## Question 1.

Consider the Winnow algorithm.

- (a) What concept class was Winnow designed for? What is Winnow's mistake bound for that class?
- (b) Adapt the algorithm to learn general conjunctions. How will the mistake bound change?

## Question 2.

Consider the halving algorithm with hypothesis class (initial hypothesis)  $\mathcal{H}_1$  of all non-contradictory conjunctions on 3 propositional variables.

- (a) Determine  $|\mathcal{H}_1|$ .
- (b) Give an upper bound on  $|\mathcal{H}_2|$  given that first prediction was incorrect.

## Question 3.

Consider halving algorithm with the initial version space  $\mathcal{H}$  consisting

(a) of all conjunctions of exactly 3 different non-negative literals, i.e.,

$$\mathcal{H} = \{ p_i \land p_j \land p_k \mid 1 \le i < j < k \le n \}$$

- (b) of all conjunctions that use some of the given variables (and the empty conjunction).
- (c) of all n-CNFs.
- 1. For each scenario, determine if the learner learns  $\mathcal{H}$  online (in the mistake-bound model) and justify your answer.
- 2. For each scenario where the learner learns in the mistake bound model, decide if they learn efficiently as well. Assume that checking the consistency of a single hypothesis with an observation takes a unit of time.
- 3. For the **first** case, assume the first example is (0, 1, 1, 1, ... 1) and it is a negative instance. What will be the learner's prediction for the second example, which is (0, 1, 0, 1, ...)? Justify your answer.

## Question 4.

Consider the following hypothesis classes. For each hypothesis class, determine its VC dimension and provide a brief proof.

- (a)  $\mathcal{H} = \{h : \mathbb{R} \mapsto \{0, 1\}, h(x) = [x > t], t \in \mathbb{R}\}$
- (b)  $\mathcal{H} = \{h : \mathbb{R} \mapsto \{0; 1\}, h(x) = [t_1 \le x < t_2], t_1 < t_2 \in \mathbb{R}\}$
- (c)  $\mathcal{H}$  is the set of all monotone conjunctions on n variables.