# A0B17MTB – Matlab

Part #11



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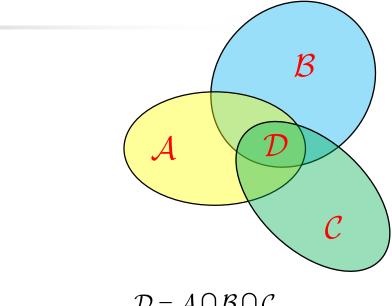


# Learning how to ...

**Set operations** 

Sorting

Searching



 $\mathcal{D} = \mathcal{A} \cap \mathcal{B} \cap \mathcal{C}$  $\mathcal{A} \cap \mathcal{B} = \left\{ x : x \in \mathcal{A} \land x \in B \right\}$ 



17.12.2018 13:29

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2

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# Set operations

- there exist following operations (operators) in Matlab applicable to arrays or individual elements
  - arithmetic (part #1)
  - relational (part #4)
  - logical (part #4)
  - <u>set</u> (part #7)
  - bit-wise (help, >> doc)

- set operations are applicable to vectors matrices, arrays, cells, strings, tables, ...
  - mutual sizes of these structures are usually not important

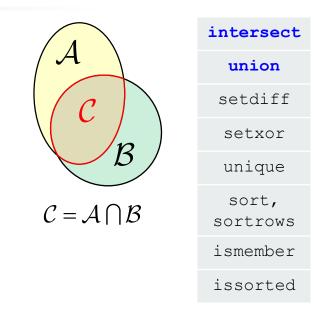
intersection of two sets	intersect
union of two sets	union
difference of two sets	setdiff
exclusive OR of two sets	setxor
unique values in a set	unique
sorting, row sorting	sort, sortrows
is the element member of a set?	ismember
is the set sorted?	issorted



# Set operations #1

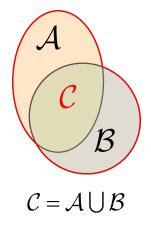
- intersection of sets: intersect
  - example: intersection of a matrix and a vector:

```
>> A = [1 -1; 3 4; 0 2];
>> b = [0 3 -1 5 7];
>> c = intersect(A, b)
% c = [-1; 0; 3]
```



- union of sets: union
  - all set operations can be carried out row-wise (in that case the number of columns has to be observed)

```
>> A = [1 2 3; 4 5 1; 1 7 1];
>> b = [4 5 1];
>> C = union(A, b, 'rows')
% C = [1 2 3; 1 7 1; 4 5 1]
```

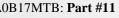




# Set operations #2

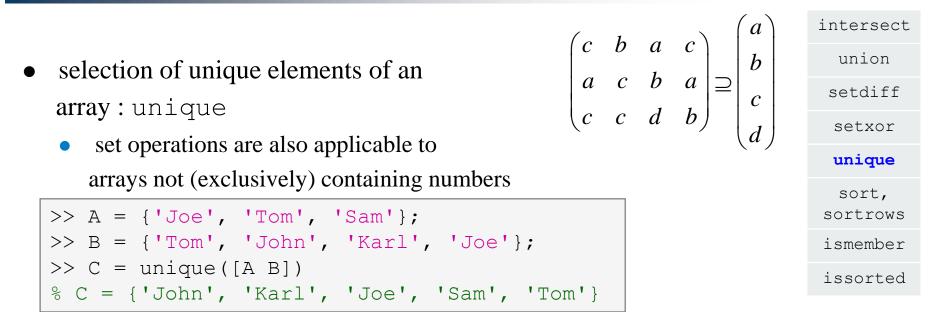
intersect union intersection of a set and complement of setdiff another set: setdiff setxor all set operations return more than one output unique parameter - we get the elements as well as the indexes sort,  $\mathcal{C} = \mathcal{A} \cap \mathcal{B}^{\mathcal{C}} = \mathcal{A} \setminus \mathcal{B}$ >>  $A = [1 \ 1; 3 \ NaN];$ sortrows >> B = [2 3; 0 1];ismember >> [C, ai] = setdiff(A,B) issorted % C = NaN, ai = 4% i.e.: C = A(ai) exclusive intersection (XOR): setxor all set operations can be carried out either as 'stable' (not changing the order of elements) or as '*sorted*' (elements are sorted)  $>> A = [5 \ 1 \ 0 \ 4];$ >> B =  $[1 \ 3 \ 5];$ >> [C, ia, ib] = setxor(A, B, 'stable')  $\mathcal{C} = \mathcal{A} \oplus \mathcal{B}$ % C = [0 4 3], ia = [3; 4], ib = [2]A0B17MTB: Part #11

5





# **Set operations #3**



- it is possible to combine all above mentioned techniques
  - e.g. row-wise listing of unique elements of a matrix including indexes:

```
>> A = round(rand(10, 3)).*mod(10:-1:1, 3)'
>> [C, ai, ci] = unique(sum(A, 2), 'rows', 'stable')
```

• Interpret the meaning of the above code? Is the 'rows' parameter necessary?



# Set operations #1

Operators

600 s

- consider three vectors **a**, **b**, **c** containing natural numbers  $x \in \mathbb{N}$  so that
  - vector **a** contains all primes up to (and including) 1000
  - vector **b** contains all even numbers up to (and including) 1000
  - vector **c** is complement of **b** in the same interval
- $\mathbf{v} = \mathbf{a} \cap (\mathbf{b} + \mathbf{c}), \qquad \mathbf{b} + \mathbf{c} \equiv \{b_i + c_i\}, \quad i \in \{1, 500\}$ find vector **v** so that  $b_{i-1} < b_i < b_{i+1} \land c_{i-1} < c_i < c_{i+1}, \forall i$ what elements does v contain? v = how many elements are there in v? Columns 1 through 24 23 31 3 11 19 43 47 59 71 79 67 Columns 25 through 48 211 223 239 251 263 347 Columns 49 through 72 491 503 523 547 563 571607 619 631 Columns 73 through 87 823 967



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### **Set operations #2**

Operators

500 s

• estimate the result of following operation (and verify using Matlab):

 $\mathbf{w} = \begin{pmatrix} \mathbf{b} \ \bigcup \ \mathbf{c} \end{pmatrix} \setminus \mathbf{a}$ 

• what is specific about elements of the resulting vector **w**?

• with the help of logical indexing and mathematical functions determine how many elements of **w** are divisible by 3



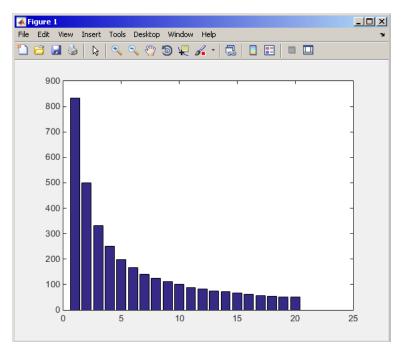
#### 500 s

- **Set operations #3** 
  - write previous exercise as a script:

- modify the script in the way to calculate how many elements of **w** are divisible by numbers 1 to 20
  - use for instance for loop to get the result
  - plot the results using bar function



#### **Set operations #4**





17.12.2018 13:29

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10

- **Set operations #5**
- Radio relay link operates at frequency of 80 GHz at 20 km distance with 64-QAM modulation
  - phase stability of  $\pm 0.5^{\circ}$  is required for sufficiently low bit error rate without using synchronization and coding
  - that corresponds to the change of distance between antennas equal to  $\pm 5 \ \mu m$
  - the statistics of link distance with normal distribution containing  $1 \cdot 10^6$  elements can be generated as:

```
L = 20e3; % length of path
deviation = 5e-6; % standard deviation
N = 1e6; % number of trials
% random distances
distances = L + randn(1, N)*deviation;
```

- How many times is the distance L contained in the vector distances?
- How many unique elements are there in distances?
- Can the distribution be considered continuous?



intersect

# Array sorting #1

- sort array elements
  - column-wise, in ascending order:
  - row-wise, in ascending order :
  - in descending order:

• in descending order, row-wise:

>> sort(A, 2, 'descend')

• apply the sorting function, to following matrices (for instance):

>> A = reshape([magic(3) magic(3)'], [3 3 2])
>> B = 'for that purpose';



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# **Array sorting #2**

		interse
function sortro	ows sorts rows of a matrix	union
	e rows are not swapped - rows are sorted as blocks	setdif
	rows are not swapped nows are soliced as blocks	setxo
	$\begin{pmatrix} 8 & 1 & 6 \end{pmatrix}$	unique
		sort, sortro
	$\begin{pmatrix} 4 & 9 & 2 \end{pmatrix}$	ismembe
SORT:	$ \begin{pmatrix} 3 & 1 & 2 \\ 4 & 5 & 6 \\ 8 & 9 & 7 \end{pmatrix} $	issorte
SORTROWS:	(3       5       7)         4       9       2         8       1       6	





# is\* functions related to sets

	intersect
• function issorted returns true if array is sorted	union
j	setdiff
	setxor
	unique
• function ismember (A, B) tests whether an element of	sort, sortrows
array B is also an element of array A	ismember
array D is also an ciclicit of array A	issorted

>> ismember([1 2 3; 4 5 6; 7 8 9], [0 0 1; 2 1 4])

>> ismember([1 2 3; 4 5 6; 7 8 9], [0 0 1; 2 1 4])

ans =

1	1	0
1	0	0
0	0	0

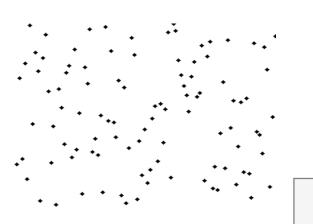


# **Array sorting**

Operators

600 s

- try to write your own sorting algorithm bubbleSort.m
  - use the *bubble sort* algorithm
  - use the function issorted to test whether the resulting array is sorted



if you wish, you can use the following code inside loops :

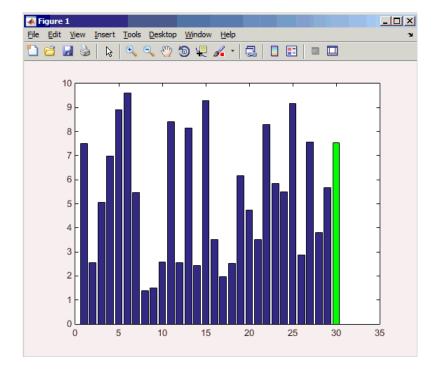
figure(1);
plot(R,'\*','LineWidth',2);
pause(0.01);

wikipedia.org

sort(R)

600 s

• try to get plot as in the figure using bar function:



**Array sorting** 

17.12.2018 13:29

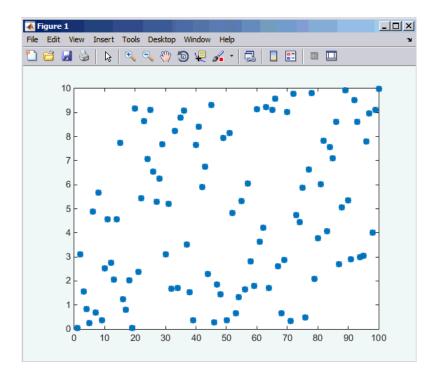
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16

# Array sorting – shaker sort

600 s

- try to write your own sorting algorithm shakerSort.m
  - use the *shaker sort* algorithm





17.12.2018 13:29

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17

# Searching in an array - find

- find function is a very useful one!!
- returns positions of non-zero (logical true) elements of a matrix
  - useful for searching in an array of logical values
  - example: find positions of those elements of vector  $\mathbf{A} = \begin{pmatrix} \frac{\pi}{2} & \pi & \frac{3}{2}\pi & 2\pi \end{pmatrix}$  fulfilling the condition  $\mathbf{A} > \pi$

>> A = pi/2\*(1:4) >> find(A > pi)

- compare the above command with A > pi. What is the difference?
- function find can also search a square matrix etc.
- to find first / last k non-zero elements of X:

```
>> ind = find(X, k, 'first')
>> ind = find(X, k, 'last')
```

• for more see >> doc find



# Array searching #1

420 s

• sort the vector  $\mathbf{v} = (16 \ 2 \ 3 \ 13 \ 5 \ 11 \ 10 \ 8 \ 9 \ 7 \ 6 \ 12 \ 4 \ 14 \ 15 \ 1)$ in descending order and find the elements of the vector (and their respective positions within the vector) that are divisible by three and at the same time are greater than 10

>> v = reshape(magic(4)', [1 numel(magic(4))])

v =																			
	16	2	3	13	5	11	10	8	9	7	6	12	4	14	15	1			
v1 :	=																		
	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0			
ans	=																		
	15	12																	
ans	=																		
	2	5																	
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# **Array searching #2**

300 s

• in matrix **w** 

>> 
$$w = (8:-1:2) ' * (1:1/2:4) . * magic(7)$$

find last 3 values that are smaller than 50

• find out the column and row positions of the values

ToT 3	=
-------	---

240.0000	468.0000	768.0000	20.0000	240.0000	532.0000	896.0000
266.0000	493.5000	98.0000	157.5000	378.0000	661.5000	812.0000
276.0000	54.0000	96.0000	255.0000	468.0000	735.0000	888.0000
25.0000	105.0000	160.0000	312.5000	510.0000	630.0000	900.0000
52.0000	90.0000	192.0000	330.0000	504.0000	616.0000	64.0000
63.0000	103.5000	192.0000	307.5000	387.0000	31.5000	144.0000
44.0000	93.0000	160.0000	245.0000	12.0000	77.0000	160.0000



# Application of the find function

600 s

• Samples of demodulated signal of a radio receiver can be approximated as :

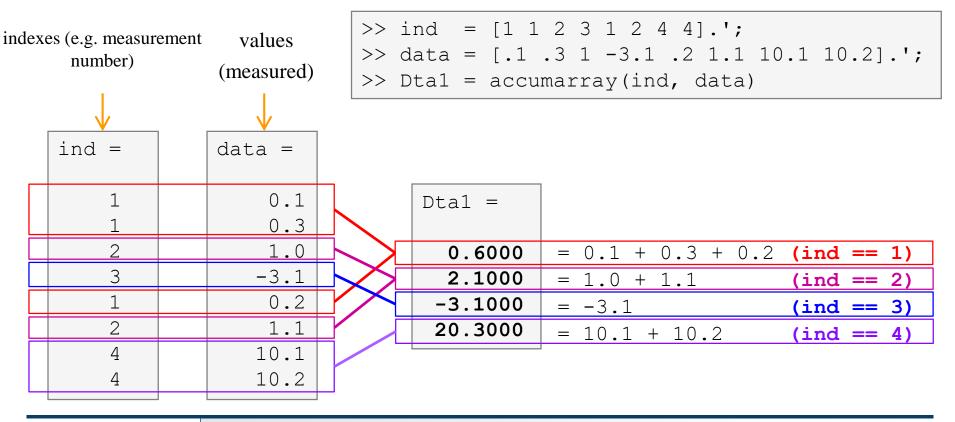
```
w = 0.6833; t = 1:10; % time
samples = 2.7 + 0.5*(cos(w*t) - sin(w*t) - cos(2*w*t) + sin(2*w*t) ...
        - cos(3*w*t) + 3*sin(3*w*t) + 2*cos(4*w*t) + 4*sin(4*w*t));
plot(samples, '*')
```

• Voltage corresponding to characters are within  $\pm 0.5$  V tolerance

• Decipher the message!	Voltage [V]	Character
	1	а
<pre>chars = 'acdgmrs'; volts = 1:7;</pre>	2	С
<pre>message = blanks(length(samples));</pre>	3	d
for iVolt = volts	4	0
logCondition = samples > (iVolt - 0.5) &	+	g
<pre>samples &lt; (iVolt + 0.5);</pre>	5	m
<pre>indices = find(logCondition);</pre>	6	r
<pre>message(indices) = chars(iVolt);</pre>	_	
end	7	S
disp(message)		

# Function accumarray #1

- the function accumarray is able to group data with the same index
  - not a very well known function, but an exceptionally useful one
- quite often we deal with a dataset that is organised in the following way:



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# Function accumarray #2

- basic operation applicable to data from one 'box' (data with the same index) is summation
- any other function can be applied, however
  - e.g. maximum of a set of elements with the same index
  - we use the max function

>> Dta2 = accumarray(ind, data, [], @max)

- e.g. listing of all elements with the same index
- we use so called handle function and cell data type

>> Dta3 = accumarray(ind, data, [],  $Q(x) \{x\}$ )

Dta2 =
0.3000
1.1000
-3.1000
10.2000

Dta3 =	=
[3x1	double]
[2x1	double]
[ -	-3.1000]
[2x1	double]



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# Function accumarray #3

- the function has a wide variety of other features
- it is possible, for instance, to use 2D indexation of results
  - the results are not put in a 1D set of 'boxes' but to a 2D array instead

>> ind = [1 1;2 2;1 2;1 3;1 1;3 1];

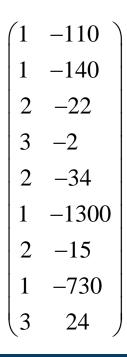
			[10 22 12 13 1 accumarray(ind,	
ind =	data =	ind == [1 1]	ind == [1 2]	ind == [1 3]
		10 + 1 = 11	12	13
1 1 2 2	10 22	ind == [2 1]	ind == [2 2]	ind == [2 3]
1 2 1 3	12 13	0	22	0
$\begin{array}{ccc} 1 & 3 \\ 1 & 1 \end{array}$	13	ind == [3 1]	ind == [3 2]	ind == [3 3]
3 1	pi	pi	0	0



# Function accumarray

300 s

- account transfers in CZK, EUR a USD are as follows
  - (CZK ~ 1, EUR ~ 2, USD ~ 3)
- find out account balance in each currency
  - the exchange rate is  $26 \text{ CZK} = 1 \text{\ensuremath{\in}}$ ,  $25 \text{ CZK} = 1 \text{\ensuremath{\notin}}$ , find out total balance



>> dta = [1 -110; 1 -140; 2 -22; 3 -2; ... 2 -34; 1 -1300; 2 -15; 1 -730; 3 24] >> K = [1 26 25]



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17.12.2018 13:29

# **Discussed functions**

intersect	intersection of sets (vectors / matrices)
union	intersection of sets (vectors / matrices)
setdiff	Subtraction of sets (intersection of a set and complement of another set)
setxor	exclusive intersection
unique	selection of unique elements of an array
sort	sort vector/matrix elements
sortrows	sorts rows of a matrix as a whole
accumarray	group data •
ismember	is given element is member of array?
issorted	is array sorted?
find	find elements fulfilling given condition



17.12.2018 13:29

. . . . . .

- measurement of temperature was carried out in the course of 5 days every second clock hour. Data was measured at 3 different sites (A, B, C)
- find out average daily temperature in given week for all 3 sites
  - i.e., get mean value of measurement at the same hour on the same site

- generate the data using temperature\_measurement.m
  - see the script on the following slide
  - see the variables required



#### Exercise #2

script for data generation

and the results ...

```
clear; close all; clc;
%% allocation
days = 5; hours = 12;
TimeA = zeros(days*hours,1);
TimeB = TimeA;
TimeC = TimeA:
%% creation of time data-set
for kDay = 1:days
    TimeA((hours*(kDay-1)+1):(hours*(kDay-1)+12),1) = 2*(randperm(12)-1)';
    TimeB((hours*(kDay-1)+1):(hours*(kDay-1)+12),1) = 2*(randperm(12)-1)';
    TimeC((hours*(kDay-1)+1):(hours*(kDay-1)+12),1) = 2*(randperm(12)-1)';
end
%% place and tempreture data-sets
PlaceA = abs(abs(TimeA - 11) - 10) + 10 + 5.0*rand(size(TimeA,1),1);
PlaceB = abs(abs(TimeB - 12) - 10) + 5 + 10.0*rand(size(TimeB, 1), 1);
PlaceC = abs(abs(TimeC - 11) - 11) + 5 + 7.5*rand(size(TimeC, 1), 1);
%% generating final variables for the example
TimeAndPlace = [TimeA/2+1 ones(size(TimeA,1),1);...
                TimeB/2+1 2*ones(size(TimeA,1),1);...
                TimeC/2+1 3*ones(size(TimeA, 1), 1)];
MeasuredData = [PlaceA; PlaceB; PlaceC];
%% plot final data-set
plot(TimeA, PlaceA, 'LineWidth', 1, 'LineStyle', 'none', 'Marker', 'x',...
    'MarkerSize',15); hold on;
plot(TimeB, PlaceB, 'LineWidth', 1, 'LineStyle', 'none', 'Marker', '*',...
    'MarkerSize', 15, 'Color', 'r');
plot(TimeC, PlaceC, 'LineWidth', 2, 'LineStyle', 'none', 'Marker', 'o',...
    'MarkerSize',10,'Color','g');
set(qcf,'Color','w','pos',[50 50 1000 600]); set(qca,'FontSize',15);
xlabel('time','FontSize',15); ylabel('Temperature','FontSize',15);
title('Measured Data'); grid on; legend('Place A', 'Place B', 'Place C');
```



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#### **Exercise #3**

- all the data are contained in 2 matrices:
  - TimeAndPlace (5×3×12,2) = (180,2)
  - MeasuredData  $(5 \times 3 \times 12, 1) = (180, 1)$

number of days

number of measurement sites

number of measurements per day

• unfortunately, data in TimeAndPlace are intentionally unsorted

<b>INDEXES:</b>	TimeAndPlace =	MeasuredData =	DATA:
tindex = $10$ , Place = $1$	10 1	15.0797	T(10,1) = 15.0797 °C
	4 1	18.9739	
	7 1	19.3836	
	12 2	9.9506	
tindex = 6, Place = $2$	6 2	19.7588	T(6,2) = 19.7588 °C
	••••	•••	
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#### **Exercise #4**

- following holds true
  - Place1 ~ measurement site A
  - Place2 ~ measurement site B
  - Place3 ~ measurement site C
  - measurement hour = 2\*(tindex-1)
- now try to place your code in the script to carry out the averaging and plot the data in the existing figure

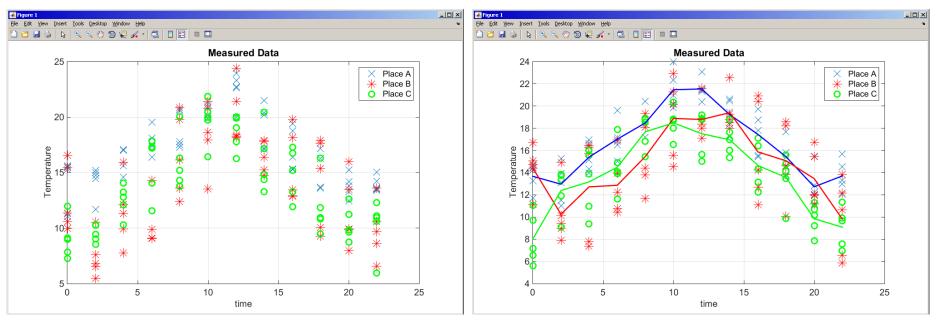




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measured and averaged data

measured data



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31

# Thank you!

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