# Robotic Information Garthering -**Exploration of Unknown Environment**

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Lecture 09

B4M36UIR - Artificial Intelligence in Robotics

## Overview of the Lecture

- Part 1 Robotic Information Gathering Robotic Exploration
  - Robotic Information Gathering
  - Robotic Exploration
  - TSP-based Robotic Exploration
  - Robotic Information Gathering

Part I

Part 1 – Robotic Exploration

## Robotic Information Gathering

Create a model of phenomena by autonomous mobile robots performing measurements in a dynamic unknown environment.

















## Challenges in Robotic Information Gathering

- Where to take new measurements?
  - To improve the phenomena model
- What locations visit first?
  - On-line decision-making
- How to efficiently utilize more robots?

To divide the task between the robots

■ How to navigate robots to the selected locations?

Improve Localization vs Model

Learning adaptivity Robotic Information Gathering

Sensing Planning

the on-line decision-making

- It includes the problems of:
  - Map building and localization Determination of the navigational waypoints

Time, energy, map quality vs robots, communication

How to efficiently utilize a group of mo-

bile robots to autonomously create a map of an unknown environment

Performance in a real mission depends on

Performance indicators vs constraints

Robotic Exploration of Unknown Environment

■ Robotic exploration is a fundamental problem of robotic information gathering

- Path planning and navigation to the waypoints
- Coordination of the actions (multi-robot team)



Courtesy of M. Kulich

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free space

# Mobile Robot Exploration

- Create a map of the environment
- Frontier-based approach

Yamauchi (1997)

Occupancy grid map

Moravec and Elfes (1985)

- Laser scanner sensor
- Next-best-view approach

Select the next robot goal



Performance metric:

Time to create the map of the whole environment

search and rescue mission

# Environment Representation – Mapping and Occupancy Grid

How to address all these aspects altogether to find a cost

efficient solution using in-situ decisions?

- The robot uses its sensors to build a map of the environment
- The robot should be localized to integrate new sensor measurements into a globally consistent map
- SLAM Simultaneous Localization and Mapping
  - The robot uses the map being built to localize itself
  - The map is primarily to help to localize the robot
  - The map is a "side product" of SLAM
- Grid map discretized world representation
  - A cell is occupied (an obstacle) or free
- Occupancy grid map
  - Each cell is a binary random variable modeling the occupancy of the cell





## Occupancy Grid

■ The problem is:

- Assumptions
  - The area of a cell is either completely free or occupied
  - Cells (random variables) are indepedent of each other
  - The state is static
- A cell is a binary random variable modeling the occupancy of the cell
  - Cell  $m_i$  is occupied  $p(m_i) = 1$
  - Cell  $m_i$  is not occupied  $p(m_i) = 0$
  - Unknown  $p(m_i) = 0.5$
- Probability distribution of the map m

$$p(m) = \prod_i p(m_i)$$

**E**stimation of map from sensor data  $z_{1:t}$  and robot poses  $x_{1:t}$ 

$$p(m|z_{1:t},x_{1:t}) = \prod_i p(m_i|z_{1:t},x_{1:t})$$

Binary Bayes filter - Bayes rule and Markov process assumption

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# Binary Bayes Filter 1/2

- Sensor data  $z_{1:t}$  and robot poses  $x_{1:t}$
- Binary random variables are indepedent and states are static

$$\begin{array}{cccc} \rho(m_{i}|z_{1:t},x_{1:t}) & \stackrel{\mathsf{Bayes \, rule}}{=} & \frac{\rho(z_{t}|m_{i},z_{1:t-1},x_{1:t})\rho(m_{i}|z_{1:t-1},x_{1:t})}{\rho(z_{t}|z_{1:t-1},x_{1:t})} \\ & \stackrel{\mathsf{Markov}}{=} & \frac{\rho(z_{t}|m_{i},x_{t})\rho(m_{i}|z_{1:t-1},x_{1:t})}{\rho(z_{t}|z_{1:t-1},x_{1:t})} \\ & \rho(z_{t}|m_{i},x_{t}) & = \frac{\rho(m_{i},z_{t},x_{t})\rho(z_{t},x_{t})}{\rho(m_{i}|x_{t})} \\ \hline \rho(m_{i},z_{1:t},x_{1:t}) & \stackrel{\mathsf{Bayes \, rule}}{=} & \frac{\rho(m_{i}|z_{t},x_{t})\rho(z_{t}|x_{t})\rho(m_{i}|z_{1:t-1},x_{1:t-1})}{\rho(m_{i}|x_{t})\rho(z_{t}|z_{1:t-1},x_{1:t-1})} \\ & \stackrel{\mathsf{Markov}}{=} & \frac{\rho(m_{i}|z_{t},x_{t})\rho(z_{t}|x_{t})\rho(m_{i}|z_{1:t-1},x_{1:t-1})}{\rho(m_{i})\rho(z_{t}|z_{1:t-1},x_{1:t})} \end{array}$$

 $I(m_i|z_t,x_t) + I(m_i,|z_{1:t-1},x_{1:t-1}) - I(m_i)$ 

recursive term

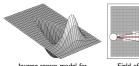
# Occupancy Mapping Algorithm

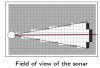
### Algorithm 1: OccupancyGridMapping( $\{l_{t-1,i}\}, x_t, z_t$ )

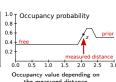
foreach m; of the map m do  $\overrightarrow{\text{if}}\ m_i$  in the perceptual field of  $z_t$  then  $I_{t,i} := I_{t-1,i} + \text{inv\_sensor\_model}(m_i, x_t, z_t) - I_0;$ 

return  $\{I_{t,i}\}$ 

Occupancy grid mapping developed by Moravec and Elfes in mid 80'ies for noisy sonars







## Algorithm 3: Frontier-based Exploration

map := init(robot, scan);

while there are some reachable frontiers do

Update occupancy map using new sensor data and Bayes rule;

 $\mathcal{M} :=$ Created grid map from *map* using thresholding;

 $\mathcal{M} :=$ Grow obstacle according to the dimension of the robot:

 $\mathcal{F} := \text{Determine frontier cells from } \mathcal{M}$ :

 $\mathcal{F} := \text{Filter out unreachable frontiers from } \mathcal{F}$ ;

f :=Select the closest frontier from  $\mathcal{F}$ , e.g. using shortest path; path := Plan a path from the current robot position to f;

Navigate robot towards f along path (for a while);

# Binary Bayes Filter 2/2

Probability a cell is occupied

$$p(m_i|z_{1:t},x_{1:t}) = \frac{p(m_i|z_t,x_t)p(z_t|x_t)p(m_i|z_{1:t-1},x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1},x_{1:t})}$$

Probability a cell is not occupied

$$p(\neg m_i|z_{1:t}, x_{1:t}) = \frac{p(\neg m_i|z_t, x_t)p(z_t|x_t)p(\neg m_i|z_{1:t-1}, x_{1:t-1})}{p(\neg m_i)p(z_t|z_{1:t-1}, x_{1:t})}$$

Ratio of the probabilities

$$\frac{p(m_i|z_{1:t},x_{1:t})}{p(\neg m_i|z_{1:t},x_{1:t})} = \frac{p(m_i|z_t,x_t)p(m_i|z_{1:t-1},x_{1:t-1})p(\neg m_i)}{p(\neg m_i|z_t,x_t)p(\neg m_i|z_{1:t-1},x_{1:t-1})p(m_i)} \\
= \frac{p(m_i|z_t,x_t)}{1-p(m_i|z_t,x_t)} \frac{p(m_i,z_{1:t-1},x_{1:t-1})}{1-p(m_i|z_{1:t-1},x_{1:t-1})} \frac{1-p(m_i)}{p(m_i)}$$

 $I(x) = \log \frac{p(x)}{1 - p(x)}$ 

 $p(x) = 1 - \frac{1}{1 - o/(x)}$ 

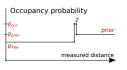
■ The product modeling the cell  $m_i$  based on  $z_{1:t}$  and  $x_{1:t}$ 

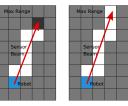
inverse sensor model

### Model for Laser Sensor

- The model is "sharp" with a precise detection of the obstacle
- For the range measurement d<sub>i</sub>, update the grid cells along a sensor







# Frontier-based Exploration

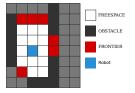
Logs Odds Notation

■ Log odds ratio is defined as

 $\blacksquare$  and the probability p(x) is

 $I(m_i|z_{1:t},x_{1:t}) =$ 

- The basic idea of the frontier based exploration is navigation of the mobile robot towards unknown regions Yamauchi (1997)
- Frontier a border of the known and unknown regions of the environment
- Based on the probability of individual cells in the occupancy grid, cells are classified into:
  - FREESPACE  $-p(m_i) < 0.5$
  - OBSTACLE  $-p(m_i) > 0.5$
  - UNKNOWN  $-p(m_i) = 0.5$
- Frontier cell is a FREESPACE cell that is incident with an UNKNOWN cell
- Frontier cells as the navigation waypoints have to be reachable, e.g., after obstacle growing

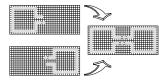


Use grid-based path planning

### Frontier-based Exploration Strategy Multi-Robot Exploration – Map Marge

■ The individual maps can be merged in a similar way as integration of new sensor measurements

$$\begin{split} P(occ_{x,y}) &= \frac{odds_{x,y}}{1 + odds_{x,y}} \\ odds_{x,y} &= \prod_{i=1}^{n} odds_{x,y}^{i}, \\ odds_{x,y}^{i} &= \frac{P(occ_{x,y}^{i})}{1 - P(occ_{x,y}^{i})} \end{split}$$



 $P(occ_{x,y}^i)$  is the probability that grid cell on the global coordinate is occupied in the map of the

We need the same global reference frame (localization).

## Multi-Robot Exploration – Overview

- We need to assign navigation waypoint to each robot, which can be formulated as the task-allocation problem
- Exploration can be considered as an iterative procedure
  - 1. Initialize the occupancy grid Occ
- 2. M ← create navigation grid(Occ) cells of M have values {freespace, obstacle, unknown}
- 3. **F** ← detect frontiers(M)
- Goal candidates G ← generate(F)
- 5. Assign next goals to each robot  $r \in R$ ,  $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}, \mathcal{M})$
- **6.** Create a plan  $P_i$  for each pair  $\langle r_i, g_n \rangle$
- 7. Perform each plan up to  $s_{max}$  operations
- At each step, update Occ using new sensor measurer 8. If |G| == 0 exploration finished, otherwise go to



- ploration performance, ■ How to determined goal candidates from the the frontiers?
- How to plan a paths and assign the goals to the robots?
- How to navigate the robots towards the goal?
- When to replan?
- etc.

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# Exploration Procedure – Decision-Making Parts

- 1. Initialize set plans for *m* robots,  $\mathcal{P} = (P_1, \dots, P_m), P_i = \emptyset$ .
- 2. Repeat
- 2.1 Navigate robots using the plans  $\mathcal{P}$ ;
- 2.2 Collect new measurements;
- 2.3 Update the navigation map  $\mathcal{M}$ ; Until replanning condition is met.
- 3. Determine goal candidates G from M.
- 4. If  $|\mathbf{G}| > 0$  assign goals to the robots
  - $(\langle r_1, g_{r_1} \rangle, \ldots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}, \mathcal{M}),$  $r_i \in \mathbf{R}, g_{r_i} \in \mathbf{G};$
  - Plan paths to the assigned goals  $\mathcal{P} = \mathsf{plan}(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle, \mathcal{M});$
  - Go to Step 2.
- 5. Stop all robots or navigate them to the depot

All reachable parts of the environment are explored

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set of m robots  $\mathbf{R} = \{r_1, r_2, \dots, r_m\}$ .

Exploration is an iterative procedure:

 $G(t) = \{g_1, g_2, \dots, g_n\}$ 

1. Collect new sensor measurements

2. Determinate a set of goal candidates

3. At time step t, select next goal for each

robot as the task-allocation problem

4. Navigate robots towards goal

Introducing utility as a computation of expected

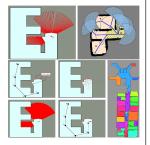
Map segmentation for identification of rooms and

exploration of the whole room by a single robot

 Consider longer planning horizon (as a solution of the Traveling Salesman Problem (TSP))

covered area from a frontier

Representatives of free edges



## Multi-Robot Exploration Strategy

- $\blacksquare$  A set of m robots at positions R = $\{r_1, r_2, \ldots, r_m\}$
- At time t, let a set of n goal candidates be  $\boldsymbol{G}(t) = \{g_1, \dots, g_n\}$



■ The exploration strategy (at the planning step t):

Select a goal  $g \in G(t)$  for each robot  $r \in R$  that will minimize the required time to explore the environment.

The problem is formulated as the task-allocation problem

$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}),$$

where M is the current map

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5. If |G(t)| > 0 go to Step 1; otherwise terminate

### **E** Evaluation for the number of robots m and sensor range $\rho$

Statistical Evaluation of the Exploration Strategies

 $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}(t))$ 

ρ	m	Iterative vs	Hungarian vs	MTSP vs
		Greedy	Iterative	Hungarian
3.0	3	+	=	+
3.0	5	+	=	+
3.0	7	+	=	+
3.0	10	+	+	_
4.0	3	+	=	+
4.0	5	+	=	=
4.0	7	+	=	+
4.0	10	+	+	_
5.0	3	+	=	+
5.0	5	+	=	<u> </u>
5.0	7	+	=	+
5.0	10	+	+	_

Total number of trials 14 280

## Improvements of the basic Frontier-based Exploration

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e.g., frontiers

using the distance cost function

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Several improvements have been proposed in the literature

Faigl, Kulich (2015)

A problem of creating a grid map of the unknown environment by a

González-Baños, Latombe (2002)

Holz, Basilico, Amigoni, Behnke (2010)

Zlot, Stentz (2006), Kulich, Faigl (2011, 2012)

Multi-Robot Exploration – Problem Definition

# Distance Cost Variants

- Simple robot-goal distance
  - Evaluate all goals using the robot-goal distance A length of the path from the robot position to the goal candidate
  - Greedy goal selection the closest one
  - Using frontier representatives improves the performance a bit



### ■ TSP distance cost

- Consider visitations of all goals Solve the associated traveling salesman problem (TSP)
- A length of the tour visiting all goals
- Use frontier representatives
- the TSP distance cost improves performance about 10-30% without any further heuristics, e.g., expected coverage (utility)



Kulich, M., Faigl, J., Přeučil, L. (2011): On Distance Utility in the Exploration Task. ICRA.

# Goal Assignment Strategies - Task Allocation Algorithms

### 1. Greedy Assignment

Yamauchi B. Robotics and Autonomous Systems 29, 1999

Randomized greedy selection of the closest goal candidate

### 2. Iterative Assignment

Werger B, Mataric M, Distributed Autonomous Robotic Systems 4, 2001

■ Centralized variant of the broadcast of local eligibility algorithm (BLE)

### 3. Hungarian Assignment

 Optimal solution of the task-allocation problem for assignment of n goals and m robots in  $O(n^3)$ 

Stachniss C, C implementation of the Hungarian method, 2004

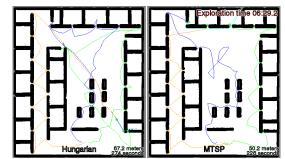
### 4. Multiple Traveling Salesman Problem - MTSP Assignment

(cluster-first, route-second), the TSP distance cost

Faigl et al. 2012

# Performance of the MTSP vs Hungarian Algorithm

■ Replanning as quickly as possible;  $m = 3, \rho = 3$  m



The MTSP assignment provides better performance

# MTSP-based Task-Allocation Approach

- Consider the task-allocation problem as the Multiple Traveling Salesman Problem (MTSP)
- MTSP heuristic ⟨cluster-first, route-second⟩
  - 1. Cluster the goal candidates G to m clusters

 $\boldsymbol{C} = \{C_1, \ldots, C_m\}, C_i \subseteq \boldsymbol{G}$ 

using K-means

2. For each robot  $r_i \in \mathbf{R}, i \in \{1, \dots m\}$  select the next goal  $g_i$  from Ci using the TSP distance cost

Kulich et at., ICRA (2011)

- Solve the TSP on the set  $C_i \cup \{r_i\}$
- the tour starts at r
- The next robot goal gi is the first goal of the found TSP tour
  - Faigl, J., Kulich, M., Přeučil, L. (2012): Goal Assignment using Distance Cost in

## Information Theory in Robotic Information Gathering

■ Employ information theory in control policy for robotic exploration

- **Entropy** uncertainty of x:  $H[x] = -\int p(x) \log p(x) dx$
- **Conditional Entropy** expected uncertainty of x after learning unknown z; H[x|z]
- Mutual information how much uncertainty of x will be reduced by learning z;  $I_{MI}[x;z] = H[x] - H[x|z]$
- Control policy is a rule how to select the robot action that reduces the uncertainty of estimate by learning measurements:

$$\operatorname{argmax}_{a \in A} I_{MI}[x; z|a],$$

where A is a set of possible actions, x is a future estimate, and z is future measurement

- Computation of the mutual information is computationally demanding
- Cauchy-Schwarz Quadratic Mutual Information (CSQMI) defined similarly to mutual information
  - A linear time approximations for CSQMI

Charrow, B. et al., (2015): Information-theoretic mapping using Cauchy-Schwarz Quadratic Mutual Information. ICRA.

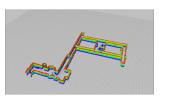
■ Compute CSQMI as Cauchy-Schwarz divergence  $I_{CS}[m; z]$  – raycast of the sensor beam and determine distribution over the range returns

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Actions

Actions are shortest path to cover the frontiers

# Example of Autonomous Exploration using CSQMI





Ground vehicle

■ Planning with trajectory optimization – determine trajectory maximizing I<sub>CS</sub> Charrow, B. et al., (2015): Information-Theoretic Planning with Trajectory Optimization for Dense 3D Mapping. RSS.

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Detect and cluster frontiers. Sampled poses to cover a cluster. Paths to the sampled pose

Select an action (a path) that maximizes the rate of

Cauchy-Schwarz Quadratic Mutual Information

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## Robotic Information Gathering

■ Robotic information gathering can be considered as the informative motion planning problem to a determine trajectory  $\mathcal{P}^*$  such that

$$\mathcal{P}^* = \operatorname{argmax}_{\mathcal{P} \in \Psi} I(\mathcal{P}), \text{ such that } c(\mathcal{P}) \leq B, \text{ where }$$

- Ψ is the space of all possible robot trajectories,
- $\blacksquare$   $I(\mathcal{P})$  is the information gathered along the trajectory  $\mathcal{P}$
- $\mathbf{c}(\mathcal{P})$  is the cost of  $\mathcal{P}$  and  $\mathcal{B}$  is the allowed budget
- Searching the space of all possible trajectories is complex and demanding problem
- A discretized problem can solved by combinatorial optimization techniques Usually scale poorly with the size of the problem
- A trajectory is from a continuous domain
- Sampling-based motion planning techniques can employed for finding maximally informative trajectories

Hollinger, G., Sukhatme, G. (2014): Sampling-based robotic information gathering algorithms. IJRR

Summary of the Lecture

# Topics Discussed

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Topics Discussed

- Robotic information gathering
- Robotic exploration of unknown environment
- Occupancy grid map
- Frontier based exploration
- Exploration procedure and decision-making
- TSP-based distance cost in frontier-based exploration
- Multi-robot exploration and task-allocation
- Mutual information and informative path planning informative and motivational
- Next: Multi-robot planning

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