#### Parsimony-Based Approaches to Inferring Phylogenetic Trees

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 there are various trees that could explain the phylogeny of the sequences AAG, AAA, GGA, AGA including these two:



• parsimony prefers the first tree because it requires fewer substitution events

## Parsimony based approaches usually these approaches involve two separate components a procedure to find the minimum number of changes needed to explain the data (for a given tree topology) a search through the space of trees

## Finding minimum number of changes for a given tree

- basic assumptions
  - any state (e.g. nucleotide, amino acid) can convert to any other state
  - the "costs" of these changes are uniform
  - positions are independent; we can compute the min number of changes for each position separately

## Finding minimum number of changes for a given tree

- brute force approach
  - for each possible assignment of states to the internal nodes, calculate the number of changes
  - report the min number of changes found
- runtime is  $O(Nk^N)$ 
  - k = number of possible character states (4 for DNA)
  - N = number of leaves

#### Fitch's Algorithm [1971]

- traverse tree from leaves to root <u>determining set of</u> <u>possible states</u> (e.g. nucleotides) for each internal node
- 2. traverse tree from root to leaves <u>picking ancestral</u> <u>states</u> for internal nodes

### Fitch's algorithm: Step 1 possible states for internal nodes

- do a post-order (from leaves to root) traversal of tree
- determine possible states  $R_i$  of internal node *i* with children *j* and *k*

$$R_{i} = \begin{cases} R_{j} \cup R_{k}, & \text{if } R_{j} \cap R_{k} = \emptyset \\ R_{j} \cap R_{k}, & \text{otherwise} \end{cases}$$

 this step calculates the number of changes required # of changes = # union operations



## Fitch's algorithm: step 2 select states for internal nodes

- do a pre-order (from root to leaves) traversal of tree
- select state  $r_j$  of internal node j with parent i

$$r_{j} = \begin{cases} r_{i}, \text{ if } r_{i} \in \mathbb{R}_{j} \\ \text{arbitrary state} \in R_{j}, \text{ otherwise} \end{cases}$$



#### Weighted parsimony

- [Sankoff & Cedergren, 1983]
- instead of assuming all state changes are equally likely, use different costs S(a,b) for different changes
- 1st step of algorithm is to propagate costs up through tree
   a → b

#### Weighted parsimony

- want to determine cost R<sub>i</sub>(a) of assigning character a to node i
- for leaves:

$$R_i(a) = \begin{cases} 0, & \text{if } a \text{ is character at leaf} \\ \infty, & \text{otherwise} \end{cases}$$

#### Weighted parsimony







#### Weighted parsimony example

Consider the two simple phylogenetic trees shown below, and the symmetric cost matrix for assessing nucleotide changes. The tree on the right has a cost of 0.8



	a	с	g	t
a	0	0.8	0.2	0.9
c	0.8	0	0.7	0.5
g	0.2	0.7	0	0.1
Ţ	0.9	0.5	0.1	0

Show how the <u>weighted</u> version of parsimony would determine the cost of the tree on the left.

What are the minimal cost characters for the internal nodes in the tree on the left?

Which of the two trees would the maximum parsimony approach prefer?

#### Weighted Parsimony Example



	a	с	g	t
a	0	0.8	0.2	0.9
с	0.8	0	0.7	0.5
g	0.2	0.7	0	0.1
t	0.9	0.5	0.1	0

$$\begin{split} R_1(a) &= 0.9 + \min\{0.8, 0.8 + 0.8, 0.2 + 0.9, 0.9 + 1.4\} = 1.7\\ R_1(c) &= 0.5 + \min\{0.8 + 0.8, 0.8, 0.7 + 0.9, 0.5 + 1.4\} = 1.3\\ R_1(g) &= 0.1 + \min\{0.2 + 0.8, 0.7 + 0.8, 0.9, 0.1 + 1.4\} = 1.0\\ R_1(t) &= 0 + \min\{0.9 + 0.8, 0.5 + 0.8, 0.1 + 0.9, 1.4\} = 1.0 \end{split}$$

The minimal cost characters for node 1 are either  $\mathbf{g}$  or  $\mathbf{t}$ . The minimal cost character for node 3 is  $\mathbf{g}$ . The maximum parsimony approach would prefer the other tree (exercise left to the reader).

# Exploring the space of trees we've considered how to find the minimum number of changes for a given tree topology need some search procedure for exploring the space of tree topologies



#### Heuristic method: hill-climbing with nearest neighbor interchange

given: set of leaves *L* create an initial tree *t* incorporating all leaves in *L best-score* = parsimony algorithm applied to *t* repeat

for each internal edge e in t

for each nearest neighbor interchange

 $t' \leftarrow$  tree with interchange applied to edge e in t

*score* = parsimony algorithm applied to *t*'

if score < best-score

best-score = score
best-tree = t'

*t* = *best-tree* until stopping criteria met



#### Exact method: branch and bound

given: set of leaves L initialize Q with a partial tree with 3 leaves from L repeat  $t \leftarrow \text{ tree in } Q \text{ with lowest lower bound}$ if t has incorporated all leaves in L return t else create new trees by adding next leaf from L to each branch of t compute lower bound for each tree put trees in Q sorted by lower bound

#### Branch and bound (alternate version)

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given: set of leaves L

use heuristic method to grow initial tree t'

initialize Q with a partial tree with 3 leaves from L

repeat

t \leftarrow \text{ tree in } Q \text{ with lowest lower bound}

if t has incorporated all leaves in L

return t

else

create new trees by adding next leaf from L to each branch of t

for each new tree n

if lower-bound(n) < score(t')

put n in Q sorted by lower bound
```

#### Rooted or unrooted trees for parsimony?

- we described parsimony calculations in terms of rooted trees
- but we described the search procedures in terms of unrooted trees
- unweighted parsimony: minimum cost is independent of where root is located
- weighted parsimony: minimum cost is independent of root if substitution cost is a metric (refer back to definition of metric from distance-based methods)

#### Comments on branch and bound

- it is a *complete* search method
  - guaranteed to find optimal solution
- may be much more efficient than exhaustive search
- in the worst case, it is no better
- efficiency depends
  - the tightness of the lower bound
  - the quality of the initial tree

#### Comments on tree inference

- search space may be large, but
  - can find the optimal tree efficiently in some cases
  - heuristic methods can be applied
- difficult to evaluate inferred phylogenies: ground truth not usually known
  - can look at agreement across different sources of evidence
  - can look at repeatability across subsamples of the data
  - can look at indirect predictions, e.g. conservation of sites in proteins
- some newer methods use data based on linear order of orthologous genes along chromosome
- phylogenies for bacteria, viruses not so straightforward because of *lateral transfer* of genetic material; "local" phylogenies might be more appropriate



#### Identifying functional regions in proteins

- we want to estimate the rate *r* for each position
- · consider a four-sequence example





#### Identifying functional region in proteins



**Fig. 2.** The peptide-binding groove of the SH2 domain. The structure of the SH2 domain in complex with the C-tail of the tyrosine kinase domain (PDB entry 1fmk, Xu *et al.*, 1997) and MSA of 233 homologues were used. The conservation pattern obtained using MP-ConSurf (**A**) and Rate4Site (**B**) is color-coded onto the molecular surface of the domain: dark violet corresponds to maximal conservation, white corresponds to average conservation level and dark turquoise to maximal variability. The peptide is shown as a balls-and-sticks model with a yellow tube tracing its backbone. The picture was drawn using GRASP (Nicholls *et al.*, 1991). The domain boundaries were set to Trp148 to Pro246 (Al-Lazikani *et al.*, 2001).

