

# Genetic Programming

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<http://cw.felk.cvut.cz/doku.php/courses/a0m33eoa/start>

























## GP Initialisation: Common Methods

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Characteristics of GROW:

- does not have a size parameter – does not allow the user to create a desired size distribution,
- does not allow the user to define the expected probabilities of certain nodes appearing in trees,
- does not give the user much control over the tree structures generated.
- there is no appropriate way to create trees with either a fixed or average tree size or depth.

RAMPED HALF-AND-HALF – GROW & FULL method each deliver half of the initial population.

$D$  is chosen between 2 to 6,

# GP Initialization: Probabilistic Tree-Creation Method

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Probabilistic tree-creation method:

- An expected desired tree size can be defined.
- Probabilities of occurrence for specific functions and terminals within the generated trees can be defined.
- Fast – running in time near-linear in tree size.

Definitions:

- $\mathbf{T}$  denotes a newly generated tree.
- $D$  is the maximal depth of a tree.
- $E_{tree}$  is the expected tree size of  $\mathbf{T}$ .
- $F$  is a function set divided into terminals  $T$  and nonterminals  $N$ .
- $p$  is the probability that an algorithm will pick a nonterminal.
- $b$  is the expected number of children to nonterminal nodes from  $N$ .
- $g$  is the expected number of children to a newly generated node in  $\mathbf{T}$ .

$$g = pb + (1 - p)(0) = pb$$



















# GP: Crossover Operators

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**Standard crossover** operators used in GP, like standard 1-point crossover, are designed to ensure **just the syntactic closure property**.

- On the one hand, they produce syntactically valid children from syntactically valid parents.
- On the other hand, the only semantic guidance of the search is from the fitness measured by the difference of behavior of evolving programs and the target programs.

This is very different from real programmers' practice where any change to a program should pay heavy attention to the change in semantics of the program.

To remedy this deficiency in GP genetic operators making use of the semantic information has been introduced:

- **Semantically Driven Crossover (SDC)**

[Beadle08] Beadle, L., Johnson, C.G.: *Semantically Driven Crossover in Genetic Programming*, 2008.

- **Semantic Aware Crossover (SAC)**

[Nguyen09] Nguyen, Q.U. et al.: *Semantic Aware Crossover for Genetic Programming: The Case for Real-Valued Function Regression*, 2009.











## Automatically Defined Functions: Motivation

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**Hierarchical problem-solving** ("divide and conquer") may be advantageous in solving large and complex problems because the solution to an overall problem may be found by decomposing it into smaller and more tractable subproblems in such a way that the solutions to the subproblems are reused many times in assembling the solution to the overall problem.

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**Automatically Defined Functions** (Koza94) – idea similar to reusable code represented by subroutines in programming languages.

- Reuse eliminates the need to "reinvent the wheel" on each occasion when a particular sequence of steps may be useful.
- Subroutines are reused with different instantiation of dummy variables.
- Reuse makes it possible to exploit a problem's modularities, symmetries and regularities.
- Code encapsulation – protection from crossover and mutation.
- Simplification – less complex code, easier to evolve.
- Efficiency – acceleration of the problem-solving process (i.e. the evolution).

[Koza94] Genetic Programming II: Automatic Discovery of Reusable Programs, 1994











## Even-3-Parity Function: Blind Search vs. Simple GP

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Experimental setup:

- Function set:  $F = \{\text{AND, OR, NAND, NOR}\}$
- The number of internal nodes fixed to 20.
- Blind search – randomly samples 10,000,000 trees
- GP without ADFs
  - Population size  $M = 50$ .
  - Number of generations  $G = 25$ .
  - A run is terminated as soon as it produces a correct solution.
  - Total number of trees generated 10,000,000.

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Results – number of times the correct function appeared in 10,000,000 generated trees:

Blind search	0
GP without ADFs	2





















## GP with Hierarchical ADFs

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Hierarchical form of automatic function definition – any function can call upon any other already-defined function.

- Hierarchy of function definitions where any function can be defined in terms of any combination of already-defined functions.
- All ADFs have the same number of dummy arguments. Not all of them have to be used in a particular function definition.
- VPB has access to all of the already defined functions.

Setup of the GP with hierarchical ADFs:

- ADF0 branch  
Functions:  $F = \{\text{AND, OR, NAND, NOR}\}$ , Terminals:  $A2 = \{\text{ARG0, ARG1, ARG2}\}$
- ADF1 branch  
Functions:  $F = \{\text{AND, OR, NAND, NOR, ADF0}\}$ , Terminals:  $A3 = \{\text{ARG0, ARG1, ARG2}\}$
- Value-producing branch  
Functions:  $F = \{\text{AND, OR, NAND, NOR, ADF0, ADF1}\}$ , Terminals:  $T4 = \{D0, D1, D2, D3\}$





## Reading

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- Poli, R., Langdon, W., McPhee, N.F.: *A Field Guide to Genetic Programming*, 2008, <http://www.gp-field-guide.org.uk/>
- Koza, J.: *Genetic Programming: On the Programming of Computers by Means of Natural Selection*, MIT Press, 1992.