Nuclear imaging Positron Emission Tomography (PET), Single-Photon Emission Computed Tomography (SPECT)

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Resources

- http://www.bic.mni.mcgill.ca/~louis/seminars/399-650/pet.html
- http://ocw.mit.edu/NR/rdonlyres/Nuclear-Engineering/ 22-01Introduction-to-Ionizing-RadiationFall2003/ 60AA5867-88AE-49C7-9478-2F4661B4EBBE/0/pet_spect.pdf

http:

//www.pet.mc.duke.edu/rsna04/turk-petspectphysicsRSNA2005.pdf

- http://www.nuclear.kth.se/courses/medphys/5A1414/TOFPET1.pdf
- http://www.fmri.org,
- A. Webb: Introduction to Biomedical Imaging
- images by: Wikipedia, NIH, Moazemi et al., Rager et al., Virginia Commonwealth University...

Principles of nuclear imaging

Radioactivity

Gamma camera

SPECT

PET

Conclusions



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Gamma

Camera

Detector

X-ray and CT

transmission imaging, external source

▶ PET, SPECT

emission imaging, source internal to body

► X-ray and CT

- transmission imaging, external source
- Anatomic imaging (shape, fracture)

PET, SPECT

- *emission* imaging, source internal to body
- Functional imaging (metabolism, perfusion), tracer concentration

► X-ray and CT

- transmission imaging, external source
- Anatomic imaging (shape, fracture)
- X-rays

PET, SPECT

- *emission* imaging, source internal to body
- Functional imaging (metabolism, perfusion), tracer concentration
- $\blacktriangleright \gamma$ rays

► X-ray and CT

- transmission imaging, external source
- Anatomic imaging (shape, fracture)
- X-rays
- Good resolution, $< 1 \, \text{mm}$

PET, SPECT

- *emission* imaging, source internal to body
- Functional imaging (metabolism, perfusion), tracer concentration
- $\blacktriangleright \gamma$ rays
- Lower resolution, 5 \sim 20 mm



Hand, osteoarthritis, CT+SPECT



Heart, myocardial perfusion, PET



Brain, FDG PET, metabolism



Renal (kidney) PET+CT, Ga-PSMA contrast agent.



Metastases, SPECT+CT, MIP

Principles of nuclear imaging

Radioactivity

Radioactive decay

Radionuclide production Cyklotron Radiopharmaceuticals

Gamma camera

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Radioactivity

- element = same number of protons
- isotope/nuclide = same number of protons and neutrons
- \blacktriangleright excess of neutrons/protons \rightarrow instability \rightarrow radioactive decay chain \rightarrow stable isotope

Valley of stability



Isotopes with Z slightly smaller than N are stable.

Radioactive decay modes

Unstable parent nucleus \rightarrow Daughter nucleus + particles (energy)

- Alpha decay (α)
- Beta decay (β)
- ▶ Positron decay (β⁺)
- Isomeric transition
- Electron capture
- Proton emission, neutron emission, ...

Alpha decay

• Spontaneous emission of α particles

- > 2 protons + 2 neutrons, ${}^{4}_{2}$ He, charged
- energy 4 \sim 8 MeV, speed 0.05c
- **>** strong interaction, low penetration (cm in air, μ m in tissue), easy shielding
- important biological effects (relative biological effectiveness 20), DNA damage
- no use in imaging, used in therapy
- happens in heavy nuclei and Be

excess energy released as γ (electromagnetic) rays (photons)



Decay chain



Beta decay

- $\blacktriangleright \beta$ particles = electrons e⁻
- Neutron conversion

$$n \xrightarrow{\beta} p + e^- + \bar{\nu}_e$$

 $\bar{\nu}_e$ — electron antineutrino

$${}^{A}_{Z}X \xrightarrow{\beta} {}^{A}_{Z+1}Y + e^{-} + \bar{\nu_{e}}$$

- For neutron-rich (N > Z) isotopes
- ▶ e⁻ ejected with high energy (β rays), continuous spectrum
- ▶ remaining energy = $\bar{\nu_e}$, nucleus recoil
- \blacktriangleright excited state nucleus $\longrightarrow \gamma$ rays

Beta decay

Examples

$$\begin{array}{l} {}^{14}_{6}C \xrightarrow{\beta} {}^{14}_{7}N + e^{-} + \bar{\nu_{e}} & \mbox{half-life 5730 years} \\ {}^{99}_{42}Mo \xrightarrow{\beta} {}^{99m}_{43}Tc + e^{-} + \bar{\nu_{e}} & \mbox{half-life 2.7 days} \end{array}$$

Isomeric transition

Excited state nucleus $\longrightarrow \gamma$ rays

Metastable **Technetium** $^{99m}_{43}$ Tc

$${}^{99m}_{43}$$
Tc ${}^{\gamma}_{
m H} {}^{99}_{43}$ Tc

half-life 6 h

Isomeric transition

Excited state nucleus $\longrightarrow \gamma$ rays

Metastable **Technetium** $^{99m}_{43}$ Tc

$$\begin{array}{ll} {}^{98}_{42}\text{Mo} \longrightarrow {}^{99}_{42}\text{Mo} & \text{neutron bombardment} \\ {}^{99}_{42}\text{Mo} \xrightarrow{\beta} {}^{99m}_{43}\text{Tc} + e^- + \bar{\nu_e} & \text{half-life 2.7 days} \end{array}$$

▶ γ (photon) energy 140 keV

Multiple decay processes

lodine



Positron decay β^+ decay

•
$$\beta^+$$
 particles = positrons e⁺

$$p \xrightarrow{\beta^+} n + e^+ + \nu_e$$

 ν_e — electron neutrino

$${}^{A}_{Z}X \xrightarrow{\beta} {}^{A}_{Z-1}Y + e^{+} + \nu_{e}$$

For proton-rich (N < Z) isotopes

Positron decay β^+ decay

Examples

Positron decay



two photons with energy 511 keV

 \blacktriangleright Parent/daughter nuclide energy difference $\gtrsim 1\,{
m MeV}$

Electron capture

Proton absorbs inner electron

$$p + e^{-} \xrightarrow{EC} n + \nu_e$$

 ${}^{A}_{Z}X + e^{-} \xrightarrow{EC} {}^{A}_{Z-1}Y + \nu_e$

Example:



- Neutrino carries all energy (characteristic spectrum)
- Can occurr for smaller energy differences
- \blacktriangleright Excited state nucleus $\longrightarrow \gamma$ rays

Decay mode chart



black: stable, light blue: β , green: β^+ or electron capture, orange: α , dark blue: fission, red: neutron emission, brown: proton emission

Nuclear imaging methods

SPECT

- \triangleright γ camera (2D)
- single photon emission computed tomography (3D)
- $\blacktriangleright~\gamma$ photon emitters

PET

- positron emission tomography (3D)
- positron emitters

Ideal radionuclides for SPECT imaging

- Physical half-life long enough to allow preparation
- Physical half-life short enough to minimize long-term effects
- Pure γ emitter (isomeric transition, electron capture)
- Photon energy high-enough to penetrate tissue
- Photon energy low-enough for efficient shielding and detection

Single photon emitters

for SPECT nuclear imaging

Nuclide		Half-life	E _{photon} [keV]	
Technetium	⁹⁹ 77c	6 h	140	most used
lodine	$^{123}_{53}$ I	13 h	159	thyroid imaging
Indium	$^{111}_{53}$ ln	2.8 d	171, 245	good, expensive
Thallium	$^{201}_{81}$ TI	3 d	$70\sim 80$	cardiac perfussion
Gallium	$^{67}_{31}$ Ga	3.25 d	$90 \sim 400$	tumor localization
lodine	$\frac{131}{53}$	8.1 d	$364\sim 606$	radiotherapy

Positron emitters for PET nuclear imaging

Nuclide		Half-life	
Rubidium	$^{82}_{37}$ Rb	1.3 min	cardiac imaging
Oxygen	$^{15}_{8}O$	2 min	
Nitrogen	${}^{13}_{7}N$	10 min	
Carbon	${}_{6}^{11}C$	20.3 min	
Gallium	$_{31}^{68}$ Ga	68 min	tumor localization
Fluorine	¹⁸ ₉ F	110 min	most often used, FDG
Copper	⁶⁴ 35Cu	12.7 h	oncology, radiotherapy

Mostly short half-time — need to be produced in-situ.

Activity

- Activity A[Bq], 1 Bq = 1 desintegration/s,
- $\blacktriangleright\,$ Older unit $1\,\text{Ci}=3.7\cdot10^{10}\,\text{Bq}-1\,\text{g}$ of radium

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For N nuclei and a decay constant λ

$$A = \lambda N = -\frac{\mathrm{d}N}{\mathrm{d}t}$$

Exponential decay

Exponential decay of N

$$N = N_0 e^{-\lambda t}$$
Exponential decay

Exponential decay of N

$$N = N_0 \mathrm{e}^{-\lambda t}$$

► Half-life

$$egin{aligned} \mathcal{T}_{1/2} &= \log 2/\lambda pprox 0.693/\lambda \; [s] \ \mathcal{N} &= \mathcal{N}_0 \left(rac{1}{2}
ight)^{rac{t}{T_{1/2}}} \end{aligned}$$

Exponential decay

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Exponential decay of A

$$A = A_0 e^{-\lambda t}$$
, with $A_0 = \lambda N_0$, $A = \lambda N$

Effective half-life

- ▶ Physical half-life T_p
- ► Biological half-life T_b
- Effective half-life T_e

$$\frac{1}{T_e} = \frac{1}{T_p} + \frac{1}{T_b}$$

Effective half-life

- ▶ Physical half-life T_p
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- Effective half-life T_e

$$\frac{1}{T_e} = \frac{1}{T_p} + \frac{1}{T_b}$$

Note: $T_e < T_p$, $T_e < T_b$

Effective Half-Life

E.g., for an isotope with a 6-hr half life attached to various carrier molecules with different biological half-lives.

T _P	Т _в	Τ _Ε	
6 hr	1 hr	0.86 hr	
6 hr	6 hr	3 hr	
6 hr	60 hr	5.5 hr	
6 hr	600 hr	5.9 hr	

Effective Half-Life

Assume 10⁶ Bq localized in a tumor site, vary T

Nuclide	Half-life (T)	λ (sec ⁻¹)	N
1	6 sec	0.115	8.7 x 10 ⁷
2	6 min	1.75 x 10 ⁻³	5.7 x 10 ⁹
3	6 hrs	3.2 x 10 ⁻⁵	3.1 x 10 ¹¹
4	6 days	1.3 x 10 ⁻⁶	7.7 x 10 ¹²
5	6 years	4 x 10 ⁻⁹	2.5 x 10 ¹⁵

Effective Half-Life

Assume 10¹⁰ atoms of radionuclide localized in a tumor site, vary T

Nuclide	Half-life (T)	λ (sec ⁻¹)	Activity (Bq)
1	6 sec	0.115	1.15 x 10 ⁹
2	6 min	1.75 x 10 ⁻³	1.7 x 10 ⁷
3	6 hrs	3.2 x 10 ⁻⁵	3.2 x 10 ⁶
4	6 days	1.3 x 10 ⁻⁶	1.3 x 10 ⁴
5	6 years	4 x 10 ⁻⁹	40

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Radioactive decay Radionuclide production

Cyklotron Radiopharmaceuticals

Gamma camera

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Conclusions

Radionuclide production

Neutron capture

- Nuclear fission
- Radionuclide generator
- (Poisitive) ion bombardment
 - Linear accelerator
 - Cyclotron

Neutron capture

Neutron activation/neutron bombardment

- $\blacktriangleright\,$ Nuclear reactor, "thermal" neutrons, low energy 0.03 $\sim 100\,\text{eV}$
- ▶ Yield depends on neutron flow ϕ , cross section σ , decay constant λ , amount of carrier (source) material
- Chemical/physical purification

Neutron capture

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- $\blacktriangleright\,$ Nuclear reactor, "thermal" neutrons, low energy 0.03 $\sim 100\,\text{eV}$
- ▶ Yield depends on neutron flow ϕ , cross section σ , decay constant λ , amount of carrier (source) material
- Chemical/physical purification

$$\mathsf{n} + {}^{98}_{42}\mathsf{Mo} \longrightarrow {}^{99}_{42}\mathsf{Mo} + \gamma$$

with proton emission

$$n + {}^{32}_{16}S \longrightarrow {}^{32}_{15}P + p$$
 half-life 14 days

Radionuclides produced by neutron capture

Radionuclide	Production Reaction	Gamma-Ray Energy (keV)	Half-Life	σ (Barn)
⁵¹ Cr	${}^{50}\mathrm{Cr}(\mathrm{n},\gamma){}^{51}\mathrm{Cr}$	320	27.7 days	15.8
⁵⁹ Fe	⁵⁸ Fe(n, γ) ⁵⁹ Fe	1099	44.5 days	1.28
⁹⁹ Mo	⁹⁸ Mo(n, γ) ⁹⁹ Mo	740	66.02h	0.13
$^{131}\mathrm{I}$	$^{130}\text{Te}(n, \gamma) \ ^{131}\text{Te} \rightarrow \ ^{131}\text{I}$	364	8.04 days	0.29

Radionuclides produced by neutron absorption.

Source: From Mughabghab et al., 1981.

Mostly used for radiotherapy (except ${}^{99}_{42}Mo$)

Nuclear fission

▶ Heavy nuclei $(A > 92) - \frac{235}{92}$ U, $\frac{237}{92}$ U, $\frac{239}{94}$ Pu, $\frac{232}{90}$ Th — irradiated by neutrons \rightarrow unstable

Fission example

$${}^{235}_{92}\mathsf{U} + {}^1_0\mathsf{n} \longrightarrow {}^{99}_{42}\mathsf{Mo} + \underbrace{{}^{133}_{50}\mathsf{Sn}}_{\mathsf{tin}} 4{}^1_0\mathsf{n}$$

Chemical/physical purification

Fission product yield for $^{235}_{92}\text{U}$



Radionuclides produced by nuclear fission

Isotope	Gamma-Ray Energy (keV)	Half-Life	Fission Yield (%)
⁹⁹ Mo	740	66.02h	6.1
131 I	364	8.05 days	2.9
¹³³ Xe	81	5.27 days	6.5
¹³⁷ Cs	662	30 a	5.9

Source: From BRH, 1970.

Radionuclide generator

- Long half-time parent isotope
- Short half-time daughter isotope, $\lambda_2 > \lambda_1$

Radionuclide generator

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- Daughter activity (for $A_{20} = 0$)

$$A_{2} = \frac{\lambda_{2}}{\lambda_{2} - \lambda_{1}} A_{10} \left(e^{-\lambda_{1}t} - e^{-\lambda_{2}t} \right)$$

Radionuclide generator

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$$\mathcal{A}_2 = rac{\lambda_2}{\lambda_2 - \lambda_1} \mathcal{A}_{10} \left(\mathrm{e}^{-\lambda_1 t} - \mathrm{e}^{-\lambda_2 t}
ight)$$

• After $\sim 10 T_{1/2}$, transient equilibrium

$$A_1 = A_{10} \mathrm{e}^{-\lambda_1 t}, \qquad A_2 = A_1 rac{\lambda_1}{\lambda_2 - \lambda_1}$$

Transient equilibrium



 $^{99}_{42}$ Mo/ $^{99m}_{43}$ Tc generator, A_1 , A_2

Technetium generator

- ⁹⁹₄₂Mo produced by fission or neutron bombardment, half-life 67 h
- Adsorbed to alumina Al₂O₃
- ▶ $^{99}_{42}$ Mo $\xrightarrow{\beta}^{99m}_{43}$ Tc (and 15% to $^{99}_{43}$ Tc),
- ▶ ^{99m}₄₃Tc half-life 6 h
- \triangleright ^{99m}₄₃Tc is eluted by physiological saline solution
- \triangleright ^{99m}₄₃Tc can by chemically manipulated
- When unused, the ratio ${}^{99}_{43}\text{Tc}/{}^{99m}_{43}\text{Tc}$ increases

Technetium generator (2)



Radionuclides produced by generators

Parent P	Parent Half-Life	Mode of Decay P → D	Daughter D	Mode of Decay of D	Daughter Half-Life	Daughter γ Energy (keV)
⁶² Zn	9.1h	β⁺ EC	⁶² Cu	β+ EC	9.8 min	511 1173
⁶⁸ Ge	280 days	EC	⁶⁸ Ga	β+ EC	68 min	511 1080
⁸¹ Rb	4.7 h	EC	⁸¹ Kr ^m	IT	13 s	190
⁸² Sr	25 days	EC	⁸² Rb	EC β+	76 s	777 511
⁹⁹ Mo	66.02h	β-	99Tcm	IT	6.02h	140
¹¹³ Sn	115.1 days	EC	¹¹³ In ^m	IT	1.66 h	392
¹⁹⁵ Hg ^m	40 h	IT EC	¹⁹⁵ Au ^m	IT	30.6 s	262

Principles of nuclear imaging

Radioactivity

Radioactive decay Radionuclide production **Cyklotron** Radiopharmaceuticals

Gamma camera

SPECT

PET

Conclusions

Ion bombardment

• Charged particles: mostly $p = \frac{1}{1}H^+$, also $\frac{2}{1}D^+$, $\frac{3}{2}He^{2+}$, $\frac{4}{2}He^{2+}$

- Accelerated to high energies by a linear accelerator or cyclotron (typical $E_p \sim 18 \, {\rm MeV}$)
- hit target, get absorbed in the nucleus, knock out a neutron
- Typical reactions

$$\begin{array}{c} {}^{11}_{5}\mathsf{B} + \mathsf{p} \longrightarrow {}^{11}_{6}\mathsf{C} + \mathsf{n} \\ {}^{68}_{30}\mathsf{Zn} + \mathsf{p} \longrightarrow {}^{67}_{31}\mathsf{Ga} + 2\mathsf{r} \\ {}^{18}_{8}\mathsf{O} + \mathsf{p} \longrightarrow {}^{18}_{9}\mathsf{F} + \mathsf{n} \end{array}$$

• neutron deficit $\longrightarrow \beta^+$ emitters (or EC), mostly short-lived

Radionuclides produced by ion bombardment

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Radionuclide	Principal Gamma-Ray Energy (keV)	Half-Life	Production Reaction
¹¹ C	511 (β+)	20.4 min	$^{14}N(p, \alpha)^{11}C$
^{13}N	511 (β+)	9.96 min	$^{13}C(p, n)^{13}N$
¹⁵ O	511 (β+)	2.07 min	$^{15}N(p, n)^{15}O$
$^{18}\mathrm{F}$	511 (β+)	109.7 min	$^{18}O(p, n)^{18}F$
⁶⁷ Ga	93, 184, 300	78.3 h	⁶⁸ Zn(p, 2n) ⁶⁷ Ga
¹¹¹ In	171, 245	67.9 h	¹¹² Cd(p, 2n) ¹¹¹ In
$^{120}\mathrm{I}$	511 (β+)	81 min	$^{127}I(p, 8n)^{120}Xe \rightarrow ^{120}I$
¹²³ I	159	13.2h	$^{124}\text{Te}(p, 2n)^{123}\text{I}$ $^{127}\text{I}(p, 5n)^{123}\text{Xe} \rightarrow ^{123}\text{I}$
124 I	511 (β+)	4.2 days	¹²⁴ Te(p, n) ¹²⁴ I
²⁰¹ Tl	68–80.3	73 h	203 Tl(p, 3n) 201 Pb $\rightarrow ^{201}$ Tl



▶ Magnetic (Lorentz) force F = qv × B, perpendicular to v and B → circular motion



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• Centripetal=centrifugal force $F = mv^2/r$



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► Magnetic (Lorentz) force F = qv × B, perpendicular to v and B → circular motion

• Centripetal=centrifugal force
$$F = mv^2/r$$

•
$$r = rac{mv}{Ba}$$
, since $v \sim r \sim I \longrightarrow$ constant f

Neglecting relativistic mass increase, electrode shape

Cyclotron



- Vacuum
- ▶ Ion source (batch), mostly H⁻
- Hollow 'D' electrodes, high frequency AC voltage (MHz)
- Magnetic field (oriented vertically)

Cyclotron



- Vacuum
- ▶ Ion source (batch), mostly H⁻

Real cyclotron



Real cyclotron



Carousel



- $\blacktriangleright\,$ after \sim 100s of cycles
- \blacktriangleright H⁻ ion hits a thin carbon foil
- \blacktriangleright \longrightarrow looses electrons, converted $p=\mathrm{H^+}$
- \blacktriangleright \longrightarrow opposite curvature
- Only part of the beam is deviated

Carousel



- after \sim 100s of cycles
- \blacktriangleright ${\rm H}^-$ ion hits a thin carbon foil

Carousel



- \blacktriangleright after \sim 100s of cycles
- \blacktriangleright H⁻ ion hits a thin carbon foil
Target chamber

Reakční komora



Target chamber

Reakční komora



- ▶ $\frac{18}{8}$ O rare (0.2%), enrichment needed (distillation, very small ΔT_{boil})
- Cooling needed (by water)
- Thin cobalt alloy foils (havar)
- Every few hours, ${}_{9}^{18}$ F can be extracted

Target chamber

Reakční komora



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Biosynthesizer



- Radiopharmaceutical radioactively labeled biologically active/compatible chemical compound.
- Quantitative & qualitative imaging of physiological processes.

Principles of nuclear imaging

Radioactivity

Radioactive decay Radionuclide production Cyklotron Radiopharmaceuticals

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Conclusions

Administration, distribution and excretion



Must traverse membranes to get to the targete organ.

Administration of radiopharmaceuticals

- Mostly physiological (saline) solution
- Blood-brain barrier
 - Intravenously administered contrast agent does not get to the brain
 - Contrast agent administered to the cerebro-spinal fluid only gets to the brain and spine.

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- Other metabolic barriers (blood-ocular, blood-air, ...)
- Imaging afinity and metabolism speed

Radiopharmaceutical construction

Radionuclide + carrier molecule (+ probe)



Typical Administered Activity (MBq)

Radionuclide	Pharmaceutical	Indication/Use	Activity (MBq)	
⁶⁷ Ga	Citrate	Tumour imaging, infection/ inflammation imaging	150ª	
⁸¹ Kr ^m	Krypton gas	Lung ventilation imaging	6000ª	
99Tcm	Albumin	Cardiac blood-pool imaging, peripheral vascular imaging	800ª	
99Tcm	Colloids, including tin colloid	Oesophageal transit and reflux	40 ^a	
	and sulphur colloid	Liver imaging	80 ^a , 200 (SPECT) ^a	
		Bone marrow imaging, GI bleeding	400 ^a	
99Tcm	DTPA	Lung ventilation imaging (aerosol)	80 ^a	
		Renal imaging/renography	300ª	
		Brain imaging (static)	500 ^a , 800 (SPECT) ^a	
		First-pass blood-flow studies	800 ^a	
99Tcm	DMSA	Renal imaging (DMSA(III))	80ª	
		Tumour imaging (DMSA(V))	400 ^a	
99Tcm	ECD	Brain imaging	500ª	
99Tcm	Erythrocytes (normal)	GI bleeding	400ª	
		Cardiac blood-pool imaging or peripheral vascular imaging	800ª	
99Tcm	Erythrocytes (heat denatured)	Spleen imaging	100ª	
99Tcm	Exametazime	Cerebral blood-flow imaging (SPECT)	500ª	
99Tcm	Iminodiacetates (IDAs)	Functional biliary system imaging	150ª	
99Tcm	Leucocvtes	Infection/inflammation imaging	200ª	
	,			

Typical Administered Activity (MBq)

Radionuclide		Pharmaceutical	Indication/Use	Activity (MBq)
	99Tcm	Macroaggregated albumin	Lung perfusion imaging	100 ^a , 200 (SPECT) ^a
	99Tcm	MAG3	Renal imaging/renography	100ª
			First-pass blood-flow imaging	200ª
	99Tcm	Nanocolloids	Lacrimal drainage	4 ^a
			Sentinel node or lymph node imaging	20 ^a
	99Tcm	Pertechnetate	Micturating cystogram	25 ^a
			Thyroid uptake	40 ^a
			Thyroid imaging, salivary gland imaging	804
			Ectopic gastric mucosa imaging (Meckel's)	400ª
			First-pass blood-flow imaging	800ª
	99Tcm	Phosphonate and phosphate compounds	Bone imaging	600°, 800 (SPECT)°
99Tcm		Sestamibi	Myocardial imaging	300 ^a , 400 (SPECT) ^a
			Tumour imaging, breast imaging	900ª
99Tcm		Sulesomab	Infection/inflammation imaging	750ª
99Tcm		Technegas	Lung ventilation imaging	40^{a}
99Tcm		Tetrofosmin	Myocardial imaging	300 ^a , 400 (SPECT) ^a
			Parathyroid imaging	900ª
¹¹¹ In		Capromab Pendetide	Biopsy-proven prostate carcinoma imaging	185 ^b
111In		DTPA	GI transit	10 ^a
			Cisternography	30 ^a

Radionuclide	Pharmaceutical	Indication/Use	Iypical Administered Activity (MBq)
¹¹¹ In	Leucocytes	Infection/inflammation imaging	20ª
111 In	Pentetreotide	Somatostatin receptor imaging	110 ^a , 220 (SPECT) ^a
¹¹¹ In	Platelets	Thrombus imaging	20ª
^{123}I	Iodide	Thyroid uptake	2ª
		Thyroid imaging	20ª
		Thyroid metastases imaging	400ª
^{123}I	Ioflupane	Striatal dopamine transporter visualisation	185ª
^{123}I	mIBG	Neuroectodermal tumour imaging	400ª
^{131}I	mIBG	Neuroectodermal tumour imaging	20 ^a
^{131}I	Iodide	Thyroid uptake	0.2ª
		Thyroid metastases imaging	400 ^a
¹³³ Xe	Xenon gas	Lung ventilation studies	400ª
201 Tl	Thallous chloride	Myocardial imaging	80–120 ^a
		Parathyroid imaging	80 ^a
		Tumour imaging	150ª

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		Thyroid imaging	20ª
		Thyroid metastases imaging	400 ^a
123 I	Ioflupane	Striatal dopamine transporter visualisation	185ª
123I	mIBG	Neuroectodermal tumour imaging	400 ^a
^{131}I	mIBG	Neuroectodermal tumour imaging	20ª
^{131}I	Iodide	Thyroid uptake	0.2ª
		Thyroid metastases imaging	400 ^a
¹³³ Xe	Xenon gas	Lung ventilation studies	400 ^a
^{201}Tl	Thallous chloride	Myocardial imaging	80-120 ^a
		Parathyroid imaging	80 ^a
		Tumour imaging	150 ^a

and others: selenium ⁷⁵Se...

Pharmaceuticals for PET imaging



- ► Half-life ¹⁵O is 2.5 min.
- Carbon dioxide (CO₂) brain blood flow
- **Oxygen** (O₂) oxygen consumption in myocardium, tumors
- **Water (**H₂O) myocardium perfusion
 - + not influenced by metabolism
 - background $^{15}\mathrm{O}$ activity in lungs and blood vessels

Nitrogen ¹³N

- ► Half-life ¹³N is 10 min.
- ▶ Ammonia (NH₃) myocardium perfusion, blood flow
 - metabolized in v tissue

Carbon ¹¹C

- ► Half-life ¹¹C is 20.4 min.
- ▶ Acetic acid (CH₃COOH) myocardium perfusion, tumor metabolism
- **Cocain, carfentanil,...** brain opiod receptor mechanisms
- **Deprenyl** monoamine oxidase inhibitor, to study Parkinson disease
- **Leucin, methionine...** amino acid tracer, brain tumor detection

Fluorine ¹⁸F

- Half-time 18 F is 109 min.
- Haloperidol neuroreceptor ligand, drug effects
- Sodium fluoride Na¹⁸F⁻ skeletal imaging, osseous blood-flow, metastases. Better signal than ^{99m}Tc
- Fluorodopa... metabolised to dopamine, neurotransmiter studies
- Flourouracil... drug, nucleic acid tracer, chemotherapy dosage
- Fluorodeoxyglucose (FDG) glucose metabolism ; neurology, cardiology, oncology. Penetrates blood-brain barier

Delivery Strategies: Metabolic pathways



FDG usage

- Brain function mapping
- ... glucose provides energy to the brain (for adults $\sim 100 \, \text{g/den}$)

FDG usage

- Brain function mapping
- \blacktriangleright . . . glucose provides energy to the brain (for adults $\sim 100\,{\rm g/den})$

Tumor mapping

... tumors have no metabolic barier

FDG in Oncology

• FDG transport into tumors occurs at a *higher* rate than in the surrounding normal tissues.

• FDG is de-phosphorylated and can then leave the cell.

• The dephosphorylation occurs at a *slower* rate in tumors.

Applications of FDG

•Locating unknown primaries

•Differentiation of tumor from normal tissue

•Pre-operative staging of disease (lung, breast, colorectal, melanoma, H&N, pancreas)

•Recurrence vs necrosis

•Recurrence vs post-operative changes (limitations with FDG)

•Monitoring response to therapy

Rubidium $^{82}\mathrm{Rb}$

- Half-life 82 Rb is 1.25 min.
- + Produced by a generator from Sr, (no cyclotron needed)
- Long positron free path \longrightarrow low spatial spatial resolution.
- + Short half-life \longrightarrow good temporal resolution
- Short half-life \longrightarrow weak signal
- Myocard perfusion
- Blood-brain barrier study

Principles of nuclear imaging

Radioactivity

Gamma camera

SPECT

PET

Conclusions

Gamma camera

Scintigraphy



Single Photon Detection with Gamma Camera



Scintillator materials

Scintillator	Density (g cm ⁻³)	Effective Z	Relative light yield	Decay constant (ns)	Wavelength of emission (nm)
Sodium Iodide (NaI)	3.67	50	100	230	410
Bismuth Germanate (BGO)	7.13	74	12	300	480
Barium Fluoride (BaF ₂)	4.89	54	5 15	0.6 - 0.8 630	220 (195) 310

- ► High Z advantageous
- BGO good for 511 keV
- ▶ For speed, use BaF_2 UV light produced

Photon Counting Detector (PCD)



- Signal propagation directed by electric field
- High quantum efficiency
- High spacial resolution

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Artifacts: scattering

Scattering of photons in patient

- Because of limited energy resolution of the detector, primary and scattered photons which pass the collimator can not be classified properly. (In the ideal case, only primary photons are used to contribute to the image)
- Effects: haziness of images, quantization is degraded.



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Artifacts: collimator blur

Collimator blur

- Because of the size of the holes, photons which are not entering the detector exactly perpendicular to the detector surface are also detected. This introduces uncertainty about the exact path the photon traveled.
- Effect: blurring which increases with larger holes. Trade off between sensitivity and resolution has to be found.



Artifacts: noise

Noise due to limited number of detected photons

- Doses and scanning time are limited while the efficiency of the collimator is also limited.
- Effects: Noise in the images. Low pass digital filtering required. This results in reduced resolution. Tradeoffs between dose, scanning time and collimator hole size have to be made.



Phantom experiments



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Lung scintigraphy



Most frequent use. Ventilation (Xe), perfusion (99m Tc). Pulmonary embolism (blocked artery)

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Image is acquired by rotating the $\gamma\text{-camera}$ around the patient and taking images at different angles



SPECT

- Patient is injected with a γ-emitting radio-pharmaceutical
- Preferred energy: 100-250 keV
- · Use of collimaters
- Collimated camera projections are acquired from different equidistant angles (30-120 projections over 180-360 degrees)
- Images are reconstructed using Filtered Back Projection
 (FBP) or Iterative Reconstruction
- Resolution: 12-20 mm
- To increase count-rate often two or three γ-camera heads are used

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SPECT, brain imaging





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SPECT, Brain perfusion



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SPECT, Whole-body imaging



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SPECT, Whole-body imaging



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Principle of PET





PET: annihilation

 $p \rightarrow n + \beta^+$



Annihilation Coincidence Detection

Isotope	Maximum Positron Range (mm)
F-18	2.6
C-11	3.8
Ga-68	9.0
Rb-82	16.5

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Gamma Ray Detections to Location of Function















- Associate detections within interval τ (a few ns)
- \blacktriangleright Start timer and wait for the second detection \longrightarrow increment count
- List mode store detections with time stamps, postprocess
- ▶ No lead collimators → higher sensitivity wrt SPECT

Time of Flight PET

Measure time interval between coincident photones



Multiple Rings, 2D – 3D



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Detector failure



Sinogram

Detector failure



Rekonstrukce

Patient motion



Lower row only uses images without motion.



Coincidence Attenuation



$$P_{C} = P_{1}P_{2}$$
$$= e^{-\mu \cdot d_{1}}e^{-\mu \cdot d_{2}}$$
$$= e^{-\mu \cdot (d_{1} + d_{2})}$$

Annihilation radiation emitted along a particular line of response has the same attenuation probability, regardless of where it originated on the line.



Calculated Attenuation Correction



 $I = I_0 \mathrm{e}^{-\mu d}$

Transmission Attenuation Measurement


Effect of Misaligned Attenuation Correction





Effect of Incorrect Ellipse Diameter



SPECT/CT





Converting Attenuation Map from Hounsfeld to 511 keV attenuation Coefficients



PET — parametry

- Effective resolution $8 \sim 10 \, \text{mm}$
- Isotropic sampling 3 mm
- Transaxial FOV 60 cm, axial 10 cm. Increase axial FOV by increasing number of detectors (=higher cost), or shift the patient (=longer time, higher dose).
- $\blacktriangleright~16\sim 64$ detector planes zachování linearity.

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PET, whole body imaging

Tumor has faster metabolism \longrightarrow contrast agents accumulates there



$\frac{\mathsf{PET} + \mathsf{FDG}}{^{18}\mathrm{F} \; \mathsf{glucose} \; (\mathsf{FDG})}$



$\mathsf{PET} + \mathsf{FDG}$

 $^{18}\mathrm{F}$ glucose (FDG). Tumor detection.



Brain Tumor FDG

6 min, 3D



PET. Lung ventilation and perfusion



PET, head



perfusion, glucose metabolism



PET, brain



Alzheimer disease



Hypometabolismus.

Parkinson disease

 $^{18}\mathrm{F}-\mathrm{DOPA}\ \mathsf{PET}\ (\mathsf{precursor}\ \mathsf{of}\ \mathsf{neurotransmiter}\ \mathsf{dopamine})$



Transplantation of dopamin producing cells.

Brain tumor



PET, Huntington disease

Reduced glucose metabolism



Brain development

FDG



1 month

3 months

6 months

1 year



Fusion of anatomical and functional data

loo:



MR1 images of a rat brain (axial, multi-slice 256 sq x 16 acquisition, coronal/sagittal views are interpolated)

Center: ¹⁴F-labeled specific ligand for the dopamin-transport protein. Compound accumulates in brain areas with a high level of dopamin containing neurons (striatum).

Bottom: Overlay in all three major directions.

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Brain at rest



Acoustic stimulation



Visual stimulation



Cognitive activity



Memory and learning



Movement





PET, heart

Contrast agent FDG



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PET, heart Contrast agent FDG







Normal





Not functional tissue, treatment not possible.





Insufficient perfusion, treatment possible.





Bad perfusion (ischemic), enlarged myocardium. Treatment possible if the metabolism is normal or increased.
Flow (e.g. NH_3) Metabolism (e.g. FDG)



Bad perfussion after load test.

Flow at rest Flow at load



Ischemic myocardium needs more glucose.

Fasting After glucose is administerd



Hibernating myocardium.

Flow (e.g. NH₃) Metabolism (e.g. FDG)



Idiopatically enlarged left ventricle. Only transplantation.

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Kinetic study

- Study the evolution of the radiotracer concentration in time
- Identify model parameters (time and transport constants)

Kinetic study

- Study the evolution of the radiotracer concentration in time
- Identify model parameters (time and transport constants)
- $\blacktriangleright \longrightarrow \mathsf{Reproducibility}$

Brain



Brain



Heart



Heart















QUALITATIVE "This pattern is characteristic of Alzheimer's Disease."

Approaches to Image Analysis



QUANTITATIVE "Metabolic rate for glucose in this region is 8.37 mg/min/100g tissue"

Normalized radioactivity image



Mean ROI value



Time-activity ROI curve



Normalized time-activity ROI curve



Ratio of regional and total activity.

Tracer modeling of the ROI curve



Find biophysical model parameters — blood flow, concentrations, diffussion coefficients.

Tracer modeling of the ROI curve



Tracer modeling of the ROI curve



Nuclear imaging — summary

- + Functional imaging; intensity of the metabolic processes
- + Targeted and specific imaging, perfussion, oncology
- Radiation dose
- Manufacturing radiopharmaceuticals, expensive
- Only partial anatomy information
- Bad spatial resolution