

# Parameter Control in Evolutionary Algorithms

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<http://cw.felk.cvut.cz/doku.php/courses/a0m33eoa/start>

## Algorithm Configuration: Motivation

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Often, finding performance-optimizing **parameter configurations of heuristic algorithms requires considerable effort**. In many cases, this task is performed **manually in an ad-hoc way**.

Automating this task is of high practical relevance in several contexts:

- **Development of complex algorithms** - setting the parameters of a heuristic algorithm is a highly labour-intensive task, and indeed can consume a large fraction of overall development time. The use of automated algorithm configuration methods can lead to significant time savings and potentially achieve better results than manual, ad-hoc methods.
- **Empirical studies, evaluations, and comparisons of algorithms** - a central question in comparing heuristic algorithms is whether one algorithm outperforms another because it is fundamentally superior, or because its developers more successfully optimized its parameters. Automatic algorithm configuration methods can mitigate this problem of unfair comparisons and thus facilitate more meaningful comparative studies.
- **Practical use of algorithms** - the ability of complex heuristic algorithms to solve large and hard problem instances often depends critically on the use of suitable parameter settings. End users often have little or no knowledge about the impact of an algorithm's parameter settings on its performance, and thus simply use default settings. Automatic algorithm configuration methods can be used to improve performance in a principled and convenient way.

# Parameter Tuning

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Typically done by experimenting with different values and selecting the ones that give the best results on the test problems at hand.

Technical drawbacks to parameter tuning:

- Parameters are not independent, but trying all different combinations systematically is practically impossible.
- It is heavily based on personal experience and is guided by a mixture of rules of thumb.
- The process of parameter tuning is time consuming, even if parameters are optimised one by one, regardless of their interactions.
- For a given problem the selected parameter values are not necessarily optimal, even if the effort made for setting them was significant.
- There are no generally good parameter settings since specific problems require specific setups for satisfactory performance.





## Parameter Tuning: F-Race

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**F-Race** [Birattari02] – procedure that empirically evaluates a set of candidate configurations by discarding bad ones as soon as statistically sufficient evidence is gathered against them.

- The process starts from a given finite pool of candidate configurations.
- If sufficient evidence is gathered that some candidate is inferior to at least another one, such a candidate is dropped from the pool and the procedure is iterated over the remaining ones.

The methodology can be applied to repetitive problems – problems where many similar instances appear over time.

# Automatic Algorithm Configuration and Parameter Tuning

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- $\Theta$  is the finite set of candidate configurations.
- $I$  is the possibly infinite set of instances.
- $P_I$  is a probability measure over the set  $I$  of instances – indicates the probability that the instance  $i$  is selected for being solved.
- $t : I \rightarrow \mathfrak{R}$  is a function associating to every instance the computational time allocated to it.
- $c(\theta, i) = c(\theta, i, t(i))$  is a random variable representing the cost of the best solution found by running configuration  $\theta$  on instance  $i$  for  $t(i)$  seconds.
- $C \subset \mathfrak{R}$  is the range of  $c$ , that is, the possible values for the cost of the best solution found in a run of a configuration  $\theta \in \Theta$  on an instance  $i \in I$ .
- $P_C$  is a probability measure over the set  $C$ :  $P_C(c|\theta, i)$  indicates the probability that  $c$  is the cost of the best solution found by running configuration  $\theta$  on instance  $i$  for  $t(i)$  seconds.
- $C(\theta) = C(\theta|\Theta, I, P_I, P_C, t)$  is the criterion that needs to be optimized with respect to  $\theta$ .
  - $P_I$  and  $P_C$  are unknown,
  - we can only estimate them.







## F-Race: Algorithm

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The optimization problem is tackled by generating a sequence  $\Theta_0 = \Theta \supseteq \Theta_1 \supseteq \Theta_2 \supseteq \dots$

The step from a set  $\Theta_{k-1}$  to  $\Theta_k$  is realized as follows

1. At step  $k$ , a new instance  $\underline{i}_k$  is considered; each candidate  $\theta \in \Theta_{k-1}$  still in the race is executed on  $\underline{i}_k$  and each observed cost  $c(\theta, \underline{i}_k)$  is appended to its  $\underline{c}^{k-1}(\theta, \underline{i})$ .
2. An aggregate comparison of the arrays  $\underline{c}^k(\theta, \underline{i})$  for all  $\theta \in \Theta_{k-1}$  is carried out by a statistical test – non-parametric Friedman 2-way analysis of variance by ranks.

The null hypothesis being that all possible rankings of the candidates within each block are equally likely.

3. If the null hypothesis is rejected, pairwise comparisons between the best candidate and each other one are carried out by means of the t-test. All candidates that result significantly worse than the best one are discarded.

Otherwise, all candidates in  $\Theta_{k-1}$  pass to  $\Theta_k$ .



## F-Race: Final Remarks

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Good technique, but:

- not suited for applications with large configuration spaces;
- thus, mainly used for configuration problems with few parameters and rather small configuration spaces.