# **3D Computer Vision**

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Open Informatics Master's Course

### How Difficult Is Stereo?



Centrum för teknikstudier at Malmö Högskola, Sweden

The Vyšehrad Fortress, Prague

- top: easy interpretation from even a single image
- bottom left: we have no help from image interpretation
- bottom right: ambiguous interpretation due to a combination of missing texture and occlusion

# A Summary of Our Observations and an Outlook

- 1. simple matching algorithms do not work
  - the success of a model-free stereo matching is unlikely  ${\rightarrow}158$
  - without scene recognition or use high-level constraints the problem seems difficult
- 2. stereopsis requires image interpretation in sufficiently complex scenes or another-modality measurement

we have a tradeoff: model strength  $\leftrightarrow$  universality

#### **Outlook:**

- 1. represent the occlusion constraint:
  - disparity in rectified images
  - uniqueness as an occlusion constraint
- 2. represent piecewise continuity
  - ordering as a weak continuity model
- 3. use a consistent framework
  - finding the most probable solution (MAP)

correspondences are not independent due to occlusions

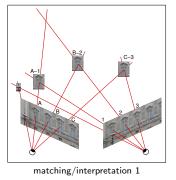
the weakest of interpretations; piecewise: object boundaries

# Structural Ambiguity in Stereovision

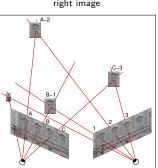
- suppose we can recognize local matches independently but have no scene model
- lack of an occlusion model ٠
- lack of a continuity model



left image



right image

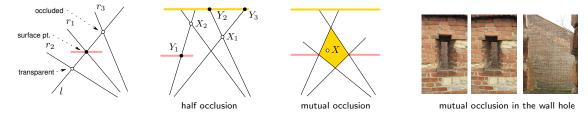


interpretation 2

- structural ambiguity in the presence of repetitions (or lack of texture)
  - Illustration of the problem
  - Keypoints: Window detections

- Repetitive keypoints  $\Rightarrow$  non-unique matching
- Cameras are not canonical; constant-depth • surface is not a plane

### ► Understanding Basic Occlusion Types



• surface point at the intersection of rays l and  $r_1$  occludes a world point at the intersection  $(l, r_3)$  and implies the world point  $(l, r_2)$  is transparent, therefore

 $(l,r_3)$  and  $(l,r_2)$  are <u>excluded</u> by  $(l,r_1)$ 

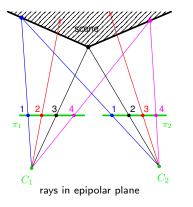
- in half-occlusion, every 3D point such as  $X_1$  or  $X_2$  is excluded by a binocularly visible surface point such as  $Y_1$ ,  $Y_2$ ,  $Y_3$  $\Rightarrow$  decisions on correspondences are not independent
- in mutual occlusion this is no longer the case: any X in the yellow zone above is not excluded

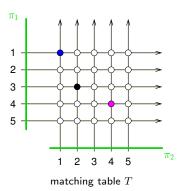


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# ► Matching Table

Based on scene opacity and the observation on mutual exclusion we expect each pixel to match at most once.





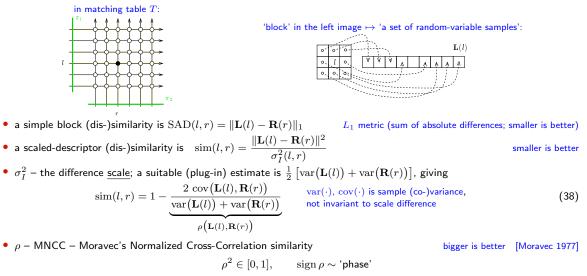
matching table

- rows and columns represent optical rays
- nodes: possible correspondence pairs
- full nodes: matches
- numerical values associated with nodes: descriptor similarities

see next

## ► Constructing An Image Similarity Cost

• let  $p_i = (l, r)$  and  $\mathbf{L}(l)$ ,  $\mathbf{R}(r)$  be (left, right) image descriptors (vectors) constructed from local image neighborhood windows



• another successful (dis-)similarity is the Hamming Distance over the Census Transform related to local binary patterns

# Census Transform (CT)

- CT: Per-pixel binarization, given reference value (e.g the window center)
- For a grayscale image:

235

185

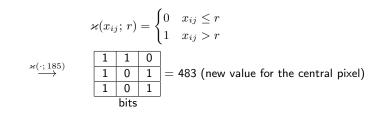
input window

61

189

217

231

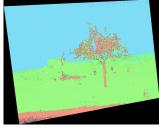




181

228

254



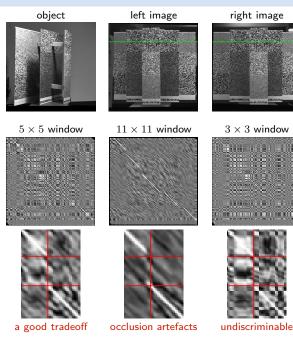


input image

 $\varkappa: \mathsf{RGB}\ \mathsf{CT},$  2-bit per pixel,  $3\times 3$  window

- preserves sharp boundaries
- may or may not use windowing (cost aggregation)

# How A Scene Looks in The Filled-In Matching Table



- MNCC  $\rho$  used ( $\alpha = 1.5, \beta = 1$ )  $\rightarrow$  182
- high-similarity structures correspond to scene objects

#### Things to notice:

#### constant disparity

- a diagonal in the matching table
- zero disparity is the main diagonal assuming standard stereopair

#### depth discontinuity

horizontal or vertical jump in matching table

#### large image window

- similarity values have better discriminability
- worse occlusion localization

#### repeated texture

horizontal and vertical block repetition

# Image Point Descriptors And Their Similarity

**Descriptors:** Image points are tagged by their (viewpoint-invariant) physical properties:

- texture window
- Census Transform
- a descriptor like DAISY
- learned descriptors
- reflectance profile under a moving illuminant
- (pixelwise) photometric ratios
- dual photometric stereo
- (pixelwise) polarization signature
- . . .
- similar points are more likely to match
- image similarity values for all 'match candidates' give the 3D matching table

y<sup>x<sub>l</sub></sup> y<sup>x<sub>r</sub></sup> y<sup>x<sub>r</sub></sup> y x<sub>l</sub> [Moravec 77] [Zabih & Woodfill 94] [Tola et al. 2010]

[Wolff & Angelopoulou 93-94] [Ikeuchi 87]

also called: 'disparity volume'

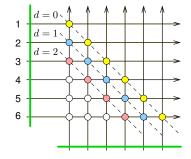
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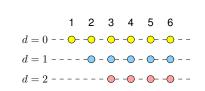
click for video

# Marroquin's Winner Take All (WTA) Matching Algorithm

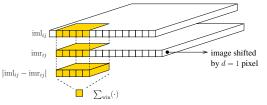
Alg: Per left-image pixel: The most SAD-similar pixel along the right epipolar line

- 1. select disparity range
- 2. represent the matching table diagonals in a compact form





- 3. use the 'image sliding & cost aggregation algorithm'
- 4. take the maximum over disparities d
- 5. threshold results by the maximal allowed SAD dissimilarity (or minimal MNCC similarity)



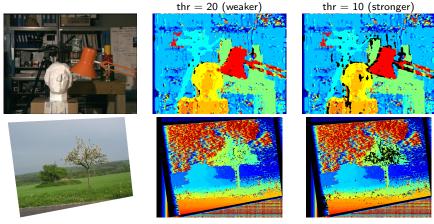
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this is a critical weak point

### A Matlab Code for WTA

```
function dmap = marroquin(iml, imr, disparityRange)
%
        iml. imr - rectified grav-scale images
% disparityRange - non-negative disparity range
% (c) Radim Sara (sara@cmp.felk.cvut.cz) FEE CTU Prague, 10 Dec 12
 thr = 20:
                                                 % bad match rejection threshold
r = 2:
 winsize = 2*r+[1 \ 1];
                                                 % 5x5 window (neighborhood) for r=2
 N = boxing(ones(size(iml)), winsize);
                                                 % the size of each local patch is
                                                 % N = (2r+1)^2 except for boundary pixels
 % --- compute dissimilarity per pixel and disparity --->
 for d = 0:disparityRange
                                                 % cycle over all disparities
  slice = abs(imr(:.1:end-d) - iml(:.d+1:end)): % pixelwise dissimilarity (unscaled SAD)
 V(:,d+1:end,d+1) = boxing(slice, winsize)./N; % window aggregation
 end
 % --- collect winners, threshold, output disparity map --->
 [cmap,dmap] = min(V,[],3);
                                                 % collect winners and their dissimilarities
 dmap(cmap > thr) = NaN;
                                                 % mask-out high dissimilarity pixels
end % of marroquin
function c = boxing(im, wsz)
% if the mex is not found. run this slow version:
 c = conv2(ones(1,wsz(1)), ones(wsz(2),1), im, 'same');
end % of boxing
```

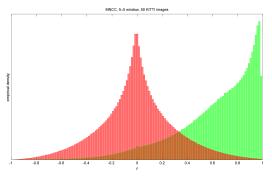
### WTA: Some Results



- results are fairly bad
- false matches in textureless image regions and on repetitive structures (book shelf)
- a more restrictive threshold (thr = 10) does not work as expected
- we searched the true disparity range, results get worse if the range is set wider
- chief failure reasons:
  - unnormalized image dissimilarity does not work well
  - no occlusion model (it just ignores the occlusion structure we have discussed ightarrow172)

### ► A Principled Approach to Similarity

Empirical Distribution of MNCC  $\rho$  for Matches (green) and Non-Matches (red)



- histograms of  $\rho$  computed from  $5\times 5$  correlation window
- KITTI dataset
  - $4.2 \cdot 10^6$  ground-truth (LiDAR) matches for  $p_1(\rho)$  (green),
  - $4.2\cdot 10^6$  random non-matches for  $p_0(
    ho)$  (red)

#### Obs:

- non-matches (red) may have arbitrarily large ho
- matches (green) may have arbitrarily low ho
- $\rho = 1$  is improbable for matches

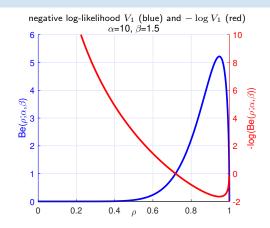
 $\rho$ : bigger is better

### Match Likelihood

- $\rho$  is just a normalized measurement
- we need a probability distribution on [0, 1] e.g. the histogram or the Beta distribution:

$$p_1(\rho) = \frac{1}{B(\alpha, \beta)} |\rho|^{\alpha - 1} (1 - |\rho|)^{\beta - 1}$$

- note that uniform distribution is obtained for  $\alpha = \beta = 1$
- when  $\alpha = 2$  and  $\beta = 1$  then  $p_1(\cdot) = 2|\rho|$



• the mode is at 
$$\sqrt{rac{lpha-1}{lpha+eta-2}}pprox 0.9733$$
 for  $lpha=10,\ \beta=1.5$ 

- if we chose  $\beta=1$  then the mode was at  $\rho=1$
- perfect similarity is 'suspicious' (depends on expected camera noise level)
- from now on we will work with negative log-likelihood cost

$$V_1ig(
ho(l,r)ig) = -\log p_1ig(
ho(l,r)ig)$$
 smaller is better

• we should also define similarity (and negative log-likelihood  $V_0(
ho(l,r))$ ) for non-matches

(39)

### ►A Principled Approach to Matching: Formulating 'What We Want'

- given matching M in table T, what is the likelihood of observed data D?
- data all cost pairs  $(V_0, V_1)$  in the matching table T
- matches pairs  $p_i = (l_i, r_i) \in M \subset T$ ,  $i = 1, \dots, n$
- matching: partitioning matching table T to matched M and excluded E pairs

$$T = M \cup E, \quad M \cap E = \emptyset$$

matching cost (negative log-likelihood, smaller is better)

$$V(D \mid M, T) = \sum_{p \in M} V_1(D \mid p) + \sum_{p \in T \setminus M} V_0(D \mid p)$$

$$V_1(D \mid p)$$
 – negative log-probability of data  $D$  at matched pixel  $p$  (39)  $V_0(D \mid p)$  – ditto at unmatched pixel  $p$ 

matching problem

$$M^* = \arg\min_{M \in \mathcal{M}(T)} V(D \mid M, T)$$

- $\mathcal{M}(T)$  the set of all matchings in table T
- symmetric: formulated over pairs, invariant to left  $\leftrightarrow$  right image swap



constant number of variables in  ${\boldsymbol{T}}$ 

unlike in WTA

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# ►(cont'd) Log-Likelihood Ratio

- we need to reduce the matching to a standard polynomial-complexity problem
- 1. convert the matching cost to an 'easier' sum

$$V(D \mid M, T) = \sum_{p \in M} V_1(D \mid p) + \sum_{p \in T \setminus M} V_0(D \mid p) + \underbrace{\sum_{p \in M} V_0(D \mid p) - \sum_{p \in M} V_0(D \mid p)}_{= \sum_{p \in M} \underbrace{\left(V_1(D \mid p) - V_0(D \mid p)\right)}_{-L(D \mid p)} + \underbrace{\sum_{p \in T \setminus M} V_0(D \mid p) + \sum_{p \in M} V_0(D \mid p)}_{\sum_{p \in T} V_0(D \mid p) = \text{const}}$$

2. hence

$$\arg\min_{M\in\mathcal{M}(T)} V(D\mid M) = \arg\max_{M\in\mathcal{M}(T)} \sum_{p\in M} L(D\mid p)$$
(40)

 $L(D \mid p)$  – logarithm of matched-to-unmatched likelihood ratio (bigger is better)

why this way: we want to use maximum-likelihood on the entire  ${\boldsymbol{T}}$ 

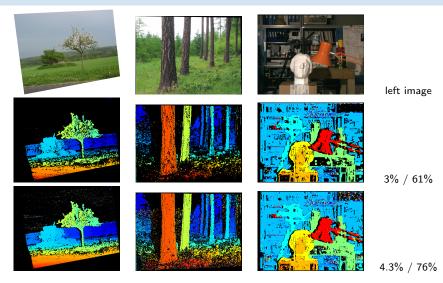
0

3. (40) is max-cost matching (maximum assignment) for the maximum-likelihood (ML) matching problem

• use the Hungarian (Munkres) algorithm and threshold the result with  $\tau$ :  $L(D \mid p) > \tau \ge 0$ 

or approximate the problem by sacrificing symmetry and accuracy to speed and use dynamic programming

### Some Results for the Maximum-Likelihood (ML) Matching



- unlike the WTA we can efficiently control the density/accuracy tradeoff with  $\tau$
- middle row: threshold  $\tau$  for  $L(D \mid p)$  set to achieve error rate of 3% (and 61% density results)
- bottom row: threshold  $\tau$  set to achieve density of 76% (and 4.3% error rate results)

black = no match

Thank You



