Artificial intelligence in robotics 2019 —

Autonomous Navigation

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- The art of getting from one place to another, safely and efficiently.
- The process of monitoring and controlling the movement of a craft or vehicle from one place to another.
- The activity of accurately ascertaining one's position and planning and following a route.
- As stated in [1], to navigate, one must answer the following three questions:

"Where am I?", "Where am I going?", "How do I get there?"

- The art of getting from one place to another, safely and efficiently.
- The process of monitoring and controlling the movement of a craft or vehicle from one place to another.
- The activity of accurately ascertaining one's position and planning and following a route.
- As stated in [1], to navigate, one must answer the following three questions:

Localisation, "Where am I going?", "How do I get there?"

- The art of getting from one place to another, safely and efficiently.
- The process of monitoring and controlling the movement of a craft or vehicle from one place to another.
- The activity of accurately ascertaining one's position and planning and following a route.
- As stated in [1], to navigate, one must answer the following three questions:

Localisation,

Mapping,

"How do I get there?"

- The art of getting from one place to another, safely and efficiently.
- The process of monitoring and controlling the movement of a craft or vehicle from one place to another.
- The activity of accurately ascertaining one's position and planning and following a route.
- As stated in [1], to navigate, one must answer the following three questions:

Localisation, Mapping, Motion planning

Lecture overview

Autonomous navigation in mobile robotics can be divided by the way it uses knowledge of the environment [2]:

- 1. Map-less navigation
 - unknown environments with known structure
 - road following, obstacle avoidance
 - observations translate to motion commands
- 2. Map-based navigation
 - known (un)structured environments
 - observations and map translate to motion commands
 - a typical intermediate step is localisation
- 3. Map-building-based navigation
 - observations and map translate to both commands and map update
 - (un)known, (un)structured environments
 - a typical intermediate step is localisation

Apriori known environment structure Sensor data → motion command Design considerations often based on [3]

Pseudo-random

behaviour-based

Optical flow

Lucas-Kanade

Line detection

RANSAC, Hough

Road segmentation

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Video location: videos/flow

Apriori known environment structure Sensor data \rightarrow motion command Design considerations often based on [3]

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Video location: videos/line-detect

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Vid. loc.: videos/road-segmentation

Apriori known environment (pre-build map)

General: $(observations, map) \rightarrow motion command$

Typical: (observations, map) \rightarrow position \rightarrow motion command

Topological map

map-less + direction

Landmark map

image features

Geometric map

CAD, polygons

Occupancy grids

2d, 3d, OctoMap

Memory-based

qualitative nav.



Video location: videos/lama

Apriori known environment (pre-build map)

General: (observations, map) \rightarrow motion command

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Topological map

map-less + direction

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qualitative nav.



Video location: videos/repli

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General: (observations, map) \rightarrow motion command

Typical: (observations, map) \rightarrow position \rightarrow motion command

Topological map

• map-less + direction

Landmark map

image features

Geometric map

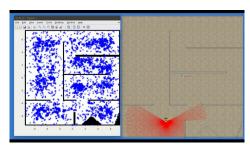
CAD, polygons

Occupancy grids

2d, 3d, OctoMap

Memory-based

qualitative nav.



Video location: videos/mcl

Apriori known environment (pre-build map)

General: (observations, map) \rightarrow motion command

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Topological map

map-less + direction

Landmark map

image features

Geometric map

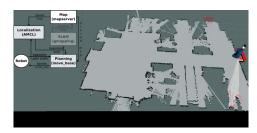
CAD, polygons

Occupancy grids

2d, 3d, OctoMap

Memory-based

qualitative nav.



Video location: videos/2dgrid

Apriori known environment (pre-build map)

General: $(observations, map) \rightarrow motion command$

Typical: (observations, map) \rightarrow position \rightarrow motion command

Topological map

map-less + direction

Landmark map

image features

Geometric map

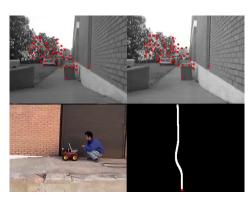
CAD, polygons

Occupancy grids

2d, 3d, OctoMap

Memory-based

qualitative nav.



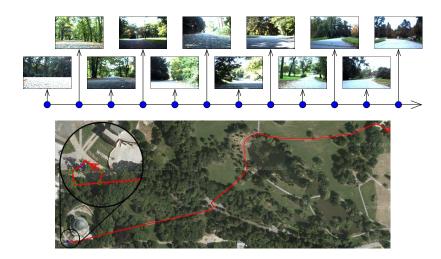
Video location: videos/qualitative

- raw distance between frames,
- local snapshots of the environment,
- robot traverses approximately the same distance,
- steers according to what is sees in front of it.



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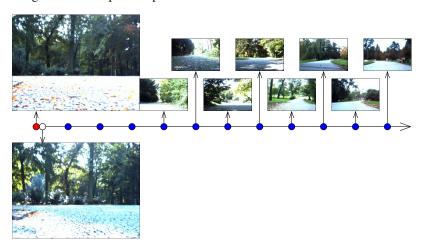
Image sequence indexed by position pics/along the learned path



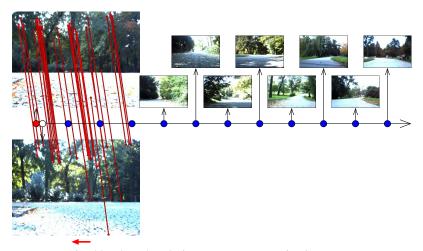
Images stored in a prior map



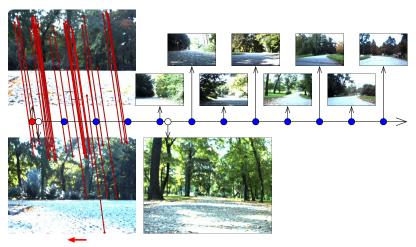
Images stored in a prior map



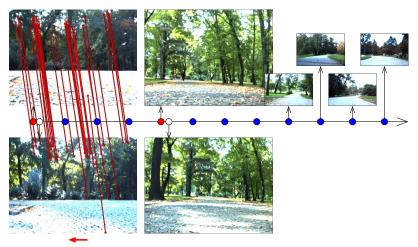
Images stored in a prior map



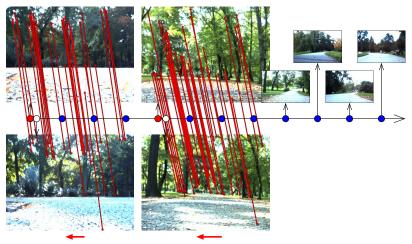
Images stored in a prior map



Images stored in a prior map



Images stored in a prior map



Images stored in a prior map

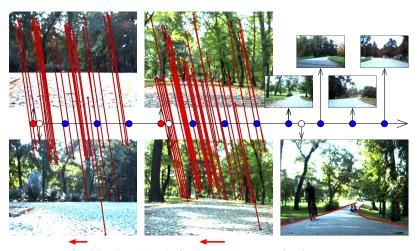


Image perceived by the robot during autonomous navigation

Images stored in a prior map

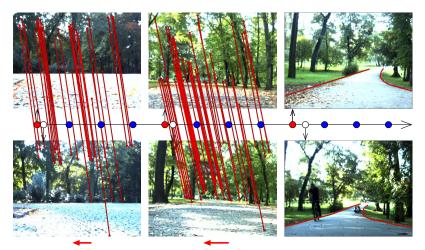


Image perceived by the robot during autonomous navigation

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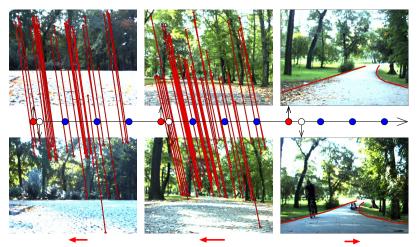
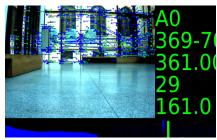


Image perceived by the robot during autonomous navigation

Autonomous navigation along a polygonal path Discrete motion model

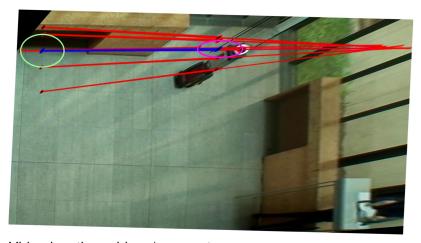
- Move forwards,
- get features from map,
- get features from image,
- establish matches.
- steer by histogram voting,
- stop and turn when odometry exceeds segment length.



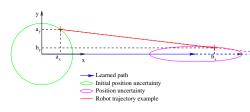
Video location: videos/navigate



Video location: videos/segment



Video location: videos/segment

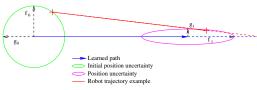


Robot position coordinates

$$b_x = a_x + s(1+v),$$

$$b_y = ma_y + \xi.$$

m - heading correction ξ, v - errors (odo+cam)



Robot position coordinates

$$b_x = a_x + s(1+v),$$

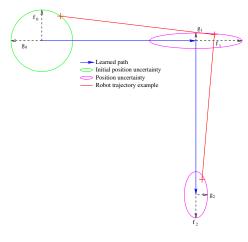
$$b_y = ma_y + \xi.$$

m - heading correction ξ, v - errors (odo+cam)

Position error ellipse axes

$$f_{i+1} = g_i + v,$$

$$g_{i+1} = mf_i + \xi$$



Robot position coordinates

$$b_x = a_x + s(1 + v),$$

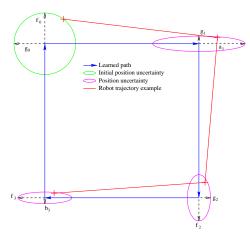
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Position error ellipse axes

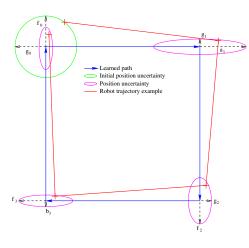
$$f_{i+1} = g_i + v,$$

$$g_{i+1} = mf_i + \xi$$

Convergence

$$\begin{split} f_{\infty} &= (\xi + v)/(1-m) \\ f_{\infty}, \, g_{\infty} \text{ finite if } \|m\| < 1. \end{split}$$

Example map-based navigation - discrete error model



Robot position coordinates

$$b_x = a_x + s(1 + v),$$

$$b_y = ma_y + \xi.$$

m - heading correction ξ, υ - errors (odo+cam)

Position error ellipse axes

$$f_{i+1} = g_i + v,$$

$$g_{i+1} = mf_i + \xi$$

Convergence

$$\begin{split} f_{\infty} &= (\xi + v)/(1-m) \\ f_{\infty}, \, g_{\infty} \text{ finite if } \|m\| < 1. \end{split}$$

Example map-based navigation - discrete error model

Robot position vector

$$\left(\begin{array}{c}b_x\\b_y\end{array}\right)=\left(\begin{array}{cc}1&0\\0&m\end{array}\right)\left(\begin{array}{c}a_x\\a_y\end{array}\right)+\left(\begin{array}{c}s+s\upsilon\\\xi\end{array}\right) \begin{array}{c}\text{coordinates}\\b_x=a_x+s(1+\upsilon),\end{array}$$

Becomes

 $\mathbf{b} = \mathbf{R^T}(\mathbf{MRa} + \mathbf{s}) = \mathbf{Na} + \mathbf{t}$ for a segment with arbitrary azimuth R

Position error covariance matrix

$$\mathbf{A_{i+1}} = \mathbf{N_i} \mathbf{A_i} \mathbf{N_i^T} + \mathbf{T_i}$$

Convergence

 $\mathbf{A}_{\infty} = \breve{\mathbf{N}} \mathbf{A}_{\infty} \breve{\mathbf{N}} + \breve{\mathbf{T}}$ (Lyapunov equation) A_{∞} exists and is finite iff

$$\|\mathbf{\check{N}}\| < 1$$

$$\ddot{\mathbf{N}} = \prod_{i=1}^{n} \mathbf{N_i} = \prod_{n=1}^{n} \mathbf{R_i^T N_i R_i}$$

Robot position

$$b_x = a_x + s(1 + v),$$

$$b_y = ma_y + \xi.$$

m - heading correction ξ, v - errors (odo+cam)

Position error ellipse axes

$$f_{i+1} = g_i + v,$$

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Example map-based navigation - discrete error model

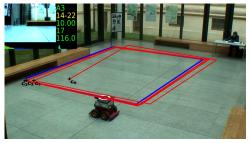
Experimental evaluation:

- 1. Teach a closed path,
- 2. displace at start,
- 3. traverse n times,
- 4. measure c_i ,
- 5. compute ε_{acc} , ε_{acc} .

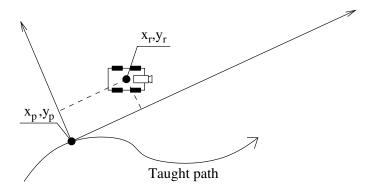
$$\varepsilon_{acc} = \sqrt{\frac{1}{n-j} \sum_{i=j}^{n} \left\| \mathbf{c_i} \right\|^2}$$

$$\varepsilon_{rep} = \sqrt{\frac{1}{n-j} \sum_{i=j}^{n} \left\| \mathbf{c_i}, \mu \right\|^2}$$

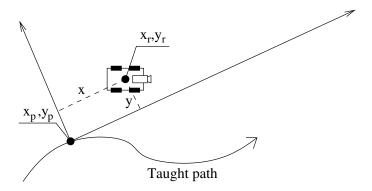
$$\mu = \sum_{i=j}^{n} \mathbf{c_i} / (n-j)$$



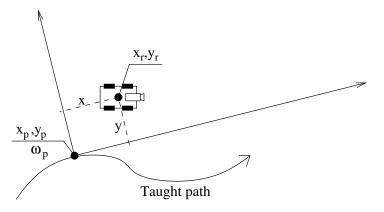
Video location: videos/converge



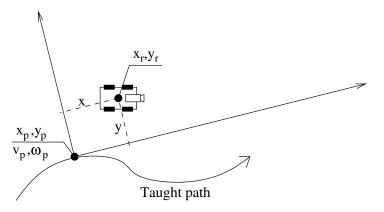
$$\dot{x} = \dot{x} = 0$$



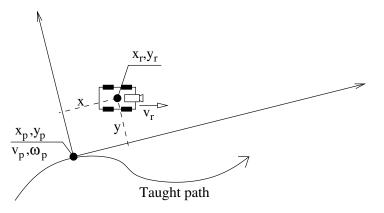
$$\dot{x} = \dot{x} = 0$$



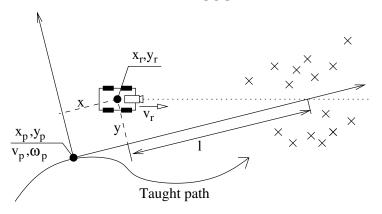
$$\dot{x} = +\omega_p y
\dot{y} = -\omega_p x$$



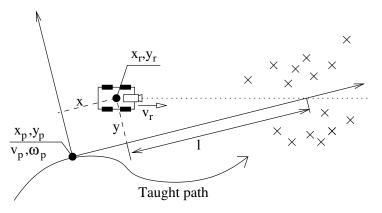
$$\dot{x} = +\omega_p y - v_p
\dot{y} = -\omega_p x$$



$$\begin{array}{llll} \dot{x} & = & +\omega_p \, y & -v_p & +v_r \\ \dot{y} & = & -\omega_p \, x \end{array}$$



$$\begin{array}{rclcrcl} \dot{x} & = & +\omega_p \, y & -v_p & +v_r \\ \dot{y} & = & -\omega_p \, x & & -v_r \, y \, l^{-1} \end{array}$$



$$\begin{array}{lclcrcl} \dot{x} & = & +\omega_p \, y & -v_p & +v_r & +s_x \\ \dot{y} & = & -\omega_p \, x & & -v_r \, y \, l^{-1} & +s_y \end{array}$$

$$\dot{x} = + \omega_p y - v_p + v_r + s_x$$

 $\dot{y} = - \omega_p x - v_r y l^{-1} + s_y$

$$\dot{x} = + \omega_p y - v_p + v_r + s_x$$

 $\dot{y} = - \omega_p x - v_r y l^{-1} + s_y$

Matrix form:

$$\begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix} = \begin{pmatrix} 0 & +\omega_p \\ -\omega_p & -v_r l^{-1} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} s_x \\ s_y \end{pmatrix},$$

$$\dot{x} = + \omega_p y - v_p + v_r + s_x$$

 $\dot{y} = - \omega_p x - v_r y l^{-1} + s_y$

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Matrix eigenvalues:

$$\lambda^2 + \lambda \frac{v_r}{I} + \omega_p^2 = 0,$$

$$\dot{x} = + \omega_p y - v_p + v_r + s_x$$

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Matrix eigenvalues:

$$\lambda^2+\lambda\frac{v_r}{l}+\omega_p^2=0,$$

$$v_r>0,\ l>0\implies Re(\lambda_{1,2})<0\ \text{iff}\ \omega_p\neq0.$$

$$\dot{x} = + \omega_p y - v_p + v_r + s_x$$

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Matrix form:

$$\begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix} = \begin{pmatrix} 0 & +\omega_p \\ -\omega_p & -v_r l^{-1} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} s_x \\ s_y \end{pmatrix},$$

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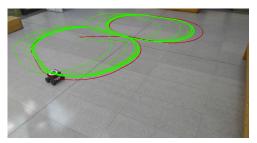
$$v_r>0,\ l>0\implies Re(\lambda_{1,2})<0\ \text{iff}\ \omega_p\neq0.$$

Position error decreases if path is not only a straight line.

Experimental evaluation similar to the discrete case

- 1. Teach a closed path,
- 2. displace at start,
- 3. traverse *n* times,
- 4. measure c_i ,
- 5. compute ε_{acc} , ε_{acc} .

$$\begin{array}{lcl} \varepsilon_{acc} & = & \sqrt{\frac{1}{n-j}\sum_{i=j}^{n}\left\|\mathbf{c_{i}}\right\|^{2}} \\ \varepsilon_{rep} & = & \sqrt{\frac{1}{n-j}\sum_{i=j}^{n}\left\|\mathbf{c_{i}},\mu\right\|^{2}} \\ \mu & = & \sum_{i=j}^{n}\mathbf{c_{i}}/(n-j) \end{array}$$



Video location: videos/continuos

Lecture wrap up: what to remember

What to remember

- Mobile robot navigation type can be divided by the map usage, which assume different prior knowledge and thus handle the robot observations in different ways. [1]
- Although simple, mapless navigation is commonly used in commercially-successfull systems (Roomba, Tesla etc). [2]
- Map-based navigation typically uses localisation [3], but it is not necessary for teach-and-repeat systems [4].

References

- [1] DeSouza et al.: Vision for mobile robot navigation: A survey. IEEE PAMI, 2002
- [2] Brooks: Intelligence without representation. Al 1991
- [3] Filiat and Meyer: Map-based navigation in mobile robots: A review... Cog.Sys. Research 2003.
- [4] Krainik et al.: Navigation without localisation ... In IROS 2018.