

**Medical Imaging**  
**Magnetic Resonance Imaging, Instrumentation**  
**(Outline of Lecture 3)**

### 3. MRI Hardware

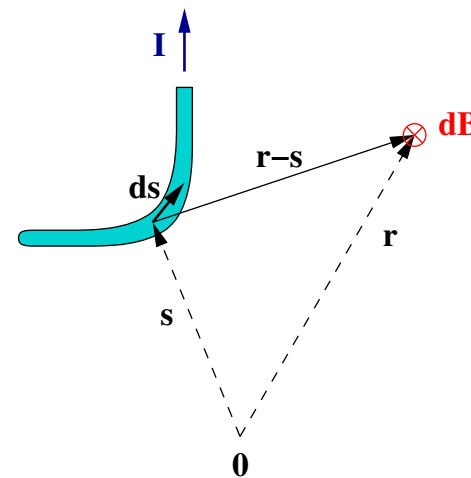
#### A. Main magnet

Requirements: strong magnetic field, homogeneous in a sufficiently large region

Electromagnet built up of solenoid coils

Relation electric current  $\Rightarrow$  magnetic field: “Thin wire” approximation of Biot–Savart law

$$\vec{B}(\vec{r}) = \frac{\mu_0 I}{4\pi} \int \frac{d\vec{s} \times (\vec{r} - \vec{s})}{\|\vec{r} - \vec{s}\|^3}$$



Simplest approximation: infinitely long solenoid with  $n_m$  – turns per meter.

$$\vec{B} = \mu_0 I n_m \vec{e}_z$$

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Real magnets:

- ◆ inhomogeneity of the  $\vec{B}$  field
- ◆ stray fields
- ◆ magnetic field  $B > 1T$  requires high current  $\Rightarrow$  high amount of power dissipated in form of heat.

Therefore *superconducting* magnets with shielding

- ◆  $T < 12K$ , liquid helium
- ◆ restrictions on: current density, magnetic fields
- ◆ radiation shields, cryocooler
- ◆ additional, independent coils for fine tuning of the field

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#### B. Gradient Chain

Gradient field  $\vec{B}_g = (g_x x + g_y y + g_z z) \vec{e}_z$

Requirements: linearity over the imaging volume, fast switching time

#### z-Gradient:

Two coaxial coils with opposite currents

Field for a ring current at z axis, Biot–Savart  $\Rightarrow$

$$\vec{B}(z) = \frac{\mu_0 I R^2}{2(z^2 + R^2)^{3/2}} \vec{e}_z$$

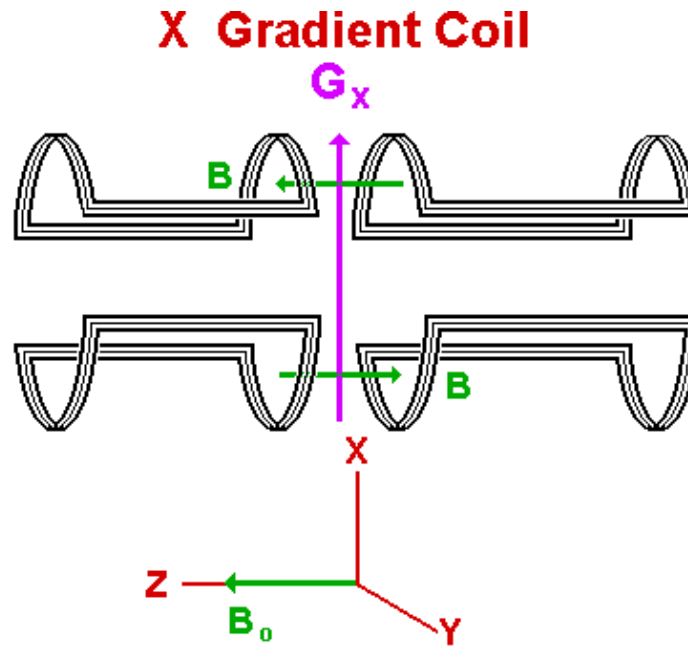
where  $R$  – radius of the ring

To increase linearity – use more than 2 rings with position dependent current.

Trade-off: linearity and small self inductance

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#### x/y-Gradient



Fast on/off switching induces eddy currents  $\Rightarrow$  active shielding

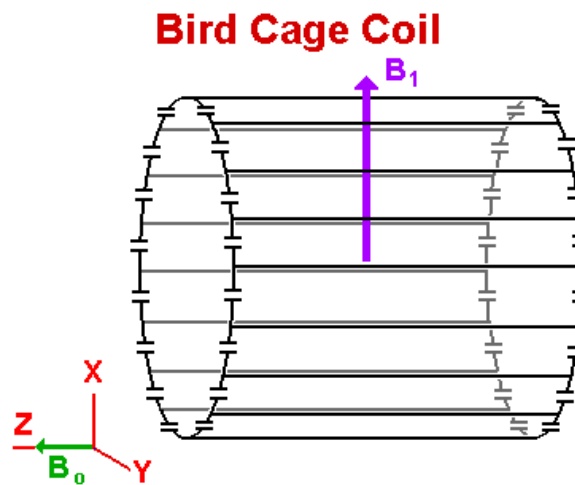
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**C. RF Coils** A single circular coil is not optimal:

$$B(y) = \frac{\mu_0 I R^2}{2(y^2 + R^2)^{3/2}}$$

inhomogeneous field, fast decay with distance.

Better solution – birdcage coil



Consider a cylinder oriented along the z-axis with the current distribution  $I_z = I_0 \cos \phi$  in its jacket. This gives a homogeneous transversal field.

Application of an alternating current gives a rotating transversal field.

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#### Exercises

**1.** Consider a solenoid electromagnet with the following layout: radius  $R = 0.5m$ , length  $l = 1m$ , made of copper wire with cross section radius  $r = 0.5cm$  and 20 turns per centimetre.

a) Calculate the current needed to have a magnetic field of 1 Tesla in the solenoid. Use the approximation of an infinitely long solenoid.

b) Copper has specific resistance  $1.6 \times 10^{-8} Ohm \cdot m$ . Calculate the voltage and power needed to operate such a magnet.

**2.**

a) Calculate the magnetic field of an infinitely long straight wire carrying the current  $I$ . Use Ampère's circuital law and utilize the symmetry of the problem.

b) Calculate the force exerted by a wire of length  $l = 1m$  onto a parallel wire of the same length at distance  $a = 2cm$  if both wires carry a current  $I$  as calculated in exercise 1. Use the approximation of an infinite wire for the magnetic field.

**3.** Calculate the magnetic field on the symmetry axis for a ring current. Use Biot–Savart's law.