

# Robotic Information Gathering - Exploration of Unknown Environment

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Lecture 05

B4M36UIR – Artificial Intelligence in Robotics

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## Robotic Information Gathering

Create a model of phenomena by autonomous mobile robots performing measurements in a dynamic unknown environment.

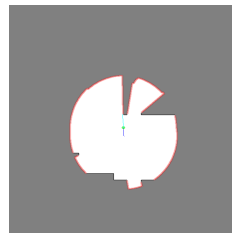


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## Mobile Robot Exploration

- Create a map of the environment
- **Frontier**-based approach  
Yamauchi (1997)
- Occupancy grid map  
Moravec and Elfes (1985)
- Laser scanner sensor
- Next-best-view approach  
Select the next robot goal



Performance metric:

Time to create the map of the whole environment

search and rescue mission

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## Overview of the Lecture

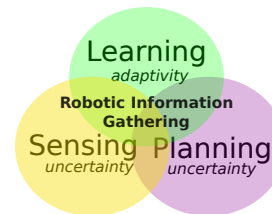
- Part 1 – Robotic Information Gathering - Robotic Exploration
  - Robotic Information Gathering
  - Robotic Exploration
  - TSP-based Robotic Exploration
  - Robotic Information Gathering

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## Challenges in Robotic Information Gathering

- Where to take new measurements?  
To improve the phenomena model
- What locations visit first?  
On-line decision-making
- How to efficiently utilize more robots?  
To divide the task between the robots
- How to navigate robots to the selected locations?  
Improve Localization vs Model



How to address all these aspects altogether to find a cost efficient solution using in-situ decisions?

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## Environment Representation – Mapping and Occupancy Grid

- The robot uses its sensors to build a map of the environment
- The robot should be localized to integrate new sensor measurements into a globally consistent map
- **SLAM** – Simultaneous Localization and Mapping
  - The robot uses the map being built to localize itself
  - The map is primarily to help to localize the robot
  - The map is a "side product" of SLAM
- **Grid map** – discretized world representation
  - A cell is **occupied** (an obstacle) or **free**
- **Occupancy grid map**
  - Each cell is a binary random variable modeling the occupancy of the cell



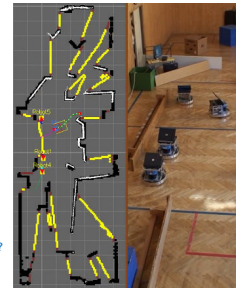
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## Robotic Exploration of Unknown Environment

- Robotic exploration is a fundamental problem of robotic information gathering
- The problem is:  
How to efficiently utilize a group of mobile robots to autonomously create a map of an unknown environment
  - Performance indicators vs constraints  
Time, energy, map quality vs robots, communication
  - Performance in a real mission depends on the on-line **decision-making**
  - It includes the problems of:
    - Map building and localization
    - Determination of the navigational waypoints
    - Path planning and navigation to the waypoints
    - Coordination of the actions (multi-robot team)



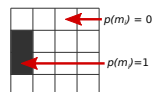
Courtesy of M. Kulich

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## Occupancy Grid

- **Assumptions**
  - The area of a cell is either completely free or occupied
  - Cells (random variables) are independent of each other
  - The state is **static**
- A cell is a binary random variable modeling the occupancy of the cell
  - Cell  $m_i$  is occupied  $p(m_i) = 1$
  - Cell  $m_i$  is not occupied  $p(m_i) = 0$
  - **Unknown**  $p(m_i) = 0.5$
- Probability distribution of the map  $m$



$$p(m) = \prod_i p(m_i)$$

- Estimation of map from sensor data  $z_{1:t}$  and robot poses  $x_{1:t}$

$$p(m|z_{1:t}, x_{1:t}) = \prod_i p(m_i|z_{1:t}, x_{1:t})$$

Binary Bayes filter – Bayes rule and Markov process assumption

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## Binary Bayes Filter 1/2

- Sensor data  $z_{1:t}$  and robot poses  $x_{1:t}$
- Binary random variables are independent and states are static

$$\begin{aligned}
 p(m_i|z_{1:t}, x_{1:t}) &\stackrel{\text{Bayes rule}}{=} \frac{p(z_t|m_i, z_{1:t-1}, x_{1:t})p(m_i|z_{1:t-1}, x_{1:t})}{p(z_t|z_{1:t-1}, x_{1:t})} \\
 &\stackrel{\text{Markov}}{=} \frac{p(z_t|m_i, x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(z_t|z_{1:t-1}, x_{1:t})} \\
 \hline
 p(z_t|m_i, x_t) &= \frac{p(m_i, z_t, x_t)p(z_t, x_t)}{p(m_i|x_t)} \\
 \hline
 p(m_i, z_{1:t}, x_{1:t}) &\stackrel{\text{Bayes rule}}{=} \frac{p(m_i|z_t, x_t)p(z_t|x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(m_i|x_t)p(z_t|z_{1:t-1}, x_{1:t})} \\
 &\stackrel{\text{Markov}}{=} \frac{p(m_i|z_t, x_t)p(z_t|x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1}, x_{1:t})}
 \end{aligned}$$

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## Occupancy Mapping Algorithm

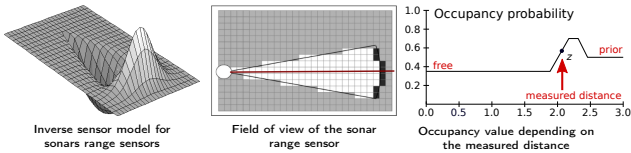
**Algorithm 1:** OccupancyGridMapping( $\{l_{t-1,i}\}, x_t, z_t$ )

```

foreach  $m_i$  of the map  $m$  do
  if  $m_i$  in the perceptual field of  $z_t$  then
     $l_{t,i} := l_{t-1,i} + \text{inv\_sensor\_model}(m_i, x_t, z_t) - l_0$ ;
  else
     $l_{t,i} := l_{t-1,i}$ ;
return  $\{l_{t,i}\}$ 

```

- Occupancy grid mapping developed by Moravec and Elfes in mid 80'ies for noisy sonars



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## Frontier-based Exploration Strategy

**Algorithm 3:** Frontier-based Exploration

```

map := init(robot, scan);
while there are some reachable frontiers do
  Update occupancy map using new sensor data and Bayes rule;
   $\mathcal{M} :=$  Created grid map from map using thresholding;
   $\mathcal{M} :=$  Grow obstacle according to the dimension of the robot;
   $\mathcal{F} :=$  Determine frontier cells from  $\mathcal{M}$ ;
   $\mathcal{F} :=$  Filter out unreachable frontiers from  $\mathcal{F}$ ;
   $f :=$  Select the closest frontier from  $\mathcal{F}$ , e.g. using shortest path;
  path := Plan a path from the current robot position to  $f$ ;
  Navigate robot towards  $f$  along path (for a while);

```

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## Binary Bayes Filter 2/2

- Probability a cell is occupied

$$p(m_i|z_{1:t}, x_{1:t}) = \frac{p(m_i|z_t, x_t)p(z_t|x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1}, x_{1:t})}$$

- Probability a cell is not occupied

$$p(\neg m_i|z_{1:t}, x_{1:t}) = \frac{p(\neg m_i|z_t, x_t)p(z_t|x_t)p(\neg m_i|z_{1:t-1}, x_{1:t-1})}{p(\neg m_i)p(z_t|z_{1:t-1}, x_{1:t})}$$

- Ratio of the probabilities

$$\begin{aligned}
 \frac{p(m_i|z_{1:t}, x_{1:t})}{p(\neg m_i|z_{1:t}, x_{1:t})} &= \frac{p(m_i|z_t, x_t)p(m_i|z_{1:t-1}, x_{1:t-1})p(\neg m_i)}{p(\neg m_i|z_t, x_t)p(\neg m_i|z_{1:t-1}, x_{1:t-1})p(m_i)} \\
 &= \frac{p(m_i|z_t, x_t)}{1 - p(m_i|z_t, x_t)} \frac{p(m_i, z_{1:t-1}, x_{1:t-1})}{1 - p(m_i, z_{1:t-1}, x_{1:t-1})} \frac{1 - p(m_i)}{p(m_i)}
 \end{aligned}$$

sensor model  $z_t$ , recursive term, prior

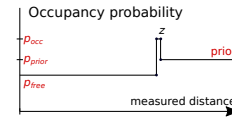
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## Model for Laser Sensor

- The model is “sharp” with a precise detection of the obstacle
- For the range measurement  $d_i$ , update the grid cells along a sensor beam

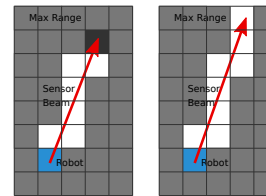


**Algorithm 2:** Update map for  $\mathcal{L} = (d_1, \dots, d_n)$

```

foreach  $d_i \in \mathcal{L}$  do
  foreach cell  $m_i$  raycasted towards  $\min(d_i, \text{range})$  do
     $p := \text{grid}(m_i)p_{\text{free}}$ ;
     $\text{grid}(m_i) := p/(2p - p_{\text{free}} - \text{grid}(m_i) + 1)$ ;
     $m_d :=$  cell at  $d_i$ ;
    if obstacle detected at  $m_d$  then
       $p := \text{grid}(m_d)p_{\text{occ}}$ ;
       $\text{grid}(m_i) := p/(2p - p_{\text{occ}} - \text{grid}(m_i) + 1)$ 
    else
       $p := \text{grid}(m_d)p_{\text{free}}$ ;
       $\text{grid}(m_i) := p/(2p - p_{\text{free}} - \text{grid}(m_i) + 1)$ 

```



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## Multi-Robot Exploration – Map Marge

- The individual maps can be merged in a similar way as integration of new sensor measurements

$$\begin{aligned}
 P(\text{occ}_{x,y}) &= \frac{\text{odds}_{x,y}}{1 + \text{odds}_{x,y}}, \\
 \text{odds}_{x,y} &= \prod_{i=1}^n \text{odds}_{x,y}^i, \\
 \text{odds}_{x,y}^i &= \frac{P(\text{occ}_{x,y}^i)}{1 - P(\text{occ}_{x,y}^i)}.
 \end{aligned}$$

$P(\text{occ}_{x,y}^i)$  is the probability that grid cell on the global coordinate is occupied in the map of the robot.

We need the same global reference frame (localization).

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## Logs Odds Notation

- Log odds ratio is defined as

$$l(x) = \log \frac{p(x)}{1 - p(x)}$$

- and the probability  $p(x)$  is

$$p(x) = 1 - \frac{1}{1 + e^{l(x)}}$$

- The product modeling the cell  $m_i$  based on  $z_{1:t}$  and  $x_{1:t}$

$$l(m_i|z_{1:t}, x_{1:t}) = \underbrace{l(m_i|z_t, x_t)}_{\text{inverse sensor model}} + \underbrace{l(m_i|z_{1:t-1}, x_{1:t-1})}_{\text{recursive term}} - \underbrace{l(m_i)}_{\text{prior}}$$

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## Frontier-based Exploration

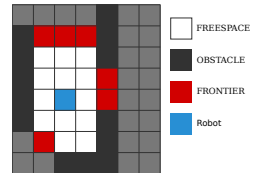
- The basic idea of the **frontier** based exploration is navigation of the mobile robot towards unknown regions

Yamauchi (1997)

- **Frontier** – a border of the known and unknown regions of the environment
- Based on the probability of individual cells in the occupancy grid, cells are classified into:

- FREESPACE –  $p(m_i) < 0.5$
- OBSTACLE –  $p(m_i) > 0.5$
- UNKNOWN –  $p(m_i) = 0.5$

- **Frontier cell** is a FREESPACE cell that is incident with an UNKNOWN cell
- Frontier cells as the navigation waypoints have to be reachable, e.g., after obstacle growing



Use grid-based path planning

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## Multi-Robot Exploration – Overview

- We need to assign navigation waypoint to each robot, which can be formulated as the **task-allocation problem**
- Exploration can be considered as an **iterative procedure**

1. Initialize the occupancy grid  $Occ$
2.  $\mathcal{M} \leftarrow \text{create\_navigation\_grid}(Occ)$   
cells of  $\mathcal{M}$  have values {freespace, obstacle, unknown}
3.  $\mathcal{F} \leftarrow \text{detect\_frontiers}(\mathcal{M})$
4. Goal candidates  $\mathcal{G} \leftarrow \text{generate}(\mathcal{F})$
5. **Assign next goals to each robot**  $r \in \mathcal{R}$ ,  
 $((r_1, g_{r_1}), \dots, (r_m, g_{r_m})) = \text{assign}(\mathcal{R}, \mathcal{G}, \mathcal{M})$   
consisting of simple operations
6. **Create a plan  $P_i$  for each pair  $(r_i, g_{r_i})$**
7. **Perform each plan up to  $s_{\max}$  operations**  
At each step, update  $Occ$  using new sensor measurements
8. If  $|\mathcal{G}| == 0$  exploration finished, otherwise go to Step 2



- There are several parts of the exploration procedure where important decisions are made regarding the exploration performance, e.g.

- How to determined goal candidates from the the frontiers?
- How to plan a paths and assign the goals to the robots?
- How to navigate the robots towards the goal?
- When to replan?
- etc.

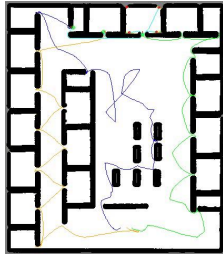
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## Exploration Procedure – Decision-Making Parts

1. Initialize – set plans for  $m$  robots,  $\mathcal{P} = (P_1, \dots, P_m)$ ,  $P_i = \emptyset$ .
2. Repeat
  - 2.1 **Navigate robots** using the plans  $\mathcal{P}$ ;
  - 2.2 Collect new measurements;
  - 2.3 Update the navigation map  $\mathcal{M}$ ;
 Until replanning condition is met.
3. Determine goal candidates  $\mathbf{G}$  from  $\mathcal{M}$ .
4. If  $|\mathbf{G}| > 0$  assign goals to the robots
  - $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \text{assign}(\mathbf{R}, \mathbf{G}, \mathcal{M})$ ,  $r_i \in \mathbf{R}, g_{r_i} \in \mathbf{G}$ ;
  - **Plan paths** to the assigned goals  
 $\mathcal{P} = \text{plan}(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle, \mathcal{M})$ ;
  - Go to Step 2.
5. Stop all robots or navigate them to the depot



All reachable parts of the environment are explored.

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## Multi-Robot Exploration Strategy

- A set of  $m$  robots at positions  $\mathbf{R} = \{r_1, r_2, \dots, r_m\}$
- At time  $t$ , let a set of  $n$  goal candidates be  $\mathbf{G}(t) = \{g_1, \dots, g_n\}$



i.e., frontiers

- The exploration strategy (at the planning step  $t$ ):

Select a goal  $g \in \mathbf{G}(t)$  for each robot  $r \in \mathbf{R}$  that will minimize the required time to explore the environment.

The problem is formulated as the **task-allocation problem**

$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \text{assign}(\mathbf{R}, \mathbf{G}(t), \mathcal{M}),$$

where  $\mathcal{M}$  is the current map

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## MTSP-based Task-Allocation Approach

- Consider the task-allocation problem as the **Multiple Traveling Salesman Problem (MTSP)**
- MTSP heuristic (*cluster-first, route-second*)
  1. Cluster the goal candidates  $\mathbf{G}$  to  $m$  clusters  
 $\mathbf{C} = \{C_1, \dots, C_m\}$ ,  $C_i \subseteq \mathbf{G}$   
*using K-means*
  2. For each robot  $r_i \in \mathbf{R}$ ,  $i \in \{1, \dots, m\}$  select the next goal  $g_i$  from  $C_i$  using the TSP distance cost  
*Kulich et al., ICRA (2011)*
    - Solve the TSP on the set  $C_i \cup \{r_i\}$   
*the tour starts at  $r_i$*
    - The next robot goal  $g_i$  is the first goal of the found TSP tour

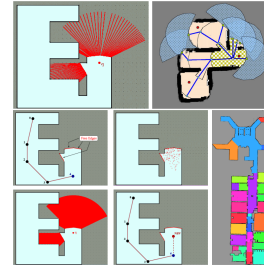
Faigl, J., Kulich, M., Přeucil, L. (2012): Goal Assignment using Distance Cost in Multi-Robot Exploration - IROS.

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## Improvements of the basic Frontier-based Exploration

Several improvements have been proposed in the literature

- Introducing utility as a computation of expected covered area from a frontier  
 González-Baños, Latombe (2002)
- Map segmentation for identification of rooms and exploration of the whole room by a single robot  
 Holz, Basilico, Amigoni, Behnke (2010)
- Consider longer planning horizon (as a solution of the Traveling Salesman Problem (TSP))  
 Zlot, Stentz (2006), Kulich, Faigl (2011, 2012)
- Representatives of free edges  
 Faigl, Kulich (2015)



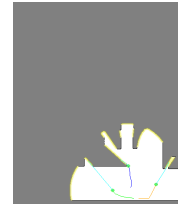
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## Multi-Robot Exploration – Problem Definition

A problem of creating a grid map of the unknown environment by a set of  $m$  robots  $\mathbf{R} = \{r_1, r_2, \dots, r_m\}$ .

Exploration is an iterative procedure:

1. Collect new sensor measurements
2. **Determine a set of goal candidates**  
 $\mathbf{G}(t) = \{g_1, g_2, \dots, g_n\}$   
*e.g., frontiers*
3. At time step  $t$ , select next goal for each robot as the **task-allocation problem**  
 $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \text{assign}(\mathbf{R}, \mathbf{G}(t), \mathcal{M}(t))$   
*using the distance cost function*
4. Navigate robots towards goal
5. If  $|\mathbf{G}(t)| > 0$  go to Step 1; otherwise terminate



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## Statistical Evaluation of the Exploration Strategies

- Evaluation for the number of robots  $m$  and sensor range  $\rho$

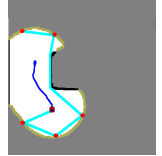
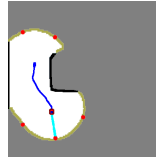
$\rho$	$m$	Iterative vs Greedy	Hungarian vs Iterative	MTSP vs Hungarian
3.0	3	+	=	+
3.0	5	+	=	+
3.0	7	+	=	+
3.0	10	+	+	-
4.0	3	+	=	+
4.0	5	+	=	=
4.0	7	+	=	+
4.0	10	+	+	-
5.0	3	+	=	+
5.0	5	+	=	+
5.0	7	+	=	+
5.0	10	+	+	-

Total number of trials 14 280

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## Distance Cost Variants

- **Simple robot-goal distance**
  - Evaluate all goals using the robot-goal distance  
*A length of the path from the robot position to the goal candidate*
  - Greedy goal selection – the closest one
  - Using frontier representatives improves the performance a bit
- **TSP distance cost**
  - Consider visitations of all goals  
*Solve the associated traveling salesman problem (TSP)*
  - A length of the tour visiting all goals
  - Use frontier representatives
  - the TSP distance cost improves performance about 10-30% without any further heuristics, e.g., expected coverage (utility)



Kulich, M., Faigl, J., Přeucil, L. (2011): On Distance Utility in the Exploration Task. ICRA.

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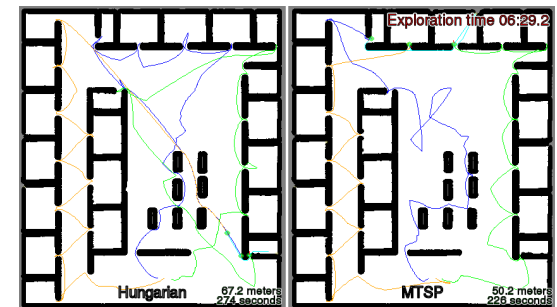
## Goal Assignment Strategies – Task Allocation Algorithms

1. **Greedy Assignment**  
 Yamauchi B, Robotics and Autonomous Systems 29, 1999
  - Randomized greedy selection of the closest goal candidate
2. **Iterative Assignment**  
 Werger B, Mataric M, Distributed Autonomous Robotic Systems 4, 2001
  - Centralized variant of the broadcast of local eligibility algorithm (BLE)
3. **Hungarian Assignment**
  - Optimal solution of the task-allocation problem for assignment of  $n$  goals and  $m$  robots in  $O(n^3)$   
*Stachniss C, C implementation of the Hungarian method, 2004*
4. **Multiple Traveling Salesman Problem – MTSP Assignment**
  - (*cluster-first, route-second*), the TSP distance cost  
*Faigl et al. 2012*

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## Performance of the MTSP vs Hungarian Algorithm

- Replanning as quickly as possible;  $m = 3, \rho = 3\text{ m}$



The MTSP assignment provides better performance

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## Information Theory in Robotic Information Gathering

- Employ information theory in control policy for robotic exploration
  - Entropy** – uncertainty of  $x$ :  $H[x] = - \int p(x) \log p(x) dx$
  - Conditional Entropy** – expected uncertainty of  $x$  after learning unknown  $z$ :  $H[x|z]$
  - Mutual information** – how much uncertainty of  $x$  will be reduced by learning  $z$ :  $I_{MI}[x; z] = H[x] - H[x|z]$
- Control policy is a rule how to select the robot action that reduces the uncertainty of estimate by learning measurements:

$$\operatorname{argmax}_{a \in A} I_{MI}[x; z|a],$$

where  $A$  is a set of possible actions,  $x$  is a future estimate, and  $z$  is future measurement

- Computation of the mutual information is computationally demanding
- Cauchy-Schwarz Quadratic Mutual Information (CSQMI)** defined similarly to mutual information

- A linear time approximations for CSQMI

Charrow, B. et al., (2015): Information-theoretic mapping using Cauchy-Schwarz Quadratic Mutual Information. ICRA.

- Compute CSQMI as Cauchy-Schwarz divergence  $I_{CS}[m; z]$  – raycast of the sensor beam and determine distribution over the range returns

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## Robotic Information Gathering

- Robotic information gathering can be considered as the **informative motion planning** problem to a determine trajectory  $\mathcal{P}^*$  such that

$$\mathcal{P}^* = \operatorname{argmax}_{\mathcal{P} \in \Psi} I(\mathcal{P}), \text{ such that } c(\mathcal{P}) \leq B, \text{ where}$$

- $\Psi$  is the space of all possible robot trajectories,
- $I(\mathcal{P})$  is the information gathered along the trajectory  $\mathcal{P}$
- $c(\mathcal{P})$  is the cost of  $\mathcal{P}$  and  $B$  is the allowed budget

- Searching the space of all possible trajectories is complex and demanding problem

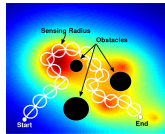
- A discretized problem can solved by combinatorial optimization techniques

*Usually scale poorly with the size of the problem*

- A trajectory is from a continuous domain

- Sampling-based motion planning techniques** can employed for finding maximally informative trajectories

Hollinger, G., Sukhatme, G. (2014): Sampling-based robotic information gathering algorithms. IJRR.



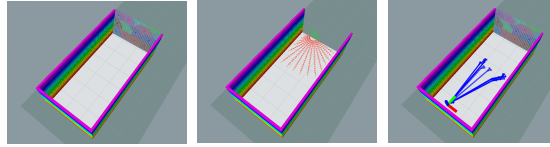
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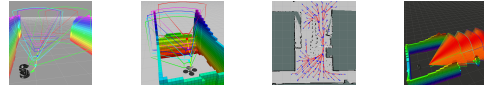
## Actions

- Actions are shortest path to cover the frontiers



Detect and cluster frontiers Sampled poses to cover a cluster Paths to the sampled poses

- Select an action (a path) that maximizes the rate of Cauchy-Schwarz Quadratic Mutual Information



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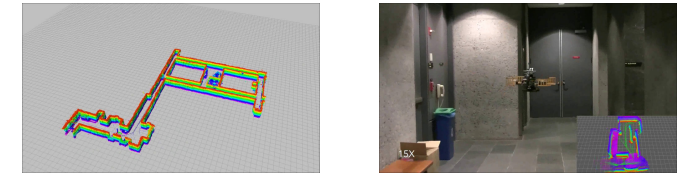
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Topics Discussed

## Summary of the Lecture

## Example of Autonomous Exploration using CSQMI



Ground vehicle

Aerial vehicle

- Planning with trajectory optimization – determine trajectory maximizing  $I_{CS}$   
Charrow, B. et al., (2015): Information-Theoretic Planning with Trajectory Optimization for Dense 3D Mapping. RSS.

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Topics Discussed

## Topics Discussed

- Robotic information gathering
- Robotic exploration of unknown environment
- Occupancy grid map
- Frontier based exploration
- Exploration procedure and decision-making
- TSP-based distance cost in frontier-based exploration
- Multi-robot exploration and task-allocation
- Mutual information and informative path planning *informative and motivational*

- Next: Randomized sampling-based motion planning methods**

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