ax = **b**
x = **A**⁻¹**b**



Matlab commands

- Matlab is cAsE sEnSiTiVe
 - almost entirely, with certain exceptions (properties of graphic objects, ...)
 - pay attention to typos and variable names (see later)
 - new versions of Matlab offer certain options

- beware of different syntax in Mathematica
 - following syntax is incorrect both in Matlab and Mathematica:

>> Sin(pi/2) % function names start with lower case
>> cos[pi/3] % function input is in parentheses ()



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Predefined values in Matlab

- Matlab contains several predefined values
 - eps precision of single/double numbers
 - eps determines the shortest distance between two single/double numbers
 - ans most recent answer
 - NaN not a number (every expression containing NaN results is NaN)
 - NaN can be used advantageously in some cases
 - Inf *infinite number* (variable Inf can be used in calculation :))
 - pay attention to Inf propagation throughout your code (use allowed operations only)
 - i, j complex unit
 - they are all basically functions (without input parameters)
 - check results of the following expressions:

| >> | t1 | = | 10/0 | | 0/0 | t1 | = | Inf | |
|----|----|---|------|----|-----|----|---|-----|--|
| >> | t2 | = | 0/0 | | 0/0 | t2 | = | NaN | |
| >> | t3 | = | t1*5 | | 0/0 | t3 | = | Inf | |
| >> | t4 | = | t1 + | t2 | 010 | t4 | = | NaN | |

• pi, intmin, intmax, realmin, realmax, ... (functions)

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Workspace - output deletion #1

• to clean (erase) the command window:

>> home % cursor (>>) is shifted to the top-left position
>> clc % Command Window is erased

• try and compare





Workspace - output deletion #2

• to clean one (or more) variable, use clear

| >> clear | % whole Workspace is deleted |
|----------------|--|
| >> clear XX | % variable XX is deleted |
| >> clear XX YY | % variables XX and YY are deleted |
| >> clear z* | <pre>% everything starting with 'z' is deleted</pre> |

- clear clear has a number other options (graphics, I/O)
- try to delete selected variables in workspace



Workspace - output deletion #3

• to delete all variables except for one (or several):

```
>> clearvars -except a3 % clears everything except a3
```

• further information in doc clear, doc clearvars



Command History window

- Command History window stores all commands from the Command Window
- Command History accessible though (\uparrow or \downarrow)
- it is possible to filter out past commands by

• e.g.
$$>> A = [+ \uparrow]$$

- It is possible to copy-and-paste entire Command History
 - SHIFT / CTRL / CTRL+A \rightarrow CTRL+C

| Command History | | \odot | | | |
|---|-------------------------|---------|--|--|--|
| $v = [1 \ 2 \ 17/81; 0]$ | 2 0; | | | | |
| 0 -2 -1]; | | | | | |
| det (U) | | | | | |
| clear,clc | | | | | |
| $- \pi = 10 + 4 + randn(10, 10);$ | | | | | |
| trace(T) | | | | | |
| | 2 0; | | | | |
| 0 -2 -1]; | Evaluate Selection | 50 | | | |
| det (U) | Create Script | ГЭ | | | |
| A = [1 2 3; 4 5] | Create Shortcut | | | | |
| $b = [6 \ 15 \ 16]';$ | Profile Code | | | | |
| x = inv(A) *b; | Cut | Ctrl+X | | | |
| $\mathbf{x} = \mathbf{A} \setminus \mathbf{b};$ | Сору | Ctrl+C | | | |
| t1 = 10/0 % t | Delete Selection | Delete | | | |
| $t_2 = 0/0$ % t | Delete to Selection | | | | |
| | Select All | Ctrl+A | | | |
| | Find | Ctrl+F | | | |
| t4 = t1 + t2 t | Print | Ctrl+P | | | |
| home % vrátí pro | Print Selection | Curri | | | |
| ⁱ clc % vymaže Co | Page Setup | | | | |
| | Clear Command Histor | | | | |
| | Cicar Contindito Histor | 7 | | | |

• later on, we will work with scripts and functions to store all the commands/code

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Variables storing and loading

• existing variables in Matlab Workspace can be stored on disk

```
>> save % stores all variables in matlab.mat in current folder
>> save task1 % stores all variables in task1.mat
>> save task1 a b c % stores variables "a", "b" and "c" in task1.mat
```

- CTRL+S in Command Window/Command History
- loading variables is analogical

```
>> load % loads matlab.mat in current folder
>> load task1 % loads all variables from task1.mat
>> load task1 a b c % loads variables "a", "b" and "c" from task1.mat
```

• alternatively, drag & drop the file from Current Folder in Command Window



Storing history and variables

180 s

- save today's Command History
 - use *.txt file
- store all variables from Workspace in Data.mat

• try to store selected variables only

• clear Workspace and load above mentioned files

• both storing and loading can be carried out using mouse!!

A0B17MTB: Part #1

.mat file structure

- .mat files of the 7.3 version have the HDF5 format
 - HDF = Hierarchical Data Format
 - enable to store variables exceeding 2GB (64-bit system)
 - scientific format for data storing
- advantages of accessing HDF directly for certain applications:
 - speed
 - it is possible to define structure of the file and the stored data
 - Matlab *High-Level* functions and HDF *Low-Level* functions are available
- for more detailed information see:
 - MATLAB → Data and File Management → Data Import and Export → Scientific Data



Variable names #1

- max. 63 characters starting with a letter (>> namelengthmax)
 - underscore is allowed in the variable name ,,_" (not at the beginning!)
 - characters not allowed are colon ,, : ", hyphen ,, -" and others
- lowercase letters in the names of scalars and variables (a = 17.59;)
- matrix names usually start with a capital letter $(A = [\dots])$
 - clear huge matrices after they are used (clear ..., memory')
- iteration variables, variables used in for cycles usually named m, n, k etc.
 - it is advisable to avoid i, j (complex unit)
- chose the names to correspond to the purpose of the variable
- avoid, if possible, standalone letter 'l' (to be confused with 1) and predefined variables in Matlab environment



Variable names #2

• exceeding the maximum variable's name length :

>> a012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789
Warning: 'a012345678901230

a01234567890123456789012345678901234567890123456789012345678901 =

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Variable names #3

• samples of valid variable names

a, A, b, c, x1, x2, M_12, test1, matrix_A, fx, fX

• samples of invalid variable names

| lvar | % starts with a number (not possible in Matlabu) |
|----------|--|
| matrix A | % contains space |
| coef.a | <pre>% possible only if coef is of type 'struct'</pre> |
| Test-1 | % algebraic expression: ans = Test - 1 |
| f(y) | % makes sense when using symbolic expressions |

- samples of valid numbers in Matlab
 - pay attention to miss inserted spaces after exponent and imaginary unit

3, -66, +0.0015, .015, 1.6025e-10, 3i, 3.17e5i, -3.51j



Discussed functions

| sin, cos | trigonometric functions |
|-------------------------|--|
| sqrt | square root |
| max | largest element of column of a matrix; largest element of a vector |
| sum | sum of elements of column of a matrix; sum of elements of a vector |
| log, log10 | natural logarithm, logarithm with base 10 |
| factorial | factorial |
| det, trace | determinant of a (square) matrix, trace of a (square) matrix |
| transpose | transpose |
| dot, cross | scalar product, vector product • |
| inv | invers of a matrix |
| round, ceil, floor, fix | rounding |
| rem | remainder after division |
| rand, randn | random number generation |
| save, load | storing, loading of variables |
| clear, clearvars | eleting variables and functions, deleting variables only |
| home, clc | command prompt shift, clears output |
| ans, eps | returns last answer, numerical accuracy of Matlab |



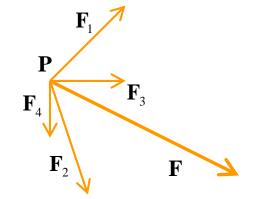


• forces were localized at point **P** in (x - y) plane:

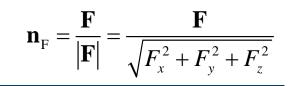
F₁ =
$$\begin{pmatrix} 2 & 2 \end{pmatrix}$$

F₂ = $\begin{pmatrix} 1 & -3 \end{pmatrix}$
F₃ = $\begin{pmatrix} 2 & 0 \end{pmatrix}$
F₄ = $\begin{pmatrix} 0 & -1.5 \end{pmatrix}$

• what is the direction of the resultant force **F**?



• normalize the resulting vector







240 s

- type-in following commands:
 - >> clear, clc; >> w1 = [1 2 3 4], w2 = [-2 -3 -4] >> w3 = [-2; -3; -4] >> w4 = w1^2, w5 = w2 - w1

- compare differences
- the error of calculating w5 resides in what?
- try also

>> w3*3, w1 - 3, >> w1 + [5 5 5 5], >> w6 = 5*w1 - [3 5 6] - w2

- calculate the norm (magnitude) of vector w1
 - try more options

$$\hat{\mathbf{w}}_1 = \frac{\mathbf{w}_1}{\left|\mathbf{w}_1\right|}$$

• how to modify the calculation in the case of a complex vector?



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Exercise #3

- calculate roots of the quadratic function
 - rearrange the terms of the function first

$$2x^{2} + 5x + 3 = 0, \implies a = 2, b = 5, c = 3$$
$$x_{1,2} = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a} = \frac{-5 \pm \sqrt{25 - 24}}{4}$$
$$x_{1} = -1, \quad x_{2} = -\frac{3}{2}$$

• Matlab provides particular function for calculation of roots of a function, try to search it out

 $-2x^2 - 5x = 3$



180 s

Exercise #4

 \mathbf{Z}_{i}

xŁ

300 s

- consider matrices (prepare matrices for later use)
 - rotating by angle α in *x*-*z* plane

$$\mathbf{R} = \begin{pmatrix} \cos(\alpha) & 0 & -\sin(\alpha) \\ 0 & 1 & 0 \\ \sin(\alpha) & 0 & \cos(\alpha) \end{pmatrix}$$

• mirroring across plane 1x + 2y + 0z = 0• use Householder's transform $\mathbf{P} = \mathbf{I} - 2\mathbf{n}_0 \mathbf{n}_0^{\mathrm{T}}$

$$\mathbf{n}_{0} = \frac{\mathbf{v}_{1} \times \mathbf{v}_{2}}{|\mathbf{v}_{1} \times \mathbf{v}_{2}|} \qquad \mathbf{P}_{1} = \begin{bmatrix} -2; 1; 0 \end{bmatrix}$$
$$\mathbf{P}_{2} = \begin{bmatrix} 0; 0; 1 \end{bmatrix}$$
$$\mathbf{v}_{k} = \left(\mathbf{P}_{k} - \mathbf{0}\right) \begin{pmatrix} \mathbf{x}_{0} \\ \mathbf{y}_{0} \\ \mathbf{z}_{0} \end{pmatrix}, \quad k \in \{1, 2\}$$

 $\mathbf{x}_{1} \mathbf{P}_{2} \mathbf{P}_{1}$ $\mathbf{x}_{1} \mathbf{P}_{0} \mathbf{1}$ \mathbf{y}_{1}



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• use rotation matrix **R** to rotate vector $\mathbf{k} = [1; 0; 0]$ by angle $\alpha = \pi/2$

$$\mathbf{m} = \mathbf{R}\mathbf{k} = \begin{pmatrix} 0 & 0 & 1 \end{pmatrix}^{\mathrm{T}}$$

• use reflection matrix **P** across plane: 1x+2y+0z=0

to mirror vectors:

$$\mathbf{u}_1 = \mathbf{n}_0, \quad \mathbf{u}_2 = \left(\frac{5}{2} \quad 0 \quad 3\right)^T$$

 $\mathbf{m}_1 = \mathbf{P}\mathbf{u}_1 = -\mathbf{n}_0, \quad \mathbf{m}_2 = \mathbf{P}\mathbf{u}_2 = \left(\frac{3}{2} \quad -2\right)^T$

- calculate the determinant of matrices **R** and **P**
 - can you interpret the results?



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180 s

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Thank you!



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