Data collection planning - TSP(N), PC-TSP(N), and OP(N))

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Lecture 07

B4M36UIR - Artificial Intelligence in Robotics

Part I

Part 1 – Data Collection Planning

(1)

PC-TSPN – Optimization Criterion

 $p_i \in \mathbb{R}^2$, at which data readings are performed

PC-TSPN includes other variants of the TSP

• for $\xi(s_i) = 0$ and $\delta \ge 0$ it is the TSPN

• for $\xi(s_i) = 0$ and $\delta = 0$ it is the ordinary TSP

• for $\delta = 0$ it is the PC-TSP

The PC-TSPN is a problem to

C(T) of T is minimal

■ Determine a set of unique locations $P = \{p_1, \dots, p_k\}, k < n$,

■ Find a cost efficient tour T visiting P such that the total cost

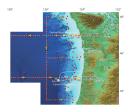
 $C(T) = \sum_{(p_l, p_{l+1}) \in T} c(p_{l_i}, p_{l_{i+1}}) + \sum_{s \in S \setminus S_T} \xi(s),$

where $S_T \subseteq S$ are sensors such that for each $s_i \in S_T$ there is p_l on

 $T = (p_{l_1}, \dots, p_{l_{k-1}}, p_{l_k})$ and $p_{l_i} \in P$ for which $|(s_i, p_{l_i})| \leq \delta$.

Autonomous Data Collection

- Having a set of sensors (sampling stations), we aim to determine a cost-efficient path to retrieve data by autonomous underwater vehicles (AUVs) from the individual sensors
 - E.g., Sampling stations on the ocean floor
- The planning problem is a variant of the Traveling Salesman Problem



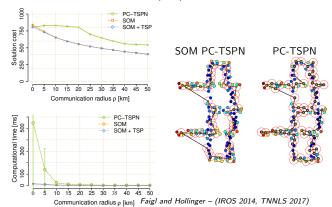
Two practical aspects of the data collection can be identified

- 1. Data from particular sensors may be of different importance
- 2. Data from the sensor can be retrieved using wireless communication

These two aspects (of general applicability) can be considered in the Prize-Collecting Traveling Salesman Problem (PC-TSP) and Orienteering Problem (OP) and their extensions with neighborhoods

PC-TSPN – Example of Solution

Ocean Observatories Initiative (OOI) scenario



■ Part 1 – Data Collection Planning

Overview of the Lecture

- Data Collection Planning Motivational Problem
- Traveling Salesman Problem (TSP)
- Traveling Salesman Problem with Neighborhoods (TSPN)
- Generalized Traveling Salesman Problem (GTSP)
- Noon-Bean Transformation
- Orienteering Problem (OP)
- Orienteering Problem with Neighborhoods (OPN)

Prize-Collecting Traveling Salesman Problem with Neighborhoods (PC-TSPN)

- Let *n* sensors be located in \mathbb{R}^2 at the locations $S = \{s_1, \dots, s_n\}$
- **Each** sensor has associated penalty $\xi(s_i) > 0$ characterizing additional cost if the data are not retrieved from si
- \blacksquare Let the data collecting vehicle operates in \mathbb{R}^2 with the motion cost $c(p_1, p_2)$ for all pairs of points $p_1, p_2 \in \mathbb{R}^2$
- The data from s_i can be retrieved within δ distance from s_i

Traveling Salesman Problem (TSP)

- Let S be a set of n sensor locations $S = \{s_1, \ldots, s_n\}, s_i \in \mathbb{R}^2$ and $c(s_i, s_i)$ is a cost of travel from s_i to s_i
- Traveling Salesman Problem (TSP) is a problem to determine a closed tour visiting each $s \in S$ such that the total tour length is minimal, i.e.,
 - determine a sequence of visits $\Sigma = (\sigma_1, \dots, \sigma_n)$ such that

minimize
$$_{\Sigma}$$
 $L = \left(\sum_{i=1}^{n-1} c(s_{\sigma_i}, s_{\sigma_{i+1}})\right) + c(s_{\sigma_n}, s_{\sigma_1})$ (2) subject to $\Sigma = (\sigma_1, \dots, \sigma_n), 1 \le \sigma_i \le n, \sigma_i \ne \sigma_j \text{ for } i \ne j$

- The TSP can be considered on a graph G(V, E) where the set of vertices V represents sensor locations S and E are edges connecting the nodes with the cost $c(s_i, s_i)$
- For simplicity we can consider $c(s_i, s_j)$ to be Euclidean distance; otherwise, it is a solution of the path planning problem Fuclidean TSP

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- If $c(s_i, s_i) \neq c(s_i, s_i)$ it is the **Asymmetric TSP**
- The TSP is known to be NP-hard unless P=NP

Existing solvers to the TSP

- Exact solutions
 - Branch and Bound, Integer Linear Programming (ILP)

E.g., Concorde solver - http://www.tsp.gatech.edu/concorde.html

- Approximation algorithms
 - Minimum Spanning Tree (MST) heuristic with $L \leq 2L_{opt}$
 - Christofides's algorithm with $L \leq \frac{3/2}{L_{out}}$
- Heuristic algorithms
 - Constructive heuristic Nearest Neighborhood (NN) algorithm
 - 2-Opt local search algorithm proposed by Croes 1958
 - Lin-Kernighan (LK) heuristic
- Soft-Computing techniques, e.g.,
 - Variable Neighborhood Search (VNS)
 - Evolutionary approaches
 - Unsupervised learning

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MST-based Approximation Algorithm to the TSP

- Minimum Spanning Tree Heuristic
 - 1. Compute the MST (denoted T) of the input graph G
 - 2. Construct a graph H by doubling every edge of T
 - 3. Shortcut repeated occurrences of a vertex in the tour



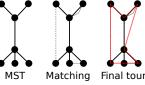
■ For the triangle inequality, the length of such a tour *L* is

 $L \leq 2L_{optimal}$,

where $L_{optimal}$ is the cost of the optimal solution of the TSP

Christofides's Algorithm to the TSP

- Christofides's algorithm
 - 1. Compute the MST of the input graph G
 - 2. Compute the minimal matching on the odd-degree vertices 3. Shortcut a traversal of the re-
 - sulting Eulerian graph



For the triangle inequality, the length of such a tour L is

Example of Unsupervised Learning for the TSP

where $L_{optimal}$ is the cost of the optimal solution of the TSP

Length of the MST is $< L_{optimal}$

Learning epoch 35

Learning epoch 53

E.g., using evolutionary techniques or unsupervised learning

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Sum of lengths of the edges in the matching $\leq \frac{1}{2}L_{optimal}$

$L \leq \frac{3}{2} L_{optimal}$,

2-Opt Heuristic

initial route

insertion

1. Use a construction heuristic to create an

2. Repeat until no improvement is made

■ route[0] to route[i-1]

NN algorithm, cheapest insertion, farther

2.1 Determine swapping that can shorten the

tour (i, j) for $1 \le i \le n$ and $i + 1 \le j \le n$

■ route[i] to route[j] in reverse order route[i] to route[end]

 Update the current route if length is shorter than the existing solution

■ Determine length of the route

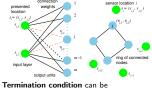
Unsupervised Learning based Solution of the TSP

- Sensor locations $S = \{s_1, ..., s_n\}$, $s_1 \in \mathbb{R}^2$; Neurons $\mathcal{N} = (\nu_1, ..., \nu_m)$, $\nu_i \in \mathbb{R}^2$, m = 2.5n
- Learning gain σ ; epoch counter i; gain decreasing rate $\alpha = 0.1$; learning rate $\mu = 0.6$
- 1. $\mathcal{N} \leftarrow \text{init ring of neurons as a small ring around some } s_i \in \mathcal{S}$, e.g., a circle with radius 0.5
- 2. $i \leftarrow 0$; $\sigma \leftarrow 12.41n + 0.06$;
- //clear inhibited neurons
- 4. foreach $s \in \Pi(S)$ (a permutation of S) 4.1 $\nu^* \leftarrow \operatorname{argmin}_{\nu \in \mathcal{N} \setminus I} ||(\nu, s)||$
 - 4.2 foreach ν in d neighborhood of ν^*

$$\nu \leftarrow \nu + \mu f(\sigma, d)(s - \nu)$$

$$\left(e^{-\frac{d^2}{\sigma^2}} \text{ for } d < 0 \right)$$

- 4.3 $I \leftarrow I \cup \{ \{ \nu^* \} \}$ // inhibit the winner
- 5. $\sigma \leftarrow (1-\alpha)\sigma$; $i \leftarrow i+1$;
- 6. If (termination condition is not satisfied) Goto Step 3; Otherwise retrieve solution

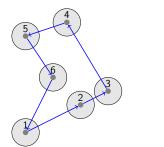


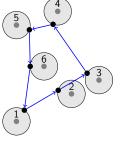
- Maximal number of learning epochs i ≤ i_{max} , e.g., $i_{max} = 120$
- Winner neurons are negligibly close to sensor locations, e.g., less than 0.001

Somhom, S., Modares, A., Enkawa, T. (1999): Competition-based neural network for the mul

Traveling Salesman Problem with Neighborhoods (TSPN)

- Euclidean TSPN with disk shaped δ -neighborhoods
- Sequence of visits to the regions with particular locations of the visit





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Approaches to the TSPN

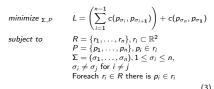
Learning epoch 12

Learning epoch 42

- A direct solution of the TSPN approximation algorithms and heuristics
- Decoupled approach
 - 1. Determine sequence of visits Σ independently on the locations PE.g., as the TSP for centroids of the regions R
 - 2. For the sequence Σ determine the locations P to minimize the total tour length, e.g.,
 - Touring polygon problem (TPP)
 - Sampling possible locations and use a forward search for finding the best locations
 - Continuous optimization such as hill-climbing E.g., Local Iterative Optimization (LIO), Váña & Faigl (IROS 2015)
- Sampling-based approaches
 - For each region, sample possible locations of visits into a discrete set of locations for each region
 - The problem can be then formulated as the Generalized Traveling Salesman Problem (GTSP)
- **E**uclidean TSPN with, e.g., disk-shaped δ neighborhoods
 - lacktriangle Simplified variant with regions as disks with radius δ remote sensing with the δ communication range

Traveling Salesman Problem with Neighborhoods (TSPN)

- Instead visiting a particular location $s \in S$, $s \in \mathbb{R}^2$ we can request to visit, e.g., a region $r \subset \mathbb{R}^2$ to save travel cost, i.e., visit regions $R = \{r_1, \dots, r_n\}$
- The TSP becomes the TSP with Neighborhoods (TSPN) where it is necessary, in addition to the determination of the order of visits Σ , determine suitable locations $P = \{p_1, \dots, p_n\}, p_i \in r_i$, of visits to R
- The problem is a combination of combinatorial optimization to determine Σ with continuous optimization to determine P



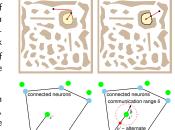


In general, TSPN is APX-hard, and cannot be approximated to within a factor $2 - \epsilon$, $\epsilon > 0$, unless P = NP.

Safra, S., Schwartz, O. (2006)

Unsupervised Learning for the TSPN

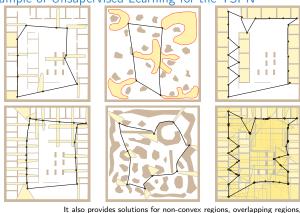
- In the unsupervised learning for the TSP, we can sample suitable sensing locations during winner selection
- We can use the centroid of the region for the shortest path computation from ν to the region r presented to the network
- Then, an intersection point of the path with the region can be used as an alternate location
- For the Euclidean TSPN with disk-shaped δ neighborhoods, we can compute the alternate location directly from the Euclidean distance



Faigl, J. et al. (2013): Visiting convex regions in a polygonal map. Robotics and Autonomous Systems.

B4M36UIR - Lecture 07: Data Collection Planning B4M36UIR - Lecture 07: Data Collection Planning Sampling-based Decoupled Solution of the TSPN

Example of Unsupervised Learning for the TSPN

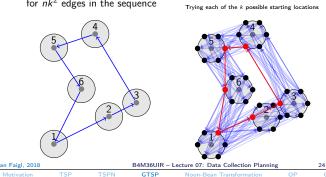


and coverage problems.

Solving the TSPN as the TPP - Iterative Refinement

- Let the sequence of *n* polygon regions be $R = (r_1, ..., r_n)$
- 1. Sampling the polygons into a discrete set of points and determine all shortest paths between each sampled points in the sequence of the regions visits
- 2. Initialization: Construct an initial touring polygons path using a sampled point of each region Let the path be defined by $P = (p_1, p_2, ..., p_n)$, where $p_i \in r_i$ and L(P) be the length of the shortest path induced by P
- 3. Refinement: For $i = 1, 2, \ldots, n$
 - Find p_i^* ∈ r_i minimizing the length of the path $d(p_{i-1}, p_i^*) + d(p_i^*, p_{i+1})$, where $d(p_k, p_l)$ is the path length from p_k to p_l , $p_0 = p_n$, and $p_{n+1} = p_1$ If the total length of the current path over point p* is
 - shorter than over p_i , replace the point p_i by p_i^*
- 4. Compute path length Lnew using the refined points
- 5. Termination condition: If $L_{new} L < \epsilon$ Stop the refinement. Otherwise $L \leftarrow L_{new}$ and go to Step 3
- 6. Final path construction: use the last points and construct the path using the shortest paths among obstacles between two consecutive points





Transformation of the GTSP to the Asymmetric TSP

■ The Generalized TSP can be transformed into the Asymmetric

TSP that can be then solved, e.g., by LKH or exactly using

Concorde with further transformation of the problem to the TSP

■ Sample each neighborhood with, e.g., k = 6 samples

the centroids of the regions

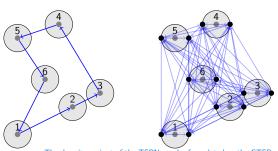
for nk^2 edges in the sequence

■ Determine sequence of visits, e.g., by a solution of the ETSP for

■ Finding the shortest tour takes in a forward search graph $O(nk^3)$

Sampling-based Solution of the TSPN

- For an unknown sequence of the visits to the regions, there are $\mathcal{O}(n^2k^2)$ possible edges
- Finding the shortest path is NP-hard, we need to determine the sequence of visits, which is the solution of the TSP

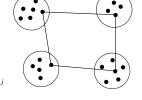


The descrite variant of the TSPN can be formulated as the GTSF B4M36UIR - Lecture 07: Data Collection Planning

Generalized Traveling Salesman Problem (GTSP)

- For sampled neighborhoods into discrete sets of locations, we can formulate the problem as the Generalized Traveling Salesman Problem (GTSP)
- For a set of n sets $S = \{S_1, \dots, S_n\}$, each with particular set of locations (nodes) $S_i = \{s_1^i, \dots, s_{n_i}^i\}$
- The problem is to determine the shortest tour visiting each set S_i , i.e., determining the order Σ of visits to S and a particular locations $s^i \in S_i$ for each $S_i \in S$

 $\Sigma = (\sigma_1, \dots, \sigma_n), 1 \le \sigma_i \le n, \sigma_i \ne \sigma_j \text{ for } i \ne j$ $s^{\sigma_i} \in S_{\sigma_i}, S_{\sigma_i} = \{s_1^{\sigma_i}, \dots, s_{n-1}^{\sigma_i}\}, S_{\sigma_i} \in S$



■ In addition to exact, e.g., ILP-based, solution, a heuristic algorithm **GLNS** is available (besides other heuristics)

Smith, S. L., Imeson, F. (2017), GLNS: An effective large neighborhood search heuristic the Generalized Traveling Salesman Problem. Computers and Operations Research.

Implementation in Julia - https://ece.uwaterlog.ca/~sl2smith/GLW

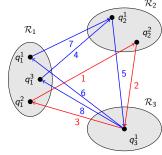
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A transformation of the GTSP to the ATSP has been proposed by Noon and Bean in 1993, and it is called as the Noon-Bean Transformation

Noon, C.E., Bean, J.C. (1993), An efficient transformation of the ge problem, INFOR: Information Systems and Operational Research Ben-Arieg, et al. (2003), Transfo

Noon-Bean Transformation

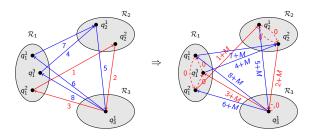
- Noon-Bean transformation to transfer GTSP to ATSP
- Modify weight of the edges (arcs) such that the optimal ATSP tour visits all vertices of the same cluster before moving to the next cluster
 - Adding a large a constant M to the weights of arcs connecting the clusters, e.g., a sum of the *n* heaviest edges
 - Ensure visiting all vertices of the cluster in prescribed order, i.e., creating zero-length cycles within each cluster
- The transformed ATSP can be further transformed to the TSP For each vertex of the ATSP created 3 ver
 - tices in the TSP, i.e., it increases the size of



Noon, C.E., Bean, J.C. (1993), An efficient transformation of the generalized traveling salesman m. INFOR: Information Systems and Operational Research

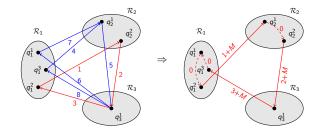
Example – Noon-Bean transformation (GATSP to ATSP)

- 1. Create a zero-length cycle in each set and set all other arcs to ∞ To ensure all vertices of the cluster are visited before leaving the cluster
- 2. For each edge (q_i^m, q_i^n) create an edge (q_i^m, q_i^{n+1}) with a value increased by sufficiently large M



Example – Noon-Bean transformation (GATSP to ATSP)

- 1. Create a zero-length cycle in each set and set all other arcs to ∞ (or 2M) To ensure all vertices of the cluster are visited before leaving the cluster
- 2. For each edge (q_i^m, q_i^n) create an edge (q_i^m, q_i^{n+1}) with a value increased by sufficiently large M



Noon-Bean transformation – Matrix Notation

■ 1. Create a zero-length cycle in each set; and 2. for each edge (q_i^m, q_i^n) create an edge (q_i^m, q_i^{n+1}) with a value increased by sufficiently large M



Transformed ATSP

Original	GA	I SP
1	1	2

_							
	q_1^1	q_1^2	q_1^3	q_2^1	q_2^2	q_3^1	
q_1^1	∞	∞	∞	7	_	_	(
q_1^1 q_1^2 q_1^3	∞	∞	∞	-	1	_	(
q_{1}^{3}	∞	∞	∞	4	_	_	(
q_{2}^{1} q_{2}^{2}	-	-	-	∞	∞	5	(
q_{2}^{2}	_	_	_	∞	∞	2	(
q_3^1	6	3	8	_	-	∞	(

	q_1^1	q_1^2	q_1^3	q_2^1	q_{2}^{2}	q_3^1
q_1^1	∞	0	∞	-	7+ <i>M</i>	-
q_1^1 q_1^2 q_1^3	∞	∞	0	1+M	_	_
q_{1}^{3}	0	∞	∞	_	4+M	_
q_2^1	-	-	-	∞	0	5+ <i>M</i>
q_{2}^{1} q_{2}^{2}	-	_	_	0	∞	2+ <i>M</i>
q_3^1	8+ <i>M</i>	6+ <i>M</i>	3+ <i>M</i>	_	-	0

Orienteering Problem – Specification

- Let the given set of n sensors be located in \mathbb{R}^2 with the locations $S = \{s_1, \ldots, s_n\}, s_i \in \mathbb{R}^2$
- Each sensor s_i has an associated score ζ_i characterizing the reward if data from si are collected
- The vehicle is operating in \mathbb{R}^2 , and the travel cost is the Euclidean distance
- Starting and final locations are prescribed
- We aim to determine a subset of k locations $S_k \subseteq S$ that maximizes the sum of the collected rewards while the travel cost to visit them is below T_{max}

The Orienteering Problem (OP) combines two NP-hard problems:

- Knapsack problem in determining the most valuable locations $S_k \subseteq S$
- Travel Salesman Problem (TSP) in determining the shortest tour

OP Benchmarks - Example of Solutions



T_{max}=80, R=1248





T_{max}=80, R =1278 T_{max}=45, R=756

Noon-Bean Transformation – Summary

- It transforms the GATSP into the ATSP which can be further
 - Solved by existing solvers, e.g., the Lin-Kernighan heuristic algorithm (LKH) http://www.akira.ruc.dk/~keld/research/LKH

- the ATSP can be further transformed into the TSP and solve it optimaly, e.g., by the Concorde solver, tsp.gatech.edu/concorde.html
- It runs in $\mathcal{O}(k^2n^2)$ time and uses $\mathcal{O}(k^2n^2)$ memory, where n is the number of sets (regions) each with up to k samples
- The transformed ATSP problem contains kn vertices

Noon, C.E., Bean, J.C. (1993), An efficient transformation of the generalized traveling salesma

Orienteering Problem – Optimization Criterion

- Let $\Sigma = (\sigma_1, \dots, \sigma_k)$ be a permutation of k sensor labels, $1 \le \sigma_i \le$ *n* and $\sigma_i \neq \sigma_i$ for $i \neq i$
- lacksquare Σ defines a tour $T=(s_{\sigma_1},\ldots,s_{\sigma_k})$ visiting the selected sensors S_k
- Let the start and end points of the tour be $\sigma_1 = 1$ and $\sigma_k = n$
- The Orienteering problem (OP) is to determine the number of sensors k, the subset of sensors S_k , and their sequence Σ such that

maximize_{k,S_k,\Sigma}
$$R = \sum_{i=1}^{k} \zeta_{\sigma_i}$$

subject to $\sum_{i=2}^{k} |(s_{\sigma_{i-1}}, s_{\sigma_i})| \le T_{max}$ and $s_{\sigma_1} = s_1, s_{\sigma_k} = s_n.$ (4)

The OP combines the problem of determining the most valuable locations S_k with finding the shortest tour T visiting the locations S_k . It is NP-hard, since for $s_1 = s_n$

and particular S_k it becomes the TSP.

Unsupervised Learning for the OP 1/2

- A solution of the OP is similar to the solution of the PC-TSP and TSP
- We need to satisfy the limited travel budget T_{max} , which needs the final tour over the sensing locations
- During the unsupervised learning, the winners are associated with the particular sensing locations, which can be utilized to determine the tour as a solution of the OP represented by the network:



Learning epoch 7 Learning epoch 55 Learning epoch 87 Final solution

■ This is utilized in the conditional adaptation of the network towards the sensing location and the adaptation is performed only if the tour represented by the network after the adaptation would satisfy T_{max}

The Orienteering Problem (OP)

- The problem is to collect as many rewards as possible within the given travel budget (T_{max}) , which is especially suitable for robotic vehicles such as multi-rotor Unmanned Aerial Vehicles (UAVs)
- The starting and termination locations are prescribed and can be different The solution may not be a closed tour as in the TSP

Travel budget $T_{max} = 50$,



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Existing Heuristic Approaches for the OP

Collected rewards R = 190

■ The Orienteering Problem has been addressed by several approaches, e.g.

4-phase heuristic algorithm proposed in [3] Results for the method proposed by Pillai in [2] Heuristic algorithm proposed in [1] Guided local search algorithm proposed in [4]

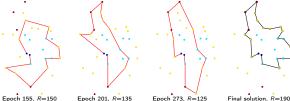
- [1] I.-M. Chao, B. L. Golden, and E. A. Wasil. A fast and effective heuristic for the orienteering problem. European Journal of Operational Research, 88(3):475-489, 1996.
- The traveling salesman subset-tour problem with one additional constraint Ph.D. thesis, The University of Tennessee, Knoxville, TN, 1992.
- [3] R. Ramesh and K. M. Brown An efficient four-phase heuristic for the generalized orienteering problem Computers & Operations Research, 18(2):151-165, 1991.
- [4] P. Vansteenwegen, W. Souffriau, G. V. Berghe, and D. V. Oudheusden. A guided local search metaheuristic for the team orienteering problem. European Journal of Operational Research, 196(1):118-127, 2009

Unsupervised Learning for the OP 2/2

- The winner selection for $s' \in S$ is conditioned according to T_{max}
 - The network is adapted only if the tour T_{win} represented by the current winners would be shorter or equal than T_{max}

$$\mathcal{L}(\mathit{T_{win}}) - |(\mathit{s_{
u_p}}, \mathit{s_{
u_n}})| + |(\mathit{s_{
u_p}}, \mathit{s'})| + |(\mathit{s'}, \mathit{s_{
u_n}})| \leq \mathit{T_{max}}$$

■ The unsupervised learning performs a *stochastic search* steered by the rewards and the length of the tour to be below T_{max}



■ Similarly to the TSP with Neighborhoods and PC-TSPN we can

formulate the Orienteering Problem with Neighborhoods.

Orienteering Problem with Neighborhoods

Comparison with Existing Algorithms for the OP

- Standard benchmark problems for the Orienteering Problem represent various scenarios with several values of T_{max}
- The results (rewards) found by different OP approaches presented as the average ratios (and standard deviations) to the best-known solution

Instances of the Tsiligirides problems

Problem Set	RB	PL	CGW	Unsupervised Learning
Set 1, $5 \le T_{max} \le 85$	0.99/0.01	1.00/0.01	1.00/0.01	1.00/0.01
Set 2, $15 \le T_{max} \le 45$	1.00/0.02	0.99/0.02	0.99/0.02	0.99/0.02
Set 3, $15 \le T_{max} \le 110$	1.00/0.00	1.00/0.00	1.00/0.00	1.00/0.00

Diamond-shaped (Set 64) and Square-shaped (Set 66) test problems

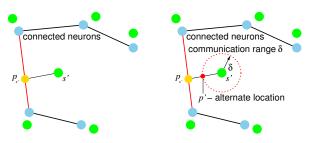
Problem Set	RB [†]	PL	CGW	Unsupervised Learning
Set 64, $5 \le T_{max} \le 80$	0.97/0.02	1.00/0.01	0.99/0.01	0.97/0.03
Set 66, $15 \le T_{max} \le 130$	0.97/0.02	1.00/0.01	0.99/0.04	0.97/0.02

Required computational time is up to units of seconds, but for small problems

,	max=45,	0=1.5,	N=1344

Generalization of the Unsupervised Learning to the Orienteering Problem with Neighborhoods

■ The same idea of the alternate location as in the TSPN



■ The location p' for retrieving data from s' is determined as the alternate goal location during the conditioned winner selection

Influence of the δ -Sensing Distance

 T_{max} =60, δ =1.5, R=1600

 Influence of increasing communication range to the sum of the collected rewards

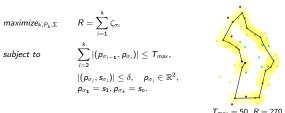
Problem	Solution of R _{best}	R_{SOM}	200	- 0- Tsiligirides Set 3, T _{max} =50 Diamond-shaped Set 64, T _{max} =45
Set 64, T _{max} =45 860 75		750 845	ected rewards - R ¹ 500 1000 1500	- Square-shaped Set 66, T _{nax} =60
the community is significantly is lected rewards, budget under	ation range ncreases t while keep	e δ may he col-	Colle	0.0 0.2 0.5 0.7 1.0 1.2 1.5 1.7 2.0 Communication range · δ

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Orienteering Problem with Neighborhoods

- Data collection using wireless data transfer allows to reliably retrieve data within some communication radius δ
 - \blacksquare Disk-shaped δ -neighborhood
- We need to determine the most suitable locations P_k such that



Introduced by Best, Faigl, Fitch (IROS 2016, SMC 2016, IJCNN 2017)

■ More rewards can be collected than for the OP formulation with the same travel budget T_{max}

OP with Neighborhoods (OPN) – Example of Solutions

■ Diamond-shaped problem Set 64 – SOM solutions for T_{max} and δ

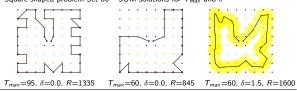






 T_{max} =80, δ =0.0, R=1278 T_{max} =45, δ =0.0, R=756

lacksquare Square-shaped problem Set 66 – SOM solutions for T_{max} and δ



In addition to unsupervised learning, Variable Neighborhood Search

(VNS) for the OP has been generalized to the OPN

Summary of the Lecture

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Topics Discussed

- Data Collection Planning motivational problem and solution
 - Prize-Collecting Traveling Salesman Problem with Neighborhoods (PC-TSPN)
- Traveling Salesman Problem (TSP)
 - Approximation and heuristic approaches
- Traveling Salesman Problem with Neighborhoods (TSPN)
 - Sampling-based and decoupled approaches
 - Unsupervised learning
- Generalized Traveling Salesman Problem (GTSP)
 - Heuristic and transformation (GTSP→ATSP) approaches
- Orienteering problem (OP)
 - Heuristic and unsupervised learning based approaches
- Orienteering problem with Neighborhoods (OPN)
 - Unsupervised learning based approach
- Next: Data-collection planning with curvature-constrained vehicles

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