Social Choice

Branislav Bošanský

Czech Technical University in Prague

branislav.bosansky@agents.fel.cvut.cz

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Assume there are 7 agents with following preferences:

- **3** agents: a > b > c
- 2 agents: b > c > a
- **2** agents: c > a > b

Which of the candidates is selected if we use different voting protocols:

- plurality
- Borda
- pairwise elimination with ordering: a) (a, b, c), b) (b, c, a), c) (c, a, b)

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Assume there are 7 agents with following preferences:

- **3** agents: a > b > c
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Assume that we want to include a fourth candidate d into the profiles. Is there a modification of the current preference profiles such that c can be the winner under Borda voting rule?

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Condorcet Loser

Condorcet loser is a candidate that loses in pairwise comparison with every other candidate.

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Assume we are using plurality voting rule. Can the winner under plurality be the Condorcet loser?

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How the situation changes if we use Borda voting protocol?

Social Choice in Practice

We can use the social choice methods for aggregating opinions of other agents/people in order to find the "ground truth".

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We can use the social choice methods for aggregating opinions of other agents/people in order to find the "ground truth".

For example, Kemeny voting rule corresponds to maximal-likelihood estimation principle – we are seeking for a model (truth), for which it is the highest probability that the evidence (gathered votes) is as observed.

Games and Social Choice

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	unweighted votes,			weighted votes,						
	constructive manipulation			constructive			destructive			
# alternatives			2	3	4	≥ 5	2	3	≥ 4	
# manipulators	1	≥ 2								
plurality	Р	Р	Р	Р	Р	Р	Р	Р	Р	
plurality with runoff	Р	Р	Р	NP-c	NP-c	NP-c	Р	NP-c	NP-c	
veto	Р	Р	Р	NP-c	NP-c	NP-c	Р	Р	Р	
cup	Р	Р	Р	Р	Р	Р	Р	Р	Р	
Copeland	Р	Р	Р	Р	NP-c	NP-c	Р	Р	Р	
Borda	Р	NP-c	Р	NP-c	NP-c	NP-c	Р	Р	Р	
Nanson	NP-c	NP-c	Р	Р	NP-c	NP-c	Р	Р	NP-c	
Baldwin	NP-c	NP-c	Р	NP-c	NP-c	NP-c	Р	NP-c	NP-c	
Black	Р	NP-c	Р	NP-c	NP-c	NP-c	Р	Р	Р	
STV	NP-c	NP-c	Р	NP-c	NP-c	NP-c	Р	NP-c	NP-c	
maximin	Р	NP-c	Р	Р	NP-c	NP-c	Р	Р	Р	
Bucklin	Р	Р	Р	NP-c	NP-c	NP-c	Р	Р	Р	
fallback	Р	Р	Р	Р	Р	Р	Р	Р	Р	
ranked pairs	NP-c	NP-c	Р	Р	Р	NP-c	Р	Р	?	
Schulze	Р	Р	Р	Р	Р	Р	Р	Р	Р	

Games and Social Choice

Design an algorithm for manipulating Borda rule.

Design an algorithm for manipulating Borda rule.

Design an algorithm for manipulating STV.