Data Collection Planning with Curvature-Constrained

Dubins Traveling Salesman Problem with Neighborhoods (DTSPN)

Dubins Orienteering Problem with Neighborhoods (DOPN)

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Lecture 09

B4M36UIR - Artificial Intelligence in Robotics

B4M36UIR - Lecture 09: Data Collection with Dubins Vehicles

g₂ can be characterized as one of two main types

■ The optimal paths are called **Dubins maneuvers**:

• Constant velocity: v(t) = v and turning radius ρ

Optimal Maneuvers for Dubins Vehicle

■ CSC type: LSL, LSR, RSL, RSR;

■ CCC type: LRL, RLR;

values $u \in \{-1, 0, 1\}$

Dubins Vehicle and Dubins Planning

■ Provide curvature-constrained path to collect the most valuable measurements with shortest possible path/time or under limited travel budget

Motivation – Surveillance Missions with Aerial Vehicles



- Formulated as routing problems with Dubins vehicle
 - Dubins Traveling Salesman Problem with Neighborhoods
 - Dubins Orienteering Problem with Neighborhoods

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■ The optimal path connecting two configurations can be found analytically

■ The Dubins maneuvers can also be used in randomized-sampling based

■ Dubins vehicle model can be considered in the multi-goal path planning

■ Surveillance, inspection or monitoring missions to periodically visits

Given a sequence of locations, what is the shortest path visting the locations,

Given a set of locations, what is the shortest Dubins path that visits each

Given a set of locations, each with associated reward, what is the Dubins path

visiting the most rewarding locations and not exceeding the given travel budget

motion planners, such as RRT, in the control based sampling

i.e., what are the headings of the vehicle at the locations

location exactly once and returns to the origin location

Dubins Traveling Salesman Problem (DTSP)

given target locations (areas) ■ Dubins Touring Problem(DTP)

■ Dubins Orienteering Problem (DOP)

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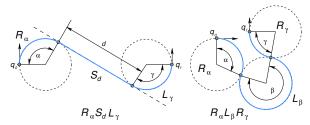
Parametrization of Dubins Maneuvers

■ Parametrization of each trajectory phase:

$$\{L_{\alpha}R_{\beta}L_{\gamma}, R_{\alpha}L_{\beta}R_{\gamma}, L_{\alpha}S_{d}L_{\gamma}, L_{\alpha}S_{d}R_{\gamma}, R_{\alpha}S_{d}L_{\gamma}, R_{\alpha}S_{d}R_{\gamma}\}$$

for $\alpha \in [0, 2\pi), \beta \in (\pi, 2\pi), d \ge 0$

Notice the prescribed orientation at q0 and qf



Overview of the Lecture

- Dubins Vehicle and Dubins Planning
- Dubins Touring Problem (DTP)

- Part 2 Bonus HW03b Data Collection Planning for

right (R)

■ For two states $q_1 \in SE(2)$ and $q_2 \in SE(2)$ in the environment without obstacles $\mathcal{W} = \mathbb{R}^2$, the optimal path connecting q_1 with

where S - straight line arc, C - circular arc oriented to left (L) or

Six types of trajectories connecting any configuration in SE(2) \blacksquare The control u is according to C and S type one of three possible

Part I

Part 1 - Data Collection Planning - Aerial

Surveillance Missions

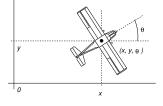
Dubins Vehicle

- as the Dubins vehicle
 - Limited minimal turning radius ρ

 - Position is $(x, y) \in \mathbb{R}^2$, vehicle heading is $\theta \in \mathbb{S}^2$, and thus

The vehicle motion can be

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = v \begin{bmatrix} \cos \theta \\ \sin \theta \\ \frac{u}{\rho} \end{bmatrix}, \quad |u| \le 1.$$

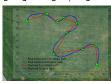


L. E. Dubins (1957) - American Journal of Mathematics

Dubins (Multi-Goal) Path

- Constant forward velocity v
- $q \in SE(2), (x, y) \in \mathbb{R}^2 \text{ and } \theta \in \mathbb{S}^1$





• Optimal path connecting $q_1 \in SE(2)$ and $q_2 \in SE(2)$ consists only of straight line arcs and arcs with the maximal curvature, i.e., two types of maneuvers CCC and CSC and the solution can be found analytically

The main difficulty is to determine the vehicle headings for a

- Part 1 Data Collection Planning Aerial Surveillance Missions

 - Dubins Traveling Salesman Problem
 - Dubins Traveling Salesman Problem with Neighborhoods
 - Dubins Orienteering Problem
 - Dubins Orienteering Problem with Neighborhoods
 - Planning in 3D Examples and Motivations
- Surveillance Missions
 - HW03b Motivation and Assignment

- Non-holonomic vehicle such as car-like or aircraft can be modeled
 - Constant forward velocity

 - Vehicle state is represented by a triplet $q = (x, y, \theta)$, where

described by the equation

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = v \begin{bmatrix} \cos \theta \\ \sin \theta \\ \frac{u}{\rho} \end{bmatrix}, \quad |u| \le 1$$

where u is the control input

E.g., for UAVs that usually operates in environment without obstacles

Planning with Dubins Vehicle – Summary

 \blacksquare Minimal turning radius ρ

■ State of the Dubins vehicle is $q = (x, y, \theta)$,

Smooth Dubins path connecting a sequence of locations is also

given sequence of waypoints

Sampling-based Solution of the DTP

■ For a closed sequence of the waypoint locations

We can sample possible heading values at each

possible Dubins maneuvers

 $P = (p_1, \ldots, p_n)$

location i into a discrete set of k headings, i.e., $\Theta^i = \{\theta^i_1, \dots, \theta^i_k\}$ and create a graph of all

Dubins Touring Problem - DTP

■ For a sequence of the *n* waypoint locations $P = (p_1, \dots p_n), p_i \in \mathbb{R}^2$, the Dubins Touring Problem (DTP) stands to determine the optimal headings $T = \{\theta_1, \dots, \theta_n\}$ at the waypoints q_i such that

minimize
$$_{T}$$
 $\mathcal{L}(T,P) = \sum_{i=1}^{n-1} \mathcal{L}(q_{i},q_{i+1}) + \mathcal{L}(q_{n},q_{1})$
subject to $q_{i} = (p_{i},\theta_{i}), \; \theta_{i} \in [0,2\pi), \; p_{i} \in P,$

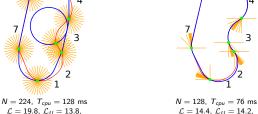
where $\mathcal{L}(q_i, q_i)$ is the length of the Dubins maneuver connecting q_i with q_i

- The DTP is a continuous optimization problem
- lacksquare The term $\mathcal{L}(q_n,q_1)$ is for possibly closed tour that can be for example requested in the TSP with Dubins vehicle, a.k.a. DTSP

On the other, the DTP can also be utilized for open paths such as solutions of the OP with Dubins vehicle

• In some cases, it may be suitable to relax the heading at the first/last locations in finding closed tours (i.e., solving DTSP)

- For a set of heading samples, the optimal solution can be found by a forward search of the graph in ings, and the complexity is $O(nk^2)$
- The key is to determined the most suitable heading samples per each waypoint



Informed sampling

 $\mathcal{L} = 19.8, \ \mathcal{L}_{II} = 13.8,$ N is the total number of samples, i.e., 32 samples per waypoint for

Uniform sampling

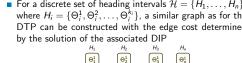
Example of Heading Sampling - Uniform vs. Informed

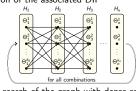
L is the length of the tour (blue) and \mathcal{L}_U is the lower bound (red) determined as a solution of the **Dubins Interval Problem (DIP)** B4M36UIR - Lecture 09: Data Collection with Dubins Vehicles

■ The arrival and departure angles may not be the same

Dubins Interval Problem (DIP)

- Dubins Interval Problem (DIP) is a generalization of Dubins maneuvers to the shortest path connecting two points p_i and p_i
- In the DIP, the leaving interval Θ_i at p_i and the arrival interval Θ_i at p_i are consider (not a single heading value)
- The optimal solution can be found analytically





■ The forward search of the graph with dense samples pro-

Manyam and Rathinam, 2015

Lower Bound of the DTP Lower Bound and Feasible Solution of the DTP

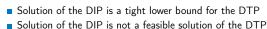
■ For a discrete set of heading intervals $\mathcal{H} = \{H_1, \dots, H_n\}$, where $H_i = \{\Theta_i^1, \Theta_i^2, \dots, \Theta_i^{k_i}\}$, a similar graph as for the DTP can be constructed with the edge cost determined

vides a tight lower bound of the DTP

Feasible path

■ DTP solution – use any particular heading of each interval in the

lower bound solution



RSR maneuver

Notice, for $\Theta_i = \Theta_i = \langle 0, 2\pi \rangle$ the optimal maneuver for DIP is a straight line segment

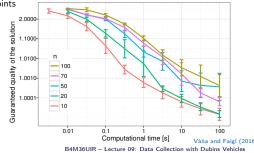
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Manyam et al. (2015)

Uniform vs Informed Sampling

The DIP-based Sampling of Headings in the DTP

- A similar forward search graph as for the DTP can be used for heading intervals instead of particular headings
- Using DIP for a sequence of waypoints is a lower bound of the DTP
- It can be used to inform how to splitting heading intervals
- The ratio between the lower bound and feasible solution of the DTP provides an estimation of the solution quality, e.g., for problems with nwaypoints

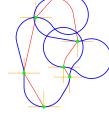


Informed Sampling of Headings in Solution of the DTP

- Iterative refinement of the heading intervals \mathcal{H} up to the angular resolution ϵ_{rea}
- The angular resolution is gradually decreased for the most promising intervals
- refineDTP divide the intervals of the lower bound solution
- solveDTP solve DTP using the heading from the refined intervals

- It simultaneously provides feasible and lower bound solutions of the DTP
- The first solution is provided very quickly any-time algorithm

 $\epsilon = 2\pi/4$, N = 28, $T_{CPU} = 8$ ms



 $\epsilon = 2\pi/4$, N = 21, $T_{CPU} = 8$ ms $\mathcal{L} = 29.9, \, \mathcal{L}_{IJ} = 13.2$

$\mathcal{L} = 27.9, \, \mathcal{L}_{II} = 13.2$

Dubins Traveling Salesman Problem (DTSP)

1. Determine a closed shortest Dubins path visit-

3. Headings $\Theta = \{\theta_{\sigma_1}, \theta_{\sigma_2}, \dots, \theta_{\sigma_n}\}$ for $p_{\sigma_i} \in P$

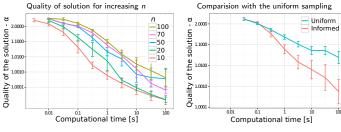
locations $P = \{p_1, \dots, p_n\}, p_i \in \mathbb{R}^2$

2. Permutation $\Sigma = (\sigma_1, \dots, \sigma_n)$ of visits

ing each location $p_i \in P$ of the given set of n

Results and Comparison with Uniform Sampling

- Random instances of the DTSP with a sequence of visits to the targets determined as a solution of the Euclidean TSP
- \blacksquare The waypoints placed in a squared bounding box with the side s= $(\rho\sqrt{n})/d$ for the $\rho=1$ and density d=0.5



- The Informed sampling-based approach provides solutions up to 0.01% from the optima
- A solution of the DTP is a fundamental bulding block for routing problems with

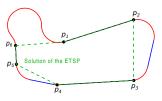
Decoupled Solution of the DTSP - Alternating Algorithm

Alternating Algorithm (AA) provides a solution of the DTSP for an even number of targets n Savla et al. (2005)

1. Solve the related Euclidean TSP

Relaxed motion constraints

- 2. Establish headings for even edges using straight line segments
- 3. Determine optimal maneuvers for odd edges using the analytical form for Dubins maneuvers



Courtesy of P. Váňa

- Let for each location $g_i \in G$ sample possible heading to k values, i.e., for each g_i the set of headings be $h_i = \{\theta_1^1, \dots, \theta_1^k\}$.
- $lue{}$ Since Σ is given, we can construct a graph connecting two consecutive locations in the sequence by all possible headings
- an optimal headings and thus, the optimal solution of the DTP.

DTSP is an optimization problem over all possible permutations Σ and **headings** Θ in the states $(q_{\sigma_1}, q_{\sigma_2}, \dots, q_{\sigma_n})$ such that $q_{\sigma_i} = (p_{\sigma_i}, \theta_{\sigma_i})$

minimize
$$\Sigma_{,\Theta}$$

$$\sum_{i=1}^{n-1} \mathcal{L}(q_{\sigma_i}, q_{\sigma_{i+1}}) + \mathcal{L}(q_{\sigma_n}, q_{\sigma_1}) \quad (1)$$
subject to $q_i = (p_i, \theta_i) \ i = 1, \dots, n,$ (2)

Sequencing part of the problem

where $\mathcal{L}(q_{\sigma_i}, q_{\sigma_i})$ is the length of Dubins path between q_{σ_i} and q_{σ_i}

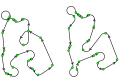
DTSP with the Given Sequence of the Visits to the Targets

- \blacksquare If the sequence of the visits Σ to the target locations is given
- the problem is to determine the optimal heading at each location
- and the problem becomes the Dubins Touring Problem (DTP) Váňa and Faigl (2016)
- For such a graph and particular headings $\{h_1, \ldots, h_n\}$, we can find

Challenges of the Dubins Traveling Salesman Problem

- The key difficulty of the DTSP is that the path length mutually depends on
- Order of the visits to the locations
 - Headings at the target locations

We need the sequence to determine headings, but headings may influence the sequence



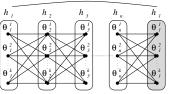
Two fundamental approaches can be found in literature

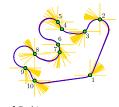
- Decoupled approach based on a given sequence of the locations
 - E.g., found by a solution of the Euclidean TSP
- Sampling-based approach with sampling of the headings at the locations into discrete sets of values and considering the problem as the variant of the Generalized TSP

Besides, further approaches are

- Genetic and memetic techniques (evolutionary algorithms)
- Unsupervised learning based approaches

DTSP as a Solution of the DTP





- The edge cost corresponds to the length of Dubins maneuver
- Better solution of the DTP can be found for more samples, which will also improve the DTSP but only for the given sequence

Two questions arise for a practical solution of the DTP

- How to sample the headings? Since more samples makes finding solution more demanding
- We need to sample the headings in a "smart" way, i.e., guided sampling using lower bound of the DTP
- What is the solution quality? Is there a tight lower bound?

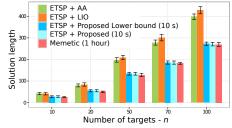
Yes, the lower bound can be computed as a solution of Dubins Interval Problem (DIP)

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DTP Solver in Solution of the DTSP

- The solution of the DTP can be used to solve DTSP for the given sequence of the waypoints
 - E.g., determined as a solution of the Euclidean TSP as in the Alternating Algorithm
- Comparision with the Alternating Algorithm (AA), Local Iterative Optimization (LIO), and Memetic algorithm AA - Savla et al., 2005, LIO - Váña & Faigl, 2015, Memetic - Zhang et al. 2014

ETSP + LIO



DTSP - Sampling-based Approach

■ Sampled heading values can be directly utilized to find the sequence as a solution of the Generalized Traveling Salesman Problem (GTSP)

Notice For Dubins vehicle, it is the Generalized Asymmetric TSP (GATSP)

The problem is to determine a shortest tour in a graph that visits all specified subsets of the graph's vertices

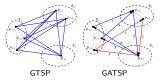
> The TSP is a special case of the GTSP when each subset to be visited consists just a single vertex

■ GATSP → ATSP

Noon and Bean (1991)

ATSP can be solved by LKH

■ ATSP → TSP, which can be solved optimally, e.g., by Concorde



Dubins Traveling Salesman Problem with Neighborhoods

- In surveillance planning, it may be required to visit a set of target regions $\boldsymbol{G} = \{R_1, \dots, R_n\}$ by the Dubins vehicle
- \blacksquare Then, for each target region R_i , we have to determine a particular point of the visit $p_i \in R_i$ and DTSP becomes the **Dubins Traveling** Salesman Problem with Neighborhoods (DTSPN)

In addition to Σ and headings Θ , waypoint locations P have to be determined

■ DTSPN is an optimization problem over all permutations Σ , headings $\Theta = \{\theta_{\sigma_1}, \dots, \theta_{\sigma_n}\}$ and points $P = (p_{\sigma_1}, \dots, p_{\sigma_n})$ for the states $(q_{\sigma_1}, \ldots, q_{\sigma_n})$ such that $q_{\sigma_i} = (p_{\sigma_i}, \theta_{\sigma_i})$ and $p_{\sigma_i} \in R_{\sigma_i}$:

minimize
$$_{\Sigma,\Theta,P}$$

$$\sum_{i=1}^{n-1} \mathcal{L}(q_{\sigma_i},q_{\sigma_{i+1}}) + \mathcal{L}(q_{\sigma_n},q_{\sigma_1})$$
 (3)

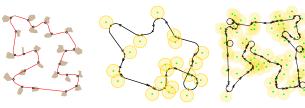
subject to
$$q_i = (p_i, \theta_i), p_i \in R_i \ i = 1, \dots, n$$
 (4)

lacksquare $\mathcal{L}(q_{\sigma_i},q_{\sigma_i})$ is the length of the shortest possible Dubins maneuver connecting the states q_{σ_i} and q_{σ_i}

DTSPN – Approches and Examples of Solution

- Similarly to the DTSP, also DTSPN can be addressed by
 - Decoupled approaches for which a sequence of visits to the regions can be found as a solution of the ETSP(N)
 - Sampling-based approaches and formulation as the GATSP ■ Clusters of sampled waypoint locations each with sampled possible

 - Soft-computing techniques such as memetic algorithms
 - Unsupervised learning techniques



Váňa and Faigl (IROS 2015), Faigl and Váňa (ICANN 2016, IJCNN 2017)

lan Faigl, 2017

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DTSPN

DOP

Dubins Orienteering Problem

■ In addition to S_k , k, Σ (OP) determine

headings $\Theta = (\theta_{\sigma_1}, \dots, \theta_{\sigma_k})$ such that

Curvature-constrained data collection path respecting Dubins vehicle model

with the minimal turning radius ρ and constant forward velocity v

The path is a sequence of waypoints $a_i \in SE(2)$, $a = (s, \theta)$, $\theta \in \mathbb{S}^1$

Variable Neighborhood Search (VNS)

DTSPN - Local Iterative Optimization (LIO)

normalized distance on the boundary of R_i

Algorithm 2: Local Iterative Optimization (LIO) for the DTSPN

Result: Waypoints $(q_{\sigma_1}, \dots, q_n)$, $q_i = (p_i, \theta_i)$, $p_i \in \delta R_i$

climbing technique

variable θ_i and α_i iteratively

while global solution is improving do for every $R_i \in G$ do

 $\theta_i := \text{optimizeHeadingLocally}(\theta_i)$ $\alpha_i := \text{optimizePositionLocally}(\alpha_i)$ $q_i := \text{checkLocalMinima}(\alpha_i, \theta_i);$

■ Instead of sampling into a discrete set of waypoint locations ech with

 \blacksquare A waypoint location p_i can be parametrized as a point on the bounday

■ The multi-variable optimization is treated independenly for each particular

// random assignment of $\alpha \in \delta R$:

of the respective region R_i , i.e., as a parameter $\alpha \in [0,1)$ measuring a

■ At each waypoint location p_i , the heading can be $\theta_i \in [0, 2\pi)$

Data: Input sequence of the goal regions $G = (R_{\sigma_1}, \dots, R_{\sigma_n})$, for the permutation Σ

sampled possible headings, we can perform local optimization, e.g., hill-

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Váňa and Faigl (IROS 2015)

Data Collection / Surveillance Planning with Travel Budget

- Visit the most important targets because of limited travel budget
- The problem can be formulated as the Orienteering Problem with Dubins vehicle, a.k.a. Dubins Orienteering Problem (DOP) Robert Pěnička, Jan Faigl, Petr Váňa and Martin Saska, RA-L 2017



maximize

subject to

The problem combines discrete combinatorial optimization (OP) with the continuous optimization for determining the vehicle headings

Variable Neighborhood Search (VNS) for the DOP

- The solution is the first k locations of the sequence of all target locations satisfying T_{max}
 - VNS for the OP Sevkli, Z. et al. (2006)
- It is an improving heuristics, i.e., an initial solution has to be provided A set of predefined neighborhoods are explored to find a better solution
- Shake explores the configuration space and Insert escape from a local minima using
 - Insert moves one random element
- Exchange exchanges two random elements
- Local Search optimizes the solution

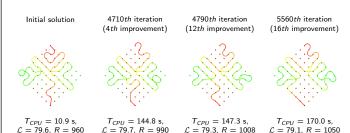
sub-sequences

- Path insert moves a random sub-sequence ■ Path exchange – exchanges two random
- **Randomized VNS** examines only n^2 changes in the *Local Search* procedure in each iteration

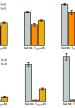
 $S_1 \rightarrow S_6 \rightarrow S_4 \rightarrow S_2 \rightarrow S_5 \rightarrow S_3 \rightarrow S_7 \rightarrow S_{10}$ Exchange Path insert



Evolution of the VNS Solution to the DOP







more computationally demanding

 $\mathcal{L} = 79.7, R = 990$

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- Variable Neighborhood Search (VNS) is a general metaheuristic for combinatorial optimization (routing problems) Hansen, P. and Mladenović, N. (2001): Variable neighborhood pplications. European Journal of Operational Research.
- The VNS is based on shake and local search procedures
 - Shake procedure aims to escape from local optima by changing the solution within the neighborhoods $N_{1,...,k_{max}}$

The neighborhoods are particular operators

■ Local search procedure searches fully specific neighborhoods of the solution using I_{max} predefined operators

Possible Solutions of the Dubins Orienteering Problem

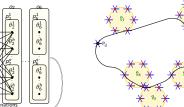
- 1. Solve the Euclidean OP (EOP) and then determine Dubins path The final path may exceed the budget and the vehicle can miss the locations because
- 2. Directly solve the Dubins Orienteering Problem (DOP), e.g.,
 - Sample possible heading values and use Variable Neighborhood Search (VNS)
 - Unsupervised learning based on Self-Organizing Maps (SOM)

Faigl. (WSOM+ 2017)

DTSPN - Decoupled Approach

1. Determine a sequence of visits to the n target regions as the solution of the ETSP

- 2. Sample possible waypoint locations and for each such a location sample possible heading values, e.g., s locations per each region and h heading per each location
- 3. Construct a search graph and determine a solution in $O(n(sh)^3)$
- 4. An example of the search graph for n = 6, s = 6, and h = 6





Variable Neighborhoods Search (VNS) for the DOPN

Dubins Orienteering Problem with Neighborhoods

- Curvature-constrained path respecting Dubins vehicle model
- Each waypoint consists of location $p \in \mathbb{R}^2$ and the heading $\theta \in \mathbb{S}^1$
- In addition to S_k , k, Σ determine locations

$$P_k = (p_{\sigma_1}, \dots, p_{\sigma_k})$$
 and headings $\Theta = (\theta_{\sigma_1}, \dots, \theta_{\sigma_k})$ such that

Comparision of the DOPN Solvers

SOM-based DOPN solver with h = 3

VNS-based



We need to solve the continuous optimization for determining the vehicle heading at each waypoint and the waypoint locations $P_k = \{p_{\sigma_1}, \dots, p_{\sigma_k}\}, p_{\sigma_i} \in \mathbb{R}^2$

■ VNS-based DOPN solver with s = 16 sampled waypoint locations per

 Aggregate results using average relative percentage error (ARPE) and relative percentage error (RPE) to the reference (best found) solution

ARPE

SOM-based (h = 3)

sensor and h = 16 heading samples per waypoint location

5.5

6.7 11.8

5,272.2 17.4

13 595 6

*The results have been obtained with a grid Xeon CPUs running at 2.2 GHz

1.4 13.650.1

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17.9

20.2

22.2 22.9

25.5

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: S - Set of the target locations : T_{max} - Maximal allowed budget o - Initial number of position waypoints for each target : m – Initial number of heading values for each

Algorithm 3: VNS based method for the DOPN

: r: - Local waypoint improvement ratio Imax - Maximal neighborhood number Output: P - Found data collecting path $S_r \leftarrow \text{getReachableLocations}(S, T_{max})$ $P \leftarrow \text{createInitialPath}(S_r, T_{max})$ while Stopping condition is not met do

while $l \le l_{max}$ do $P' \leftarrow \text{shake}(P, I)$ $P'' \leftarrow localSearch(P', I, r_i)$ if $\mathcal{L}_d(P'') \leq T_{max}$ and [R(P'') > R(P)] or [R(P'') == (P)] and $\mathcal{L}_d(P'') < \mathcal{L}_d(P)\mathcal{L}_d(P'')$]] then

The particular I for the individual operators of the shake procedure are:

- Waypoint Shake (/ = 1)
- Path Move (*l* = 2)
- Path Exchange (/ = 3)

The local search procedure consists of three operators and the particular I for the individual operators of the local search procedure are:

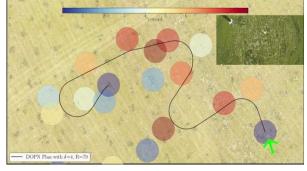
- Waypoint Improvement (*l* = 1)
- One Point Move (l=2)
- One Point Exchange (/ = 3)

Pěnička, R., Faigl, J., Saska, M., Váňa, P. (2017)

DOPN - Example of Solution and Practical Deployment

VNS-based solution of the DOPN

Robert Pěnička, Jan Faigl, Martin Saska and Petr Váña, ICUAS 2017



http://mrs.felk.cvut.cz/jint17dopr

	If altitude changes are too high, additional helix segments are insert
--	--

DTSPN in 3D

Problem set

Set 64. $\delta = 0.0$

Set 64 $\delta = 0.5$

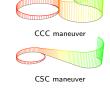
Set 66. $\delta = 0.0$

- Using the same principles as for the DTSPN in 2D, we can generalize the approaches for 3D planning using the Dubins Airplane model instead of simple Dubins vehicle
- The regions can be generalized to 3D and the problem can be addressed by decoupled or sampling-based approaches, i.e., using GATSP formulation
- In the case of LIO, we need a parametrization of the possible waypoint location, e.g.,











Solutions of the 3D-DTSPN

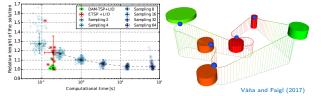


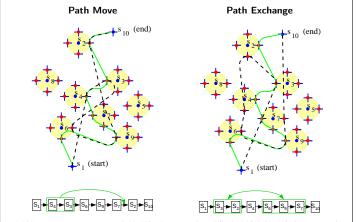
Algorithm 4: LIO-based Solver for 3D-DTSPN Data: Regions R Result: Solution represented by Q and Σ $\Sigma \leftarrow \text{getInitialSequence}(\mathcal{R});$ $Q \leftarrow getInitialSolution(\mathcal{R}, \Sigma);$ while terminal condition do $Q \leftarrow \mathsf{optimizeHeadings}(Q, \mathcal{R}, \Sigma);$ $Q \leftarrow \text{optimizeAlpha}(Q, \mathcal{R}, \Sigma)$ $Q \leftarrow \text{optimizeBeta}(Q, \mathcal{R}, \Sigma);$

return Q, Σ ;

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TSP+LIO), and sampling-based approach with transfor

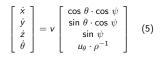




VNS for DOPN – Example of the Shake Operators

3D Data Collection Planning with Dubins Airplane Model

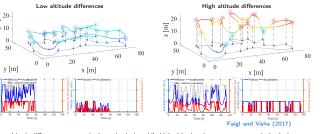
■ Dubins Airplane model describes the vehicle state $q=(p,\theta,\psi), p\in\mathbb{R}^3$ and $\theta,\psi\in\mathbb{S}^1$ as



- Constant forward velocity v, the minimal turning radius ρ , and limited pitch angle, i.e., $\psi \in [\psi_{min}, \psi_{max}]$
- \mathbf{u}_{θ} controls the vehicle heading, $|u_{\theta}| \leq 1$, and v is the forward velocity
- Generation of the 3D trajectory is based on the 2D Dubins maneuver

3D Surveillance Planning

- Parametrization of smooth 3D multi-goal trajectory as a sequence of Bézier curves
- Unsupervised learning for the TSPN can be generalized for such trajectories
- During the solution of the sequencing part of the problem, we can determine a velocity profile along the curve and compute the so-called Travel Time Estimation (TTE)
- Bézier curves better fit the limits of the multi-rotor UAVs that are limited by the maximal accelerations and velocities rather than minimal turning radius as for Dubins



■ Low altitude differences saturate horizontal velocity while high altitudes changes saturate vertical velocity



Solutions based on LIO (ETSP+LIO), TSP with the travel cost according to Dubins Airplane Model (DAM-

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Part II

Part 2 – Data Collection Planning for Surveillance Missions

■ There is a framework for testing and evaluation of UAVs control strategies developed and maintained by the winners of the Mohamed Bin Zayed International Robotics Challenge (MBZIRC) 2017

Multi-robot Systems (MRS) group

http://mrs.felk.cvut.cz



- The framework allows a direct evaluation of the planned trajectories, i.e., Dubins trajectories, in the same way for the simulator and also for real vehicles
- It provides an unique opportunity to become more familiar with multi-rotor unmanned aerial vehicles and gain experie with practical deployment of the planned trajectories to UAVs
- Full support of the evaluation environment is provided together with setuped computers at the dedicated computer lab of the MRS (KN:E-118)
- A practical deployment on real UAVs would be possible during the first campaigns in spring 2018

https://www.youtube.com/watch?v=ju3YbCtXpE



Up to additional 15 points can be gained for the implementation of the DTS and/or DTSPN, and execution of the trajectories in the MRS simulation framework

Goal: Solve data collection planning problem formulated as the DTSP (DT-

SPN) and deploy the planned path to the model of UAVs and eventually

- Implement a solution of the DTSP, e.g., one of the following methods
 - (2 points) for simple ETSP and Alternating Algorithm (AA), a.k.a ETSP+AA; (6 points) become familiar with the MRS simulation framework and deploy the planned trajectories within the simulator
- Voluntary implementation of the DTSP and DTSPN sampling-based solvers
 - (4 points) ETSP+DTP (forward search graph) or GATSP→ATSP and solution
 - (3 points) Extension of the DTSP to DTSPN, e.g., forward search graph for DTP generalized for the DTRP or GATSP based approach

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Summary of the Lecture

Topics Discussed

Topics Discussed

- Dubins vehicles and planning Dubins maneuvers
- Dubins Interval Problem (DIP)
- Dubins Touring Problem (DTP)
- Dubins Traveling Salesman Problem (DTSP) and Dubins Traveling Salesman with Neighborhoods (DTSPN)
 - Decoupled approaches Alternating Algorithm
 - Sampling-based approaches GATSP
- Dubins Orienteering Problem (OP) and Dubins Orienteering
- Data collection and surveillance planning in 3D

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- Problem with Neighborhoods (DOPN)
- Next: Multirobot Path Planning (MPP)