Homework 4 for the Physics for OI

This homework is focused on the motion in a rotating system and on the Coriolis' force calculation.

<u>The problem</u>: A circular disk of radius $r_1 = 2$ m rotates around the vertical axis with constant angular velocity $\omega = 8 \text{ s}^{-1}$. At a distance $r_0 = 0.5$ m from the axis there is a sphere of mass m = 0.25 kg inside a radial groove on the disk. Assume that the sphere is fixed at the r_0 position and released at the moment t = 0.



Your tasks:

- a) To evaluate and plot the time dependence of the distance of the sphere from the disk centre r(t).
- b) To evaluate and plot the time dependence of the sphere's velocity relative to the center of the disk v(t).
- c) To evaluate and plot the time dependence of the centrifugal acceleration acting on the sphere $a_n(t)$.
- d) To evaluate and plot the time dependence of the magnitude of Coriolis' force acting on the sphere $F_c(t)$.

Additional instructions and hints:

Build up the basic differential equation. You will need the second Newton's law and the relation for the centrifugal force. Use initial conditions as additional equations for the *DSolve*.

Calculate consequently r(t), v(t), $a_n(t)$ and $F_c(t)$.

Calculate exact time corresponding to the moment when the sphere reaches the edge of the disk (*FindRoot*). Plot all four graphs separately using blue thick line and choose convenient *PlotRange*.

Each graph should contain the maximum value corresponding to the edge of the disk (r_1) . The value can be represented by horizontal dashed red line, for example.

Recommended functions for the *Plot – GridLines*, *Frame*, *PlotStyle* and *PlotRange*.

Note: You can check your general solution for the r(t) at the problem 1-57 in the textbook.