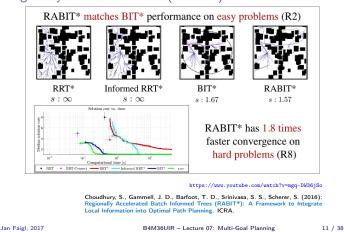


8 / 38

Jan Faigl, 2017

Selected Sampling-based Motion Planner

## Regionally Accelerated BIT\* (RABIT\*) - Demo



## Multi-Goal Path Planning

## Motivation

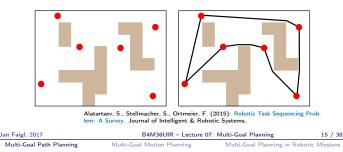
Multi-Goal Path Planning

Having a set of locations (goals) to be visited, determine the cost-efficient path to visit them and return to a starting location.

- Locations where a robotic arm performs some task
- Locations where a mobile robot has to be navigated

To perform measurements such as scan the environment or read data from sensors

Multi-Goal Planning in Robotic Missions



## Multi-Goal Path Planning (MTP) Problem

Given a map of the environment  $\mathcal{W}$ , mobile robot  $\mathcal{R}$ , and a set of locations, what is the shortest possible collision free path that visits each location exactly once and returns to the origin location.

- MTP problem is a robotic variant of the TSP with the edge costs as the length of the *shortest* path connecting the locations
- For *n* locations, we need to compute up to  $n^2$ shortest paths (solve  $n^2$  motion planning problems)
- The paths can be found as the shortest path in a graph (roadmap), from which the G(V, E)for the TSP can be constructed

Jan Faigl, 2017

Visibility graph as the roadmap for a point robot provides a straight forward solution, but such a shortest path may not be necessarily feasible for more complex robots

B4M36UIR - Lecture 07: Multi-Goal Planning

Jan Faigl, 2017

Selected Sampling-based Motion Planners

2. Anytime RRT\* [4] Non-holonomic

Ontimal B-PPT\* [36]Holonomic

8. Adapted RRT\* [64], Non-holonomic

15. Mitsubishi RRT\* [2] Non-holonomic

10. Informed RRT\* [34] Holonomic

Approaches

RRT\* [7]

B-RRT\* [58]

RRT\*-Smart [35]

4. RRT\*FN [33]

RRT# [50

9. SRRT\* [44]

11. IB-RRT\* [37]

12. DT-RRT [39]

14. RTR+CS\* [43]

16. CARRT\* [65]

17. PRRT\* [48]

Multi-Goal Path Planning

Jan Faigl, 2017

lan Faigl, 2017

Multi-Goal Path Planning

itself

13. RRT\*i[3]

Overview of Improved Algorithm

Constraints

Holonomi

Holonomic

Holonomic

Holonomic

Holonomic

Holonomic

Non-holonomic

Non-holonomic Online

Non-holonomic Offline

Non-holonomic Online

Non-holonomic Offline

Traveling Salesman Problem (TSP)

is a path in the plane.

algorithms can be found in literature.

Multi-Goal Motion Planning

ematics at the Limits of Computation

Multi-Goal Motion Planning

and returns to the origin city.

Non-holonomic

Optimal motion planning is an active research field

Offline

Online

Offline

Offline

Offlin

Offline

Offline

Offline

Offlin

Offlin

Offline

Offline

Onlin

Planning Mode Kinematic Model Sampling Strategy

Uniform

Uniform

Local bia

Uniform

Intelligen

Uniform

Uniform

Uniform

Uniform

Intelligent

Hybrid

Uniform

Uniform

B4M36UIR - Lecture 07: Multi-Goal Planning

Noreen, I., Khan, A., Habib, Z. (2016): Optimal path planning using RRT\* based 

Direct Sampling

Local Samplin

Point

Point

Point

Point

UAV

Point

Point

UAV

Car-like

Car-like

Humanoid

P3-DX

Multi-Goal Motion Planning

Autonomous Ca

Given a set of cities and the distances between each pair of cities,

It is known, the TSP is NP-hard (its decision variant) and several

In the previous cases, we consider existing roadmap or relatively

"simple" collision free (shortest) paths in the polygonal domain

However, determination of the collision-free path in a high dimen-

Therefore, we can generalize the MTP to multi-goal motion plan-

ning (MGMP) considering motion (trajectory) planners in C-space.

sional configuration space (C-space) can be a challenging problem

William J. Cook (2012) - In Pursuit of the Traveling Salesman: Math-

B4M36UIR - Lecture 07: Multi-Goal Planning

Dubin Ca

Rigid Body

Robotic Arm

Car-like and UAV

Euclidean

Goal biased

Euclidean

Euclidean

Euclidean

Euclidean

A \* Henristic

Uniform + Local Planning Angular + Euclidear

Greedy + Euclidea

Angular + Euclidear

Weighted Euclidea

MW Energy Cos

Euclidean

A\* Heuristic

Euclidean + Velocit

Cumulative Euclidear

Geometric + dynamic constraint

Multi-Goal Planning in Robotic Missions

12 / 38

an Faigl, 2017

an Faigl, 2017

16 / 38

Multi-Goal Planning in Robotic Mission

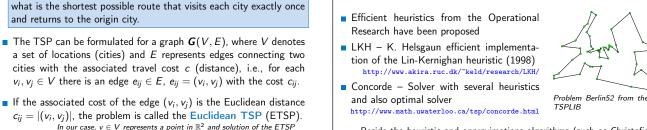
Multi-Goal Path Planning

Solutions of the TSP

B4M36UIR - Lecture 07: Multi-Goal Planning

20 / 38 Jan Faigl, 2017





Beside the heuristic and approximations algorithms (such as Christofides 3/2-approximation algorithm), other (...soft-computing") approaches have been proposed, e.g., based on genetic algorithms, and memetic approaches, ant colony optimization (ACO), and neural networks.

B4M36UIR - Lecture 07: Multi-Goal Planning

Part II

Part 2 – Multi-Goal Path and Motion

Planning

B4M36UIR - Lecture 07: Multi-Goal Planning

Goal Planning in Robotic Mi

13 / 38

17 / 38

Multi-Goal Planning in Robotic Missi

Multi-Goal Planning in Robotic Mission

Problem Statement – MGMP Problem

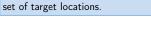
The working environment  $\mathcal{W} \subset \mathbb{R}^3$  is represented as a set of obstacles  $\mathcal{O} \subset \mathcal{W}$  and the robot configuration space  $\mathcal{C}$  describes all possible configurations of the robot in  $\mathcal W$ 

Multi-Goal Motion Planning

- For  $q \in C$ , the robot body  $\mathcal{A}(q)$  at q is collision free if  $\mathcal{A}(q) \cap \mathcal{O} = \emptyset$ and all collision free configurations are denoted as  $C_{free}$
- Set of *n* goal locations is  $\mathcal{G} = (g_1, \ldots, g_n), g_i \in \mathcal{C}_{free}$
- Collision free path from  $q_{start}$  to  $q_{goal}$  is  $\kappa : [0,1] \rightarrow C_{free}$  with  $\kappa(0) = q_{start}$  and  $d(\kappa(1), q_{end}) < \epsilon$ , for an admissible distance  $\epsilon$
- Multi-goal path  $\tau$  is admissible if  $\tau : [0,1] \to C_{free}, \tau(0) = \tau(1)$ and there are *n* points such that  $0 \leq t_1 \leq t_2 \leq \ldots \leq t_n$ ,  $d(\tau(t_i), v_i) < \epsilon$ , and  $\bigcup_{1 < i < n} v_i = \mathcal{G}$
- **The problem is to find the path**  $\tau^*$  for a cost function *c* such that  $c(\tau^*) = \min\{c(\tau) \mid \tau \text{ is admissible multi-goal path}\}$

21 / 38

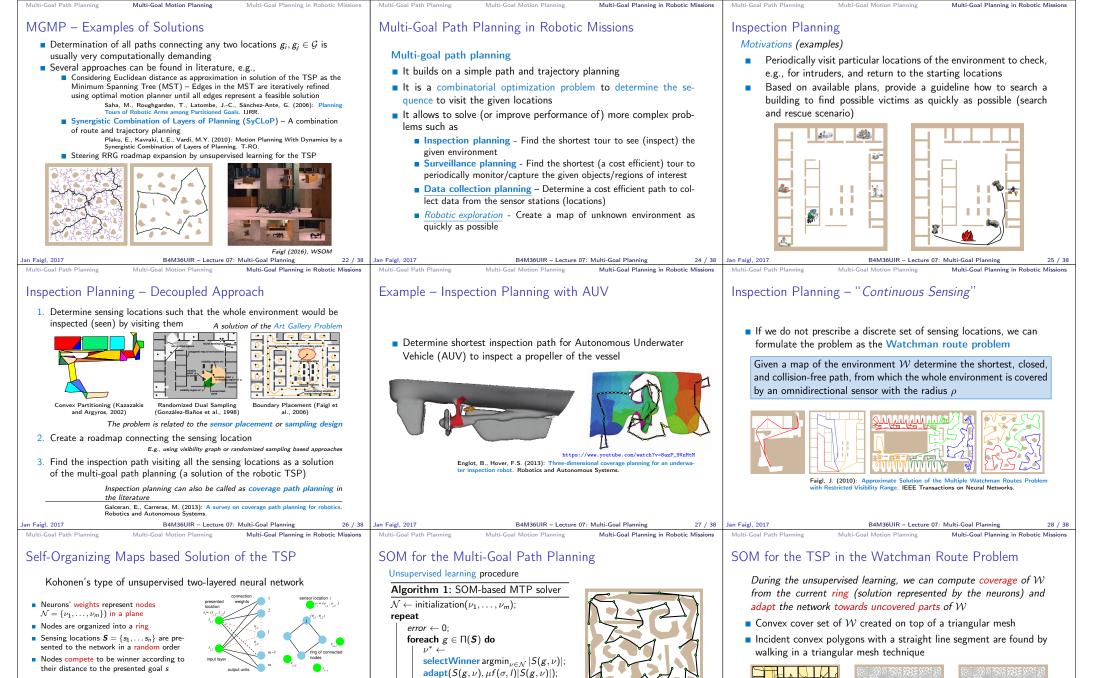




An example of MGMP can be

Plan a cost efficient trajectory for

hexapod walking robot to visit a



error  $\leftarrow \max\{error, |S(g, \nu^*)|\};$ 

For multi-goal path planning - the selectWinner and adapt procedures

Problem Neurocomputing

are based on the solution of the path planning problem

 $\sigma \leftarrow (1 - \alpha)\sigma;$ 

until error  $< \delta$ ;

- Best matching unit v to the presented prototype s is determined according to distance function  $|\mathcal{D}(\nu, s)|$
- For the Euclidean TSP,  $\mathcal{D}$  is the Euclidean distance
- However, for problems with obstacles, the multi-goal path planning,  $\mathcal{D}$  should correspond to the length of the shortest, collision free path

B4M36UIR - Lecture 07: Multi-Goal Planning

for  $d < m/n_f$ ,

 $\nu^* = \operatorname{argmin}_{\nu \in \mathcal{N}} |\mathcal{D}(\nu, s)|$ 

adapted (moved) towards the city accord-

The winner and its neighbouring nodes are

ing to the neighbouring function

Jan Faigl, 2017

29 / 38 Jan Faigl, 2017 B4M36UIR - Lecture 07: Multi-Goal Planning

Faigl, J et al. (2011): An Application of Self-Organizing Map in the non-Euclidean

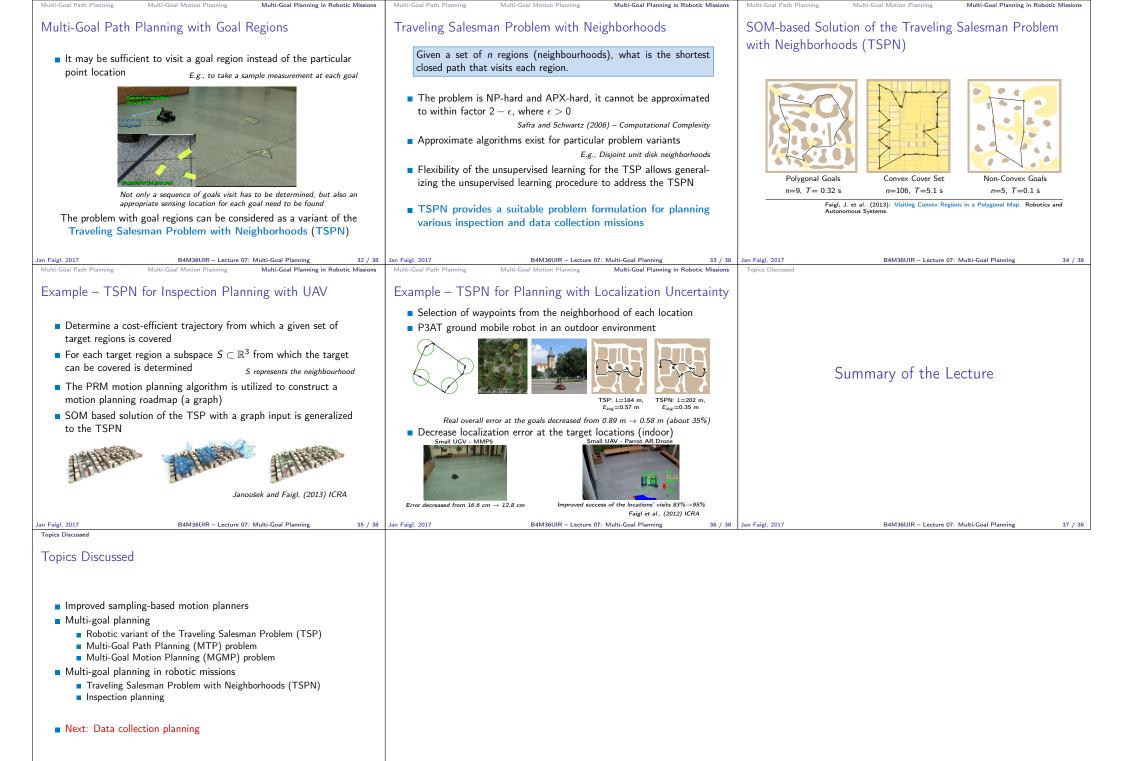
Jan Faigl, 2017

30 / 38

B4M36UIR - Lecture 07: Multi-Goal Planning

Faigl, J. (2010), TNN

and the second



Jan Faigl, 2017 B4M36UIR - Lecture 07: Multi-Goal Planning