Data Collection Planning with Curvature-Constrained

Dubins Traveling Salesman Problem with Neighborhoods (DTSPN)

Dubins Orienteering Problem with Neighborhoods (DOPN)

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Lecture 08

B4M36UIR - Artificial Intelligence in Robotics

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■ Non-holonomic vehicle such as car-like or aircraft can be modeled

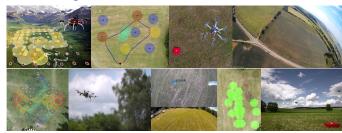
■ Vehicle state is represented by a triplet $q = (x, y, \theta)$, where

■ Position is $(x, y) \in \mathbb{R}^2$, vehicle heading is $\theta \in \mathbb{S}^2$, and thus

Dubins Vehicle and Dubins Planning

Motivation – Surveillance Missions with Aerial Vehicles

■ Provide curvature-constrained path to collect the most valuable measurements with shortest possible path/time or under limited travel budget



- Formulated as routing problems with Dubins vehicle
 - Dubins Traveling Salesman Problem with Neighborhoods
 - Dubins Orienteering Problem with Neighborhoods

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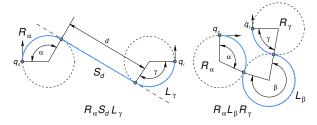
Parametrization of Dubins Maneuvers

■ Parametrization of each trajectory phase:

 $\{L_{\alpha}R_{\beta}L_{\gamma}, R_{\alpha}L_{\beta}R_{\gamma}, L_{\alpha}S_{d}L_{\gamma}, L_{\alpha}S_{d}R_{\gamma}, R_{\alpha}S_{d}L_{\gamma}, R_{\alpha}S_{d}R_{\gamma}\}$

for $\alpha \in [0, 2\pi), \beta \in (\pi, 2\pi), d \ge 0$

Notice the prescribed orientation at q0 and qf



Overview of the Lecture

- Part 1 Data Collection Planning Aerial Surveillance Missions
 - Dubins Vehicle and Dubins Planning
 - Dubins Touring Problem (DTP)
 - Dubins Traveling Salesman Problem
 - Dubins Traveling Salesman Problem with Neighborhoods
 - Dubins Orienteering Problem
 - Dubins Orienteering Problem with Neighborhoods
 - Planning in 3D Examples and Motivations
- Part 2 Bonus HW03b Data Collection Planning for Surveillance Missions
 - Task10 Bonus Motivation and Assignment

Dubins Vehicle

as the Dubins vehicle

The vehicle motion can be

described by the equation

where u is the control input

■ Constant forward velocity

Limited minimal turning radius ρ

Optimal Maneuvers for Dubins Vehicle

■ For two states $q_1 \in SE(2)$ and $q_2 \in SE(2)$ in the environment without obstacles $\mathcal{W} = \mathbb{R}^2$, the optimal path connecting q_1 with g₂ can be characterized as one of two main types

Part I

Part 1 - Data Collection Planning - Aerial

Surveillance Missions

- CCC type: LRL, RLR;
- CSC type: LSL, LSR, RSL, RSR;

where S - straight line arc, C - circular arc oriented to left (L) or right (R) L. E. Dubins (1957) - American Journal of Mathematics

- The optimal paths are called **Dubins maneuvers**:
 - Constant velocity: v(t) = v and turning radius ρ
 - **Six** types of trajectories connecting any configuration in SE(2)

 \blacksquare The control u is according to C and S type one of three possible values $u \in \{-1, 0, 1\}$

Planning with Dubins Vehicle – Summary

- The optimal path connecting two configurations can be found analytically E.g., for UAVs that usually operates in environment without obstacles
- The Dubins maneuvers can also be used in randomized-sampling based motion planners, such as RRT, in the control based sampling
- Dubins vehicle model can be considered in the multi-goal path planning
 - Surveillance, inspection or monitoring missions to periodically visits given target locations (areas)
- Dubins Touring Problem(DTP)

Given a sequence of locations, what is the shortest path visting the locations, i.e., what are the headings of the vehicle at the locations

Dubins Traveling Salesman Problem (DTSP)

Given a set of locations, what is the shortest Dubins path that visits each location exactly once and returns to the origin location

■ Dubins Orienteering Problem (DOP)

Given a set of locations, each with associated reward, what is the Dubins path visiting the most rewarding locations and not exceeding the given travel budget

Dubins (Multi-Goal) Path

- \blacksquare Minimal turning radius ρ
- Constant forward velocity v
- State of the Dubins vehicle is $q = (x, y, \theta)$, $q \in SE(2), (x, y) \in \mathbb{R}^2 \text{ and } \theta \in \mathbb{S}^1$







Smooth Dubins path connecting a sequence of locations is also

• Optimal path connecting $q_1 \in SE(2)$ and $q_2 \in SE(2)$ consists only of straight line arcs and arcs with the maximal curvature, i.e., two types of maneuvers CCC and CSC and the solution can be found analytically

The main difficulty is to determine the vehicle headings for a given sequence of waypoints

Sampling-based Solution of the DTP

■ For a closed sequence of the waypoint locations

 $P = (p_1, \ldots, p_n)$

 $\Theta^i = \{\theta^i_1, \dots, \theta^i_k\}$ and create a graph of all

possible Dubins maneuvers

Dubins Touring Problem - DTP

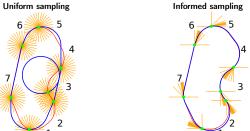
■ For a sequence of the *n* waypoint locations $P = (p_1, \dots p_n), p_i \in \mathbb{R}^2$, the Dubins Touring Problem (DTP) stands to determine the optimal headings $T = \{\theta_1, \dots, \theta_n\}$ at the waypoints q_i such that

minimize
$$_T$$
 $\mathcal{L}(T,P) = \sum_{i=1}^{n-1} \mathcal{L}(q_i,q_{i+1}) + \mathcal{L}(q_n,q_1)$ subject to $q_i = (p_i,\theta_i), \; \theta_i \in [0,2\pi), \; p_i \in P,$

- lacksquare The term $\mathcal{L}(q_n,q_1)$ is for possibly closed tour that can be for example requested in the TSP with Dubins vehicle, a.k.a. DTSP

in finding closed tours (i.e., solving DTSP)

- For a set of heading samples, the optimal solution can be found by a forward search of the graph in ings, and the complexity is $O(nk^2)$
- The key is to determined the most suitable heading samples per each waypoint



N = 224, $T_{cpu} = 128$ ms $\mathcal{L} = 19.8, \ \mathcal{L}_{II} = 13.8,$

 $\mathcal{L} = 14.4, \ \mathcal{L}_{II} = 14.2,$

N is the total number of samples, i.e., 32 samples per waypoint for

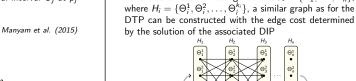
Example of Heading Sampling - Uniform vs. Informed

L is the length of the tour (blue) and \mathcal{L}_U is the lower bound (red) determined as a solution of the **Dubins Interval Problem (DIP)**

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Dubins Interval Problem (DIP)

- Dubins Interval Problem (DIP) is a generalization of Dubins maneuvers to the shortest path connecting two points p_i and p_i
- In the DIP, the leaving interval Θ_i at p_i and the arrival interval Θ_i at p_i are consider (not a single heading value)
- The optimal solution can be found analytically





- Solution of the DIP is a tight lower bound for the DTP
- Solution of the DIP is not a feasible solution of the DTP

Notice, for $\Theta_i = \Theta_i = \langle 0, 2\pi \rangle$ the optimal maneuver for DIP is a straight line segment

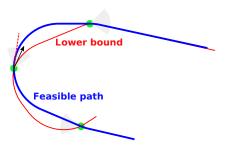
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vides a tight lower bound of the DTP

Manyam and Rathinam, 2015

Lower Bound and Feasible Solution of the DTP

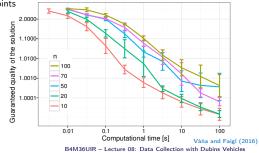
■ The arrival and departure angles may not be the same



■ DTP solution – use any particular heading of each interval in the lower bound solution

The DIP-based Sampling of Headings in the DTP

- A similar forward search graph as for the DTP can be used for heading intervals instead of particular headings
- Using DIP for a sequence of waypoints is a lower bound of the DTP
- It can be used to inform how to splitting heading intervals
- The ratio between the lower bound and feasible solution of the DTP provides an estimation of the solution quality, e.g., for problems with nwaypoints

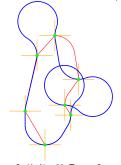


Informed Sampling of Headings in Solution of the DTP

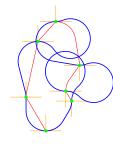
- Iterative refinement of the heading intervals \mathcal{H} up to the angular resolution ϵ_{rea}
- creased for the most promising intervals
- lower bound solution
- from the refined intervals

- It simultaneously provides feasible and lower bound solutions of the DTP
- The first solution is provided very quickly any-time algorithm

Uniform vs Informed Sampling



 $\epsilon=2\pi/4$, N=28, $T_{CPU}=8$ ms



 $\epsilon = 2\pi/4$, N = 21, $T_{CPU} = 8$ ms $\mathcal{L} = 29.9, \, \mathcal{L}_{IJ} = 13.2$

 $\mathcal{L} = 27.9, \, \mathcal{L}_{II} = 13.2$

We can sample possible heading values at each location i into a discrete set of k headings, i.e.,

minimize
$$_{T}$$
 $\mathcal{L}(T,P) = \sum_{i=1}^{n-1} \mathcal{L}(q_{i},q_{i+1}) + \mathcal{L}(q_{n},q_{1})$

where $\mathcal{L}(q_i, q_i)$ is the length of the Dubins maneuver connecting q_i with q_i

- The DTP is a continuous optimization problem

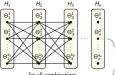
On the other, the DTP can also be utilized for open paths such as solutions of the OP with Dubins vehicle

In some cases, it may be suitable to relax the heading at the first/last locations

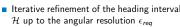
Lower Bound of the DTP

■ For a discrete set of heading intervals $\mathcal{H} = \{H_1, \dots, H_n\}$,

DTP can be constructed with the edge cost determined by the solution of the associated DIP



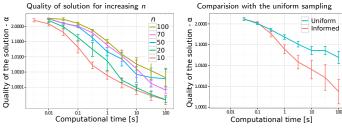
■ The forward search of the graph with dense samples pro-



- The angular resolution is gradually de-
- refineDTP divide the intervals of the
- solveDTP solve DTP using the heading

Results and Comparison with Uniform Sampling

- Random instances of the DTSP with a sequence of visits to the targets determined as a solution of the Euclidean TSP
- \blacksquare The waypoints placed in a squared bounding box with the side s= $(\rho\sqrt{n})/d$ for the $\rho=1$ and density d=0.5



- The Informed sampling-based approach provides solutions up to 0.01% from the optima
- A solution of the DTP is a fundamental bulding block for routing problems with

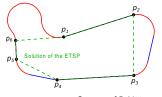
Decoupled Solution of the DTSP - Alternating Algorithm

Alternating Algorithm (AA) provides a solution of the DTSP for an even number of targets n Savla et al. (2005)

1. Solve the related Euclidean TSP

Relaxed motion constraints

- 2. Establish headings for even edges using straight line segments
- 3. Determine optimal maneuvers for odd edges using the analytical form for Dubins maneuvers

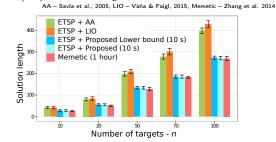


DTP Solver in Solution of the DTSP

■ The solution of the DTP can be used to solve DTSP for the given sequence of the waypoints

E.g., determined as a solution of the Euclidean TSP as in the Alternating Algorithm

Comparision with the Alternating Algorithm (AA), Local Iterative Optimization (LIO), and Memetic algorithm



Dubins Traveling Salesman Problem (DTSP)

- 1. Determine a closed shortest Dubins path visiting each location $p_i \in P$ of the given set of nlocations $P = \{p_1, \dots, p_n\}, p_i \in \mathbb{R}^2$
- 2. Permutation $\Sigma = (\sigma_1, \dots, \sigma_n)$ of visits Sequencing part of the problem
- 3. Headings $\Theta = \{\theta_{\sigma_1}, \theta_{\sigma_2}, \dots, \theta_{\sigma_n}\}$ for $p_{\sigma_i} \in P$
- **DTSP** is an optimization problem over all possible permutations Σ and **headings** Θ in the states $(q_{\sigma_1}, q_{\sigma_2}, \dots, q_{\sigma_n})$ such that $q_{\sigma_i} = (p_{\sigma_i}, \theta_{\sigma_i})$

$$\begin{array}{ll} \textit{minimize}_{\Sigma,\Theta} & \sum_{i=1}^{n-1} \mathcal{L}(q_{\sigma_i}, q_{\sigma_{i+1}}) + \mathcal{L}(q_{\sigma_n}, q_{\sigma_1}) & (1) \\ \textit{subject to} & q_i = (p_i, \theta_i) \ i = 1, \dots, n, \end{array}$$

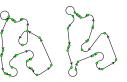
where $\mathcal{L}(q_{\sigma_i}, q_{\sigma_i})$ is the length of Dubins path between q_{σ_i} and q_{σ_i}

- \blacksquare If the sequence of the visits Σ to the target locations is given
- the problem is to determine the optimal heading at each location
- and the problem becomes the Dubins Touring Problem (DTP)
- Let for each location $g_i \in G$ sample possible heading to k values, i.e., for each g_i the set of headings be $h_i = \{\theta_1^1, \dots, \theta_1^k\}$.
- $lue{}$ Since Σ is given, we can construct a graph connecting two consecutive locations in the sequence by all possible headings
- For such a graph and particular headings $\{h_1, \ldots, h_n\}$, we can find

Challenges of the Dubins Traveling Salesman Problem

- The key difficulty of the DTSP is that the path length mutually depends on
- Order of the visits to the locations
 - Headings at the target locations

We need the sequence to determine headings, but headings may influence the sequence



Two fundamental approaches can be found in literature

■ Decoupled approach based on a given sequence of the locations

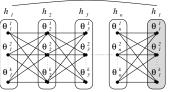
E.g., found by a solution of the Euclidean TSP

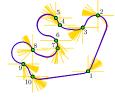
■ Sampling-based approach with sampling of the headings at the locations into discrete sets of values and considering the problem as the variant of the Generalized TSP

Besides, further approaches are

- Genetic and memetic techniques (evolutionary algorithms)
- Unsupervised learning based approaches

DTSP as a Solution of the DTP





- The edge cost corresponds to the length of Dubins maneuver
- Better solution of the DTP can be found for more samples, which will also improve the DTSP but only for the given sequence

Two questions arise for a practical solution of the DTP

■ How to sample the headings? Since more samples makes finding solution more demanding

We need to sample the headings in a "smart" way, i.e., guided sampling using lower bound of the DTP

■ What is the solution quality? Is there a tight lower bound?

Yes, the lower bound can be computed as a solution of Dubins Interval Problem (DIP)

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Dubins Traveling Salesman Problem with Neighborhoods

- In surveillance planning, it may be required to visit a set of target regions $\boldsymbol{G} = \{R_1, \dots, R_n\}$ by the Dubins vehicle
- \blacksquare Then, for each target region R_i , we have to determine a particular point of the visit $p_i \in R_i$ and DTSP becomes the **Dubins Traveling** Salesman Problem with Neighborhoods (DTSPN)

In addition to Σ and headings Θ , waypoint locations P have to be determined

■ DTSPN is an optimization problem over all permutations Σ , headings $\Theta = \{\theta_{\sigma_1}, \dots, \theta_{\sigma_n}\}$ and points $P = (p_{\sigma_1}, \dots, p_{\sigma_n})$ for the states $(q_{\sigma_1}, \ldots, q_{\sigma_n})$ such that $q_{\sigma_i} = (p_{\sigma_i}, \theta_{\sigma_i})$ and $p_{\sigma_i} \in R_{\sigma_i}$:

minimize
$$_{\Sigma,\Theta,P}$$

$$\sum_{i=1}^{n-1} \mathcal{L}(q_{\sigma_i}, q_{\sigma_{i+1}}) + \mathcal{L}(q_{\sigma_n}, q_{\sigma_1})$$
(3
subject to $q_i = (p_i, \theta_i), p_i \in R_i \ i = 1, \dots, n$ (4

lacksquare $\mathcal{L}(q_{\sigma_i},q_{\sigma_i})$ is the length of the shortest possible Dubins maneuver connecting the states q_{σ_i} and q_{σ_i}

DTSP - Sampling-based Approach

■ Sampled heading values can be directly utilized to find the sequence as a solution of the Generalized Traveling Salesman Problem (GTSP)

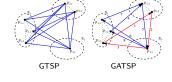
Notice For Dubins vehicle, it is the Generalized Asymmetric TSP (GATSP)

The problem is to determine a shortest tour in a graph that visits all specified subsets of the graph's vertices

Noon and Bean (1991)

ATSP can be solved by LKH

■ ATSP → TSP, which can be solved optimally, e.g., by Concorde



DTSP with the Given Sequence of the Visits to the Targets

Váňa and Faigl (2016)

an optimal headings and thus, the optimal solution of the DTP.

Courtesy of P. Váňa

The TSP is a special case of the GTSP when each subset to be visited consists just a single vertex

■ GATSP → ATSP

1. Determine a sequence of visits to the n target regions as the solution of the ETSP

heading values, e.g., s locations per each region and h heading per each location

2. Sample possible waypoint locations and for each such a location sample possible

3. Construct a search graph and determine a solution in $O(n(sh)^3)$

4. An example of the search graph for n = 6, s = 6, and h = 6

DTSPN – Approches and Examples of Solution

- Similarly to the DTSP, also DTSPN can be addressed by
 - Decoupled approaches for which a sequence of visits to the regions can be found as a solution of the ETSP(N)
 - Sampling-based approaches and formulation as the GATSP ■ Clusters of sampled waypoint locations each with sampled possible
 - **Soft-computing** techniques such as memetic algorithms
 - Unsupervised learning techniques

Váña and Faigl (IROS 2015), Faigl and Váña (ICANN 2016, IJCNN 2017)

■ Similarly to the lower bound of the DTSP based on the **Dubins** Interval Problem (DIP) a lower bound for the DTSPN can be computed using Generalized DIP (GDIP)





■ In the DTSPN, we need to determined not only the headings, but the

■ Dubins Interval Problem is not sufficient to provide tight lower-bound

Lower Bound for the DTSP with Neighborhoods

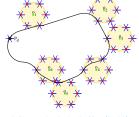
Generalized Dubins Interval Problem

waypoint locations themselves



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DTSPN - Decoupled Approach



Generalized Dubins Interval Problem (GDIP) and its Optimal Solution

■ Determine the shortest Dubins maneuver connecting P_i and P_i given the angle intervals $\theta_i \in [\theta_i^{min}, \theta_i^{max}]$ and $\theta_i \in [\theta_i^{min}, \theta_i^{max}]$







■ Optimal solution – Closed-form expressions for (1–6) and convex optimization (7)

| 1) S type | | | | | | |
|-------------|--|--|--|--|--|--|
| F1 2 Q 13 | | | | | | |
| 4) CSC type | | | | | | |







■ Váňa and Faigl: Optimal Solution of the Generalized Dubins Interval Problem, RSS 2018, best student pape

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DTSPN - Local Iterative Optimization (LIO)

- Instead of sampling into a discrete set of waypoint locations ech with sampled possible headings, we can perform local optimization, e.g., hillclimbing technique
- At each waypoint location p_i , the heading can be $\theta_i \in [0, 2\pi)$
- \blacksquare A waypoint location p_i can be parametrized as a point on the bounday of the respective region R_i , i.e., as a parameter $\alpha \in [0,1)$ measuring a normalized distance on the boundary of R_i
- The multi-variable optimization is treated independenly for each particular variable θ_i and α_i iteratively

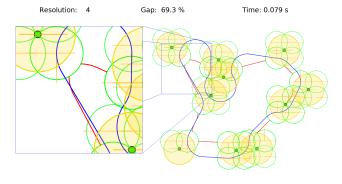
Algorithm 2: Local Iterative Optimization (LIO) for the DTSPN Data: Input sequence of the goal regions $G = (R_{\sigma_1}, \dots, R_{\sigma_n})$, for the permutation Σ Result: Waypoints $(q_{\sigma_1}, \dots, q_n)$, $q_i = (p_i, \theta_i)$, $p_i \in \delta R_i$ // random assignment of $q_i \in \delta R_i$; while global solution is improving do for every $R_i \in G$ do $\theta_i := \text{optimizeHeadingLocally}(\theta_i)$ $\alpha_i := \text{optimizePositionLocally}(\alpha_i)$ $q_i := \text{checkLocalMinima}(\alpha_i, \theta_i);$ Váňa and Faigl (IROS 2015)

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Time: 1.292 s

GDIP-based Informed Sampling for the DTSPN

Iterative refinement of the neighborhood samples and heading samples



GDIP-based Informed Sampling for the DTSPN

DTSPN similarly as the DIP for the DTSP

■ Iterative refinement of the neighborhood samples and heading samples

■ Generalized Dubins Interval Problem (GDIP) can be utilized for the

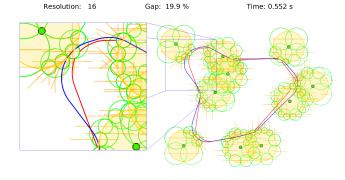
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■ Váňa and Faigl: Optimal Solution of the Generalized Dubins Interval Problem, RSS 2018, best student pape

Gap: 39.4 % Resolution: 8 Time: 0.211 s

GDIP-based Informed Sampling for the DTSPN

Iterative refinement of the neighborhood samples and heading samples



GDIP-based Informed Sampling for the DTSPN

Resolution: 32

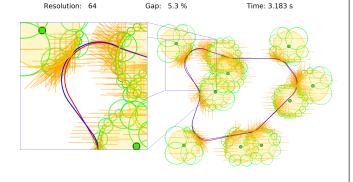
■ Iterative refinement of the neighborhood samples and heading samples Gap: 10.7 %

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GDIP-based Informed Sampling for the DTSPN

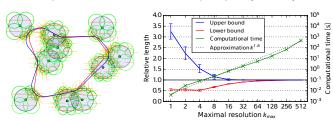
■ Iterative refinement of the neighborhood samples and heading samples



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DTSPN - Convergence to the Optimal Solution

■ For a given sequence of visits to the target regions (locations)



- The algorithm scales linearly with the number of locations
- Complexity of the algorithm is approximately $\mathcal{O}(nk^{1.8})$

https://github.com/comrob/gdip

Váña and Faigl: Optimal Solution of the Generalized Dubins Interval Problem. RSS 2018, best student pape

Variable Neighborhood Search (VNS)

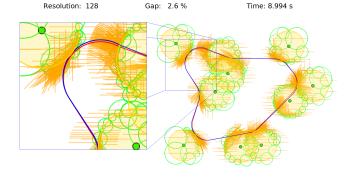
- Variable Neighborhood Search (VNS) is a general metaheuristic for combinatorial optimization (routing problems) Hansen, P. and Mladenović, N. (2001): Variable neighborhood search: Principles and
- The VNS is based on shake and local search procedures
 - Shake procedure aims to escape from local optima by changing the solution within the neighborhoods $N_{1,...,k_{max}}$

The neighborhoods are particular operators

■ Local search procedure searches fully specific neighborhoods of the solution using I_{max} predefined operators

GDIP-based Informed Sampling for the DTSPN

Iterative refinement of the neighborhood samples and heading samples



Data Collection / Surveillance Planning with Travel Budget

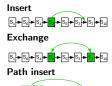
- Visit the most important targets because of limited travel budget
- The problem can be formulated as the Orienteering Problem with Dubins vehicle, a.k.a. Dubins Orienteering Problem (DOP)

Variable Neighborhood Search (VNS) for the DOP

■ The solution is the first k locations of the sequence of all target locations satisfying T_{max}

VNS for the OP - Sevkli, Z. et al. (2006)

- It is an improving heuristics, i.e., an initial solution has to be provided
- A set of predefined neighborhoods are explored to find a better solution
- Shake explores the configuration space and
- escape from a local minima using ■ Insert - moves one random element
- Exchange exchanges two random elements
- Local Search optimizes the solution
 - Path insert moves a random sub-sequence ■ Path exchange – exchanges two random sub-sequences
- **Randomized VNS** examines only n^2 changes in the Local Search procedure in each iteration

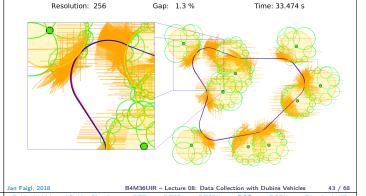


 $S_1 \rightarrow S_3 \rightarrow S_4 \rightarrow S_7 \rightarrow S_2 \rightarrow S_{10}$

Path exchange

GDIP-based Informed Sampling for the DTSPN

■ Iterative refinement of the neighborhood samples and heading samples

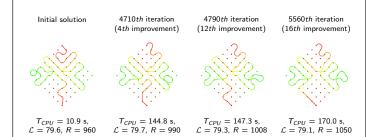


Dubins Orienteering Problem

- Curvature-constrained data collection path respecting Dubins vehicle model with the minimal turning radius ρ and constant forward velocity v
- The path is a sequence of waypoints $q_i \in SE(2)$, $q = (s, \theta)$, $\theta \in \mathbb{S}^1$.
- In addition to S_k , k, Σ (OP) determine headings $\Theta = (\theta_{\sigma_1}, \dots, \theta_{\sigma_k})$ such that subject to

The problem combines discrete combinatorial optimization (OP) with the continuous optimization for determining the vehicle headings

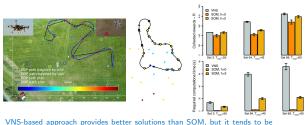
Evolution of the VNS Solution to the DOP



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Possible Solutions of the Dubins Orienteering Problem

- 1. Solve the Euclidean OP (EOP) and then determine Dubins path The final path may exceed the budget and the vehicle can miss the locations because
- 2. Directly solve the Dubins Orienteering Problem (DOP), e.g.,
 - Sample possible heading values and use Variable Neighborhood Search (VNS) Pěnička, Faigl, Váňa, Saska (RA-L 2017)
 - Unsupervised learning based on Self-Organizing Maps (SOM)



more computationally demanding

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Dubins Orienteering Problem with Neighborhoods

- Curvature-constrained path respecting Dubins vehicle model
- Each waypoint consists of location $p \in \mathbb{R}^2$ and the heading $\theta \in \mathbb{S}^1$
- In addition to S_k , k, Σ determine locations

 $P_k = (p_{\sigma_1}, \dots, p_{\sigma_k})$ and headings $\Theta = (\theta_{\sigma_1}, \dots, \theta_{\sigma_k})$ such that

Comparision of the DOPN Solvers

■ SOM-based DOPN solver with h = 3

VNS-based

 $\max_{k,S_k,\Sigma}$

subject to

 $q_{\sigma_i}^{i=2} = (p_{\sigma_i}, \theta_{\sigma_i}), p_{\sigma_i} \in \mathbb{R}^2, \theta_{\sigma_i} \in S^1$ $||p_{\sigma_i}, s_{\sigma_i}|| \leq \delta, s_{\sigma_i} \in S_i$ $p_{\sigma_1} = s_1, p_{\sigma_k} = s_r$

We need to solve the continuous optimization for determining the vehicle heading at each waypoint and the waypoint locations $P_k = \{p_{\sigma_1}, \dots, p_{\sigma_k}\}, p_{\sigma_i} \in \mathbb{R}^2$

■ VNS-based DOPN solver with s = 16 sampled waypoint locations per

 Aggregate results using average relative percentage error (ARPE) and relative percentage error (RPE) to the reference (best found) solution

RPE ARPE

SOM-based (h = 3)

sensor and h = 16 heading samples per waypoint location

: S - Set of the target locations Tmax - Maximal allowed budget o - Initial number of position waypoints for each target

Input : m - Initial number of heading values for each r: - Local waynoint improvement ratio Imax - Maximal neighborhood number Output: P - Found data collecting path $S_r \leftarrow \text{getReachableLocations}(S, T_{max})$ $P \leftarrow \text{createInitialPath}(S_r, T_{max})$ while Stopping condition is not met do while $l \le l_{max}$ do $P' \leftarrow \text{shake}(P, I)$ $P'' \leftarrow localSearch(P', I, r_i)$ if $\mathcal{L}_d(P'') \le T_{max}$ and [[R(P'') > R(P)] or [R(P'') = (P)] and $\mathcal{L}_d(P'') < \mathcal{L}_d(P)\mathcal{L}_d(P'')$]] then

| *I* ← *I* + 1

an Faigl, 2018

Algorithm 3: VNS based method for the DOPN

The particular I for the individual operators of the shake procedure are:

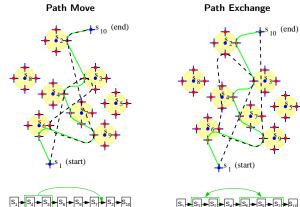
- Waypoint Shake (/ = 1)
- Path Move (*l* = 2)
- Path Exchange (/ = 3)

The local search procedure consists of three operators and the particular I for the individual operators of the local search procedure are:

- Waypoint Improvement (*l* = 1)
- One Point Move (I=2)
- One Point Exchange (/ = 3)

Pěnička, R., Faigl, J., Saska, M., Váňa, P. (2017)

VNS for DOPN - Example of the Shake Operators



| an | Faigl, | 2018 | | B4M |
|----|--------|------|--|-----|

6.546.6 1.4 13.650.1

*The results have been obtained with a grid Xeon CPUs running at 2.2 GHz

11.8

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8.3 17.9 20.2 22.2 22.9

25.5

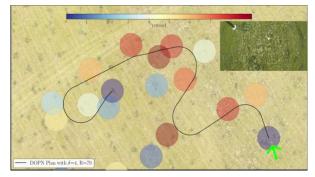
DOPN - Example of Solution and Practical Deployment

Variable Neighborhoods Search (VNS) for the DOPN

VNS-based solution of the DOPN

Robert Pěnička, Jan Faigl, Martin Saska and Petr Váňa, ICUAS 2017

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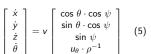


http://mrs.felk.cvut.cz/jint17dops

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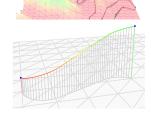
3D Data Collection Planning with Dubins Airplane Model

■ Dubins Airplane model describes the vehicle state $q=(p,\theta,\psi), p\in\mathbb{R}^3$ and $heta, \psi \in \mathbb{S}^1$ as



Chitsaz, H., LaValle, S.M. (2017)

Constant forward velocity v, the minimal turning radius ρ , and limited pitch angle, i.e., $\psi \in [\psi_{min}, \psi_{max}]$



- \mathbf{u}_{θ} controls the vehicle heading, $|u_{\theta}| \leq 1$, and v is the forward velocity
- Generation of the 3D trajectory is based on the 2D Dubins maneuver
- If altitude changes are too high, additional helix segments are inserted

DTSPN in 3D

Problem set

- Using the same principles as for the DTSPN in 2D, we can generalize the approaches for 3D planning using the Dubins Airplane model instead of simple Dubins vehicle
- The regions can be generalized to 3D and the problem can be addressed by decoupled or sampling-based approaches, i.e., using GATSP formulation
- In the case of LIO, we need a parametrization of the possible waypoint location, e.g.,





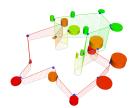






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Solutions of the 3D-DTSPN



Data: Regions R Result: Solution represented by Q and Σ $\Sigma \leftarrow \text{getInitialSequence}(\mathcal{R});$ $Q \leftarrow getInitialSolution(\mathcal{R}, \Sigma);$ while terminal condition do $Q \leftarrow \mathsf{optimizeHeadings}(Q, \mathcal{R}, \Sigma)$; $Q \leftarrow \text{optimizeAlpha}(Q, \mathcal{R}, \Sigma);$

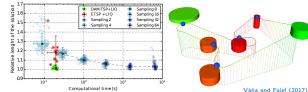
Algorithm 4: LIO-based Solver for 3D-DTSPN

 $Q \leftarrow \text{optimizeBeta}(Q, \mathcal{R}, \Sigma);$

return Q, Σ ;

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Solutions based on LIO (ETSP+LIO), TSP with the travel cost according to Dubins Airplane Model (DAM-TSP+LIO), and sampling-based approach with transformation of the GTSP to the ATSP solved by LKH



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3D Surveillance Planning Motivation ■ Parametrization of smooth 3D multi-goal trajectory as a sequence of Bézier curves Unsupervised learning for the TSPN can be generalized for such trajectories ■ There is a framework for testing and eval-■ During the solution of the sequencing part of the problem, we can determine a velocity uation of UAVs control strategies develprofile along the curve and compute the so-called Travel Time Estimation (TTE) oped and maintained by the winners of the Part II ■ Bézier curves better fit the limits of the multi-rotor UAVs that are limited by the Mohamed Bin Zaved International Robotics maximal accelerations and velocities rather than minimal turning radius as for Dubins Challenge (MBZIRC) 2017 Part 2 - Data Collection Planning for Multi-robot Systems (MRS) group http://mrs.felk.cvut.cz Surveillance Missions jectories, i.e., Dubins trajectories, in the same way for the simulator and also for real vehicles with practical deployment of the planned trai Full support of the evaluation environment is provided together with setuped computers at the dedicated computer lab of the MRS (KN:E-118) A practical deployment on real UAVs would be possible during the first campaigns in spring 2018 https://www.youtube.com/watch?v=ju3YbCtXpEw ■ Low altitude differences saturate horizontal velocity while high altitudes changes saturate vertical velocity B4M36UIR - Lecture 08: Data Collection with Dubins Vehicles B4M36UIR - Lecture 08: Data Collection with Dubins Vehicles Task10 Bonus - Motivation and Assignmen Topics Discusse Assignment – Task10 Bonus Topics Discussed Topic: Data Collection Planning for Surveillance Missions ■ Dubins vehicles and planning – Dubins maneuvers Goal: Solve data collection planning problem formulated as the DTSP Dubins Interval Problem (DIP) (DTSPN) and deploy the planned path to the model of UAVs and ■ Dubins Touring Problem (DTP) eventually experimentally verify the paths using real UAV Summary of the Lecture ■ Dubins Traveling Salesman Problem (DTSP) and Dubins Assignment: https://cw.fel.cvut.cz/wiki/courses/b4m36uir/hw/task10bonus Traveling Salesman with Neighborhoods (DTSPN) Up to additional 5 points can be gained for the implementation of the DTS and/or ■ Decoupled approaches – Alternating Algorithm DTSPN, and execution of the trajectories in the MRS simulation framework ■ Sampling-based approaches - GATSP ■ Implement a solution of the DTSP(N), e.g., one of the following methods ■ Dubins Orienteering Problem (OP) and Dubins Orienteering (1 points) for simple ETSP and Alternating Algorithm (AA), a.k.a ETSP+AA; Problem with Neighborhoods (DOPN) (4 points) become familiar with the MRS simulation framework and deploy the ■ Data collection and surveillance planning in 3D planned trajectories within the simulator Additional implementation of the DTSPN sampling-based solver ■ (5 points) Employ a solution of the Generalized Dubins Interval Problem (GDIP) ■ Next: Multirobot Path Planning (MPP) in sampling-based solution of the DTSPN and determining the lower bound of the DTSPN for a particular sequence of visits (e.g., using solution of the ETSP) Jan Faigl, 2018 B4M36UIR - Lecture 08: Data Collection with Dubins Vehicles B4M36UIR - Lecture 08: Data Collection with Dubins Vehicles B4M36UIR - Lecture 08: Data Collection with Dubins Vehicles