## **Robotic Information Garthering -Exploration of Unknown Environment**

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Lecture 05

**B4M36UIR – Artificial Intelligence in Robotics** 

Part I

Part 1 – Robotic Exploration

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### Overview of the Lecture

■ Part 1 – Robotic Information Gathering - Robotic Exploration Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering 1 / 37 Jan Faigl, 2017 2 / 37 B4M36UIR - Lecture 05: Robotic Exploration Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Robotic Information Gathering Create a model of phenomena by autonomous mobile robots performing measurements in a dynamic unknown environment.



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Robotic Exploration of Unknown Environment Challenges in Robotic Information Gathering Robotic exploration is a fundamental problem of robotic information gathering Where to take new measurements? The problem is: To improve the phenomena model How to efficiently utilize a group of mo-What locations visit first? Learning bile robots to autonomously create a adaptivity On-line decision-making map of an unknown environment **Robotic Information** How to efficiently utilize more Gathering Performance indicators vs constraints robots? Planning Sensina Time, energy, map quality vs robots, communication To divide the task between the robots Performance in a real mission depends on uncertainty uncertaintv the on-line decision-making How to navigate robots to the selected locations? It includes the problems of: Improve Localization vs Model Map building and localization Determination of the navigational waypoints Where to go next? Path planning and navigation to the waypoints How to address all these aspects altogether to find a cost Coordination of the actions (multi-robot team) efficient solution using in-situ decisions? Courtesy of M. Kulich Jan Faigl, 2017 B4M36UIR - Lecture 05: Robotic Exploration 6 / 37 Jan Faigl, 2017 B4M36UIR - Lecture 05: Robotic Exploration 7 / 37 Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Environment Representation – Mapping and Occupancy Grid Mobile Robot Exploration Create a map of the environment The robot uses its sensors to build a map of the environment Frontier-based approach The robot should be localized to integrate new sensor measurements into a globally consistent map Yamauchi (1997) Occupancy grid map SLAM – Simultaneous Localization and Mapping Moravec and Elfes (1985) The robot uses the map being built to localize itself The map is primarily to help to localize the robot Laser scanner sensor The map is a "side product" of SLAM Next-best-view approach Grid map – discretized world representation Select the next robot goal A cell is occupied (an obstacle) or free Occupancy grid map Performance metric: Each cell is a binary random variable modeling Time to create the map of the whole environment the occupancy of the cell search and rescue mission

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## Occupancy Grid

#### Assumptions

- The area of a cell is either completely free or occupied
- Cells (random variables) are indepedent of each other
- The state is static
- A cell is a binary random variable modeling the occupancy of the cell
  - Cell  $m_i$  is occupied  $p(m_i) = 1$
  - Cell  $m_i$  is not occupied  $p(m_i) = 0$
  - Unknown  $p(m_i) = 0.5$
- Probability distribution of the map *m*

$$p(m) = \prod_i p(m_i)$$

• Estimation of map from sensor data  $z_{1:t}$  and robot poses  $x_{1:t}$ 

 $p(m|z_{1:t}, x_{1:t}) = \prod_i p(m_i|z_{1:t}, x_{1:t})$ 

Binary Bayes filter - Bayes rule and Markov process assumption

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# Binary Bayes Filter 2/2

Probability a cell is occupied

$$p(m_i|z_{1:t}, x_{1:t}) = \frac{p(m_i|z_t, x_t)p(z_t|x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1}, x_{1:t})}$$

Probability a cell is not occupied

 $p(\neg m_i | z_{1:t}, x_{1:t}) = \frac{p(\neg m_i | z_t, x_t) p(z_t | x_t) p(\neg m_i | z_{1:t-1}, x_{1:t-1})}{p(\neg m_i) p(z_t | z_{1:t-1}, x_{1:t})}$ 

Ratio of the probabilities

$$\frac{p(m_i|z_{1:t}, x_{1:t})}{p(\neg m_i|z_{1:t}, x_{1:t})} = \frac{p(m_i|z_t, x_t)p(m_i|z_{1:t-1}, x_{1:t-1})p(\neg m_i)}{p(\neg m_i|z_t, x_t)p(\neg m_i|z_{1:t-1}, x_{1:t-1})p(m_i)}$$
  
= 
$$\frac{p(m_i|z_t, x_t)}{1 - p(m_i|z_t, x_t)} \frac{p(m_i, z_{1:t-1}, x_{1:t-1})}{1 - p(m_i|z_{1:t-1}, x_{1:t-1})} \frac{1 - p(m_i)}{p(m_i)}$$
  
sensor model  $z_t$ , recursive term, prior

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# Binary Bayes Filter 1/2

free space

occupied space

p(m) = 0

 $p(m_i)=1$ 

- Sensor data  $z_{1:t}$  and robot poses  $x_{1:t}$
- Binary random variables are indepedent and states are static

$$p(m_{i}|z_{1:t}, x_{1:t}) = \frac{p(z_{t}|m_{i}, z_{1:t-1}, x_{1:t})p(m_{i}|z_{1:t-1}, x_{1:t})}{p(z_{t}|z_{1:t-1}, x_{1:t})}$$

$$\frac{p(m_{i}|z_{1:t}, x_{1:t}) = \frac{p(z_{t}|m_{i}, x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(z_{t}|z_{1:t-1}, x_{1:t})}$$

$$p(z_{t}|m_{i}, x_{t}) = \frac{p(m_{i}, z_{t}, x_{t})p(z_{t}, x_{t})}{p(m_{i}|x_{t})}$$

$$p(m_{i}, z_{1:t}, x_{1:t}) = \frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(m_{i}|x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

$$\frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(m_{i}|x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

$$P(m_{i}|z_{t}, x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1}) = \frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(m_{i})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

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$$P(m_{i}|z_{t}, x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1}) = \frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1})}{p(m_{i})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

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## Logs Odds Notation

Log odds ratio is defined as

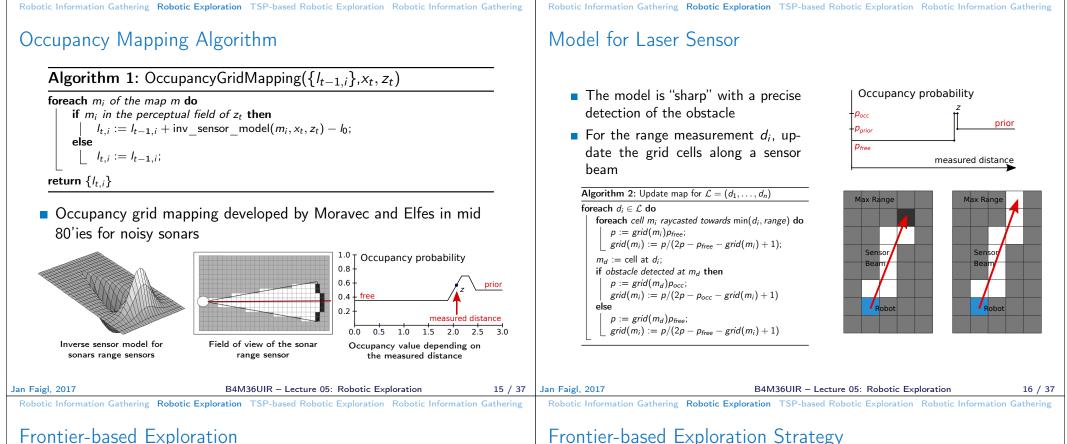
$$l(x) = \log \frac{p(x)}{1 - p(x)}$$

• and the probability p(x) is

$$p(x) = 1 - \frac{1}{1 - e^{I(x)}}$$

• The product modeling the cell  $m_i$  based on  $z_{1:t}$  and  $x_{1:t}$ 

$$I(m_i|z_{1:t}, x_{1:t}) = I(m_i|z_t, x_t) + I(m_i, |z_{1:t-1}, x_{1:t-1}) - I(m_i)$$
  
inverse sensor model recursive term prior

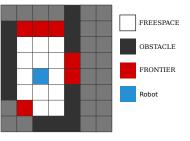


## Frontier-based Exploration

■ The basic idea of the frontier based exploration is navigation of the mobile robot towards unknown regions

Yamauchi (1997)

- **Frontier** a border of the known and unknown regions of the environment
- Based on the probability of individual cells in the occupancy grid, cells are classified into:
  - FREESPACE  $p(m_i) < 0.5$
  - OBSTACLE  $p(m_i) > 0.5$
  - UNKNOWN  $p(m_i) = 0.5$
- Frontier cell is a FREESPACE cell that is incident with an UNKNOWN cell
- Frontier cells as the navigation waypoints have to be reachable, e.g., after obstacle growing



Use grid-based path planning

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Algorithm 3: Frontier-based Exploration

map := init(robot, scan);

while there are some reachable frontiers do

Update occupancy *map* using new sensor data and Bayes rule;

- $\mathcal{M} :=$ Created grid map from *map* using thresholding;
- $\mathcal{M} :=$  Grow obstacle according to the dimension of the robot;

 $\mathcal{F} :=$  Determine frontier cells from  $\mathcal{M}$ :

 $\mathcal{F} :=$  Filter out unreachable frontiers from  $\mathcal{F}$ :

f := Select the closest frontier from  $\mathcal{F}$ , e.g. using shortest path;

path := Plan a path from the current robot position to f;

Navigate robot towards f along *path* (for a while);

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Multi-Robot Exploration – Map Marge	Multi-Robot Exploration – Overview			
• The individual maps can be merged in a similar way as integration of new sensor measurements $P(occ_{x,y}) = \frac{odds_{x,y}}{1 + odds_{x,y}}, \\ odds_{x,y} = \prod_{i=1}^{n} odds_{x,y}^{i}, \\ odds_{x,y}^{i} = \frac{P(occ_{x,y})}{1 - P(occ_{x,y})}.$ $P(occ_{x,y}^{i})$ $P(occ_{x,y}^{i})$ is the probability that grid cell on the global coordinate is occupied in the map of the robot. We need the same global reference frame (localization)	<ul> <li>We need to assign navigation waypoint to each robot, which can be formulated as the task-allocation problem</li> <li>Exploration can be considered as an iterative procedure <ol> <li>Initialize the occupancy grid Occ</li> <li>M ← create_navigation_grid(Occ) cells of M have values {freespace, obstacle, unknown}</li> <li>F ← detect_frontiers(M)</li> <li>Goal candidates G ← generate(F)</li> <li>Assign next goals to each robot r ∈ R, ((r<sub>1</sub>, g<sub>n</sub>),, (r<sub>m</sub>, g<sub>rm</sub>)) = assign(R, G, M)</li> <li>Create a plan P<sub>i</sub> for each pair (r<sub>i</sub>, g<sub>n</sub>) consisting of simple operations <ol> <li>Perform each plan up to smax operations At each step, update Occ using new sensor measurements</li> <li>If  G  == 0 exploration finished, otherwise go to Step 2</li> </ol> </li> </ol></li></ul>			
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Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Exploration Procedure – Decision-Making Parts 1. Initialize – set plans for <i>m</i> robots, $\mathcal{P} = (P_1, \dots, P_m)$ , $P_i = \emptyset$ .	Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Improvements of the basic Frontier-based Exploration			
2. Repeat	Several improvements have been proposed in the literature			
<ul> <li>2.1 Navigate robots using the plans P;</li> <li>2.2 Collect new measurements;</li> <li>2.3 Update the navigation map M;</li> <li>Until replanning condition is met.</li> <li>3. Determine goal candidates G from M.</li> <li>4. If  G  &gt; 0 assign goals to the robots <ul> <li>(⟨r<sub>1</sub>, g<sub>r<sub>1</sub></sub>⟩,, ⟨r<sub>m</sub>, g<sub>r<sub>m</sub></sub>⟩)=assign(R, G, M),</li> <li>r<sub>i</sub> ∈ R, g<sub>r<sub>i</sub></sub> ∈ G;</li> <li>Plan paths to the assigned goals</li> <li>P = plan(⟨r<sub>1</sub>, g<sub>r<sub>1</sub></sub>⟩,, ⟨r<sub>m</sub>, g<sub>r<sub>m</sub></sub>⟩, M);</li> </ul> </li> </ul>	<ul> <li>Introducing utility as a computation of expected covered area from a frontier González-Baños, Latombe (2002)</li> <li>Map segmentation for identification of rooms and exploration of the whole room by a single robot Holz, Basilico, Amigoni, Behnke (2010)</li> <li>Consider longer planning horizon (as a solution of the Traveling Salesman Problem (TSP)) Zlot, Stentz (2006), Kulich, Faigl (2011, 2012)</li> <li>Representatives of free edges Faigl, Kulich (2015)</li> </ul>			

- Go to Step 2.
- 5. Stop all robots or navigate them to the depot

All reachable parts of the environment are explored.

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## Multi-Robot Exploration Strategy

- A set of *m* robots at positions R = $\{r_1, r_2, \ldots, r_m\}$
- At time t, let a set of n goal candidates be  $\boldsymbol{G}(t) = \{g_1, \ldots, g_n\}$ I.e. frontiers



The exploration strategy (at the planning step *t*):

Select a goal  $g \in G(t)$  for each robot  $r \in \mathbf{R}$  that will minimize the required time to explore the environment.

The problem is formulated as the task-allocation problem

 $(\langle r_1, g_{r_1} \rangle, \ldots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}),$ 

where  $\mathcal{M}$  is the current map

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## Multi-Robot Exploration – Problem Definition

Evaluate all goals using the robot-goal distance

Using frontier representatives improves the per-

Solve the associated traveling salesman problem (TSP)

■ Greedy goal selection – the closest one

A length of the path from the robot position to the

A problem of creating a grid map of the unknown environment by a set of *m* robots  $\mathbf{R} = \{r_1, r_2, ..., r_m\}$ .

Kulich, M., Faigl, J. Přeučil, L. (2011): On Distance Utility in the Exploration Task. ICRA.

Exploration is an iterative procedure:

1. Collect new sensor measurements

**Distance Cost Variants** 

formance a bit

TSP distance cost

Simple robot-goal distance

goal candidate

Consider visitations of all goals

Use frontier representatives

A length of the tour visiting all goals

e.g., expected coverage (utility)

• the TSP distance cost improves performance

about 10-30% without any further heuristics,

2. Determinate a set of goal candidates

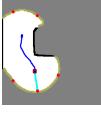
$$\boldsymbol{G}(t) = \{g_1, g_2, \ldots, g_n\}$$

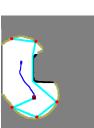
e.g., frontiers

3. At time step t, select next goal for each robot as the task-allocation problem

> $(\langle r_1, g_{r_1} \rangle, \ldots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}(t))$ using the distance cost function

- 4. Navigate robots towards goal
- 5. If  $|\mathbf{G}(t)| > 0$  go to Step 1; otherwise terminate







Goal Assignment Strategies – Task Allocation Algorithms

#### 1. Greedy Assignment

Yamauchi B, Robotics and Autonomous Systems 29, 1999

Randomized greedy selection of the closest goal candidate

#### 2. Iterative Assignment

Werger B, Mataric M, Distributed Autonomous Robotic Systems 4, 2001

Centralized variant of the broadcast of local eligibility algorithm (BLE)

#### 3. Hungarian Assignment

• Optimal solution of the task-allocation problem for assignment of *n* goals and *m* robots in  $O(n^3)$ 

Stachniss C, C implementation of the Hungarian method, 2004

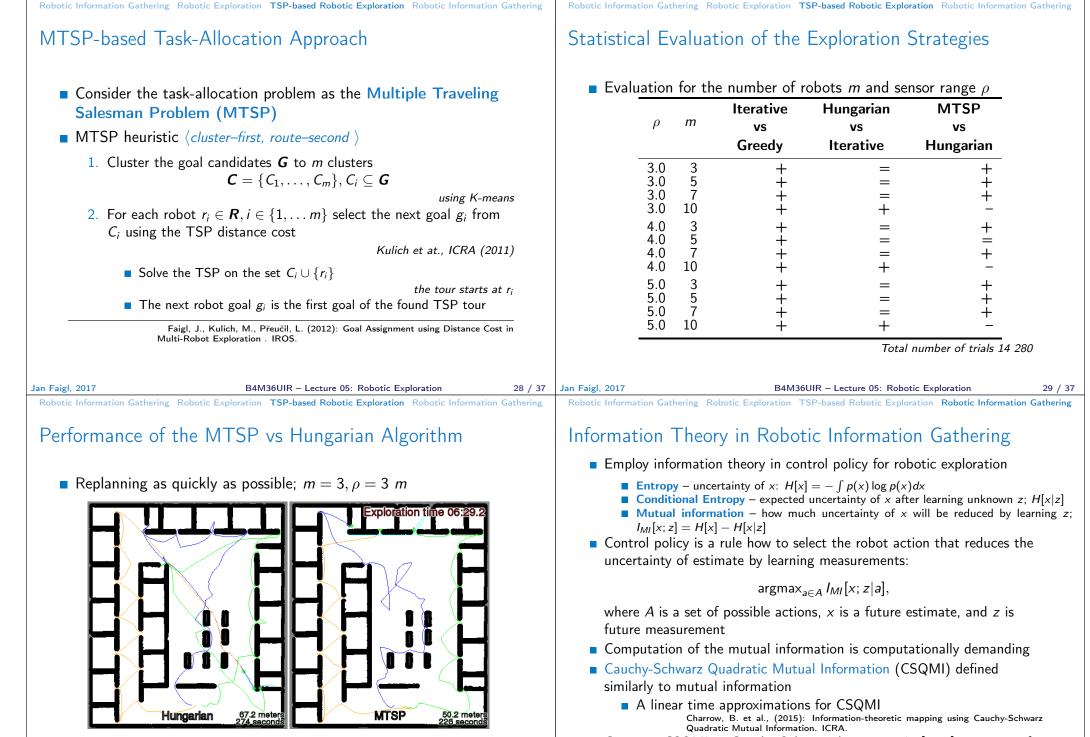
#### 4. Multiple Traveling Salesman Problem – MTSP Assignment

cluster-first, route-second, the TSP distance cost

Faigl et al. 2012

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The MTSP assignment provides better performance

#### Compute CSQMI as Cauchy-Schwarz divergence I<sub>CS</sub>[m; z] – raycast of the sensor beam and determine distribution over the range returns

Aerial vehicle

## Example of Autonomous Exploration using CSQMI

Planning with trajectory optimization – determine trajectory maximizing I<sub>CS</sub>

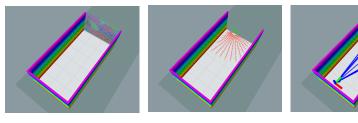
mization for Dense 3D Mapping. RSS.

Charrow, B. et al., (2015): Information-Theoretic Planning with Trajectory Opti-

Ground vehicle

## Actions

Actions are shortest path to cover the frontiers



Detect and cluster frontiers Sampled poses to cover a cluster Paths to the sampled poses

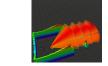
Select an action (a path) that maximizes the rate of Cauchy-Schwarz Quadratic Mutual Information

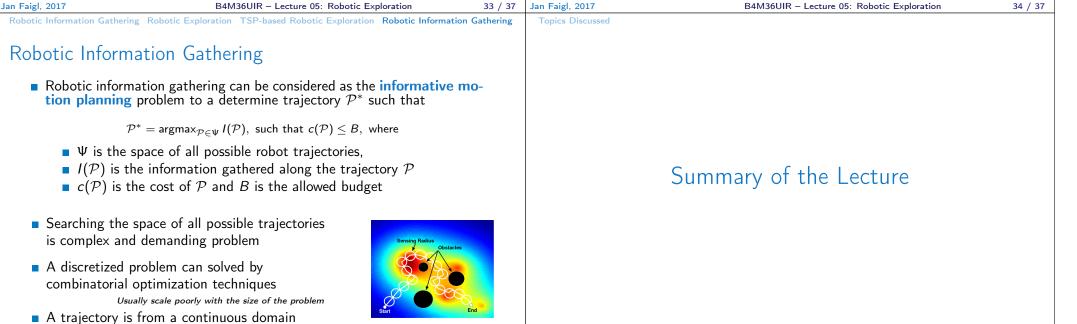












Sampling-based motion planning techniques can employed for

finding maximally informative trajectories Hollinger, G., Sukhatme, G. (2014): Sampling-based robotic information gathering algorithms. IJRR.

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## Topics Discussed

- Robotic information gathering
- Robotic exploration of unknown environment
- Occupancy grid map
- Frontier based exploration
- Exploration procedure and decision-making
- **TSP-based distance cost in frontier-based exploration**
- Multi-robot exploration and task-allocation
- Mutual information and informative path planning informative and motivational

Next: Randomized sampling-based motion planning methods

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