Text Search

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PAL 2012

- Nondeterministic Finite Automata
- Transformation NFA to DFA and Simulation of NFA
- Text Search Using Automata
- Power of Nondeterministic Approach
- Regular Expression Search
- Dealing with ε–transitions

Languages, grammars, automata

Czech instant sources:
[1] M. Demlová: **A4B01JAG**
http://math.feld.cvut.cz/demlova/teaching/jag/
Pages 1-27, in PAL, you may wish to skip: Proofs, chapters 2.4, 2.6, 2.8.

[2] I. Černá, M. Křetínský, A. Kučera: **Automaty a formální jazyky I**
http://is.muni.cz/do/1499/el/estud/fi/js06/ib005/Formalni_jazyky_a_automaty_I.pdf
Chapters 1 and 2, skip same parts as in [1].

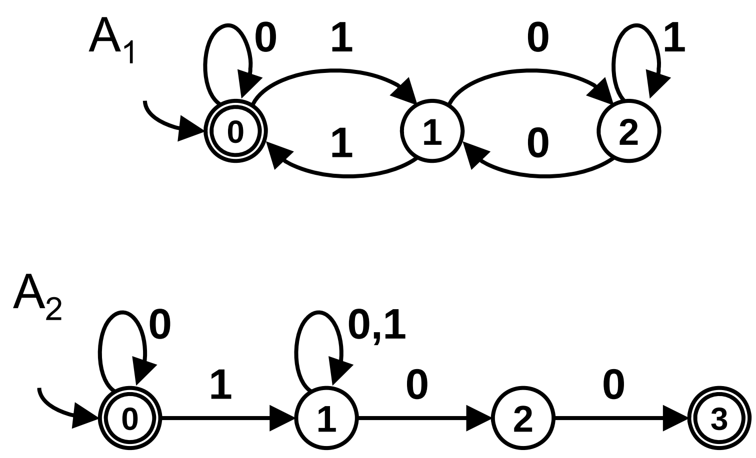
English sources:
[3] B. Melichar, J. Holub, T. Polcar: **Text Search Algorithms**
http://cw.felk.cvut.cz/lib/exe/fetch.php/courses/a4m33pal/melichar-tsa-lectures-1.pdf
Chapters 1.4 and 1.5, it is probably reasonably short, there is nothing to skip.

[4] J. E. Hopcroft, R. Motwani, J. D. Ullman: **Introduction to Automata Theory**
folow the link at http://cw.felk.cvut.cz/doku.php/courses/a4m33pal/literatura_odkazy
Chapters 1., 2., 3., there is a lot to skip, consult the teacher preferably.

For more references see PAL links pages
http://cw.felk.cvut.cz/doku.php/courses/b4m33pal/odkazy-zdroje (CZ)
https://cw.fel.cvut.cz/wiki/courses/be4m33pal/references (EN)

Deterministic Finite Automaton (DFA)
Nondeterministic Finite Automaton (NFA)

Both DFA nd NFA consist of:
- Finite input alphabet Σ.
- Finite set of internal states Q.
- One start state $q_0 \in Q$.
- Nonempty set of accept states $F \subseteq Q$.
- Transition function δ.

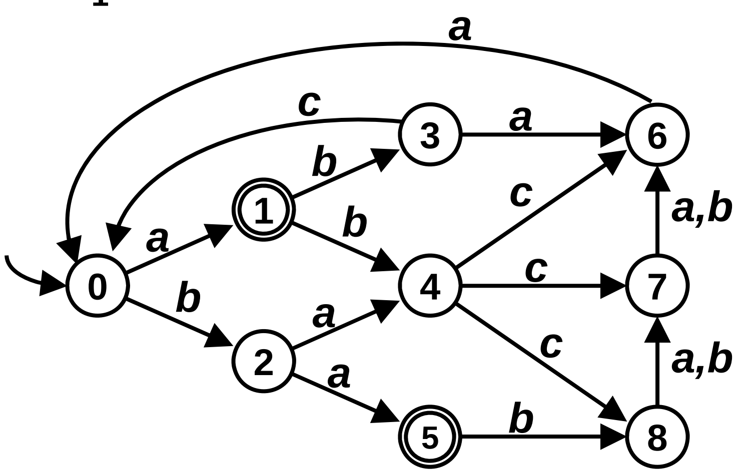


DFA transition function is $\delta: Q \times \Sigma \to Q$.
DFA is always in one of its states $q \in Q$.
DFA transits from current state to another state depending on the current input symbol.

NFA transition function is $\delta: \ Q \times \Sigma \to P(Q)$ ($P(Q)$ is the powerset of Q)
NFA is always (simultaneously) in a set of some number of its states.
NFA transits from set of current states to another set of states
depending on the current input symbol.

NFA $\mathbf{A_1}$, its transition diagram and its transition table

$\mathbf{A_1}$

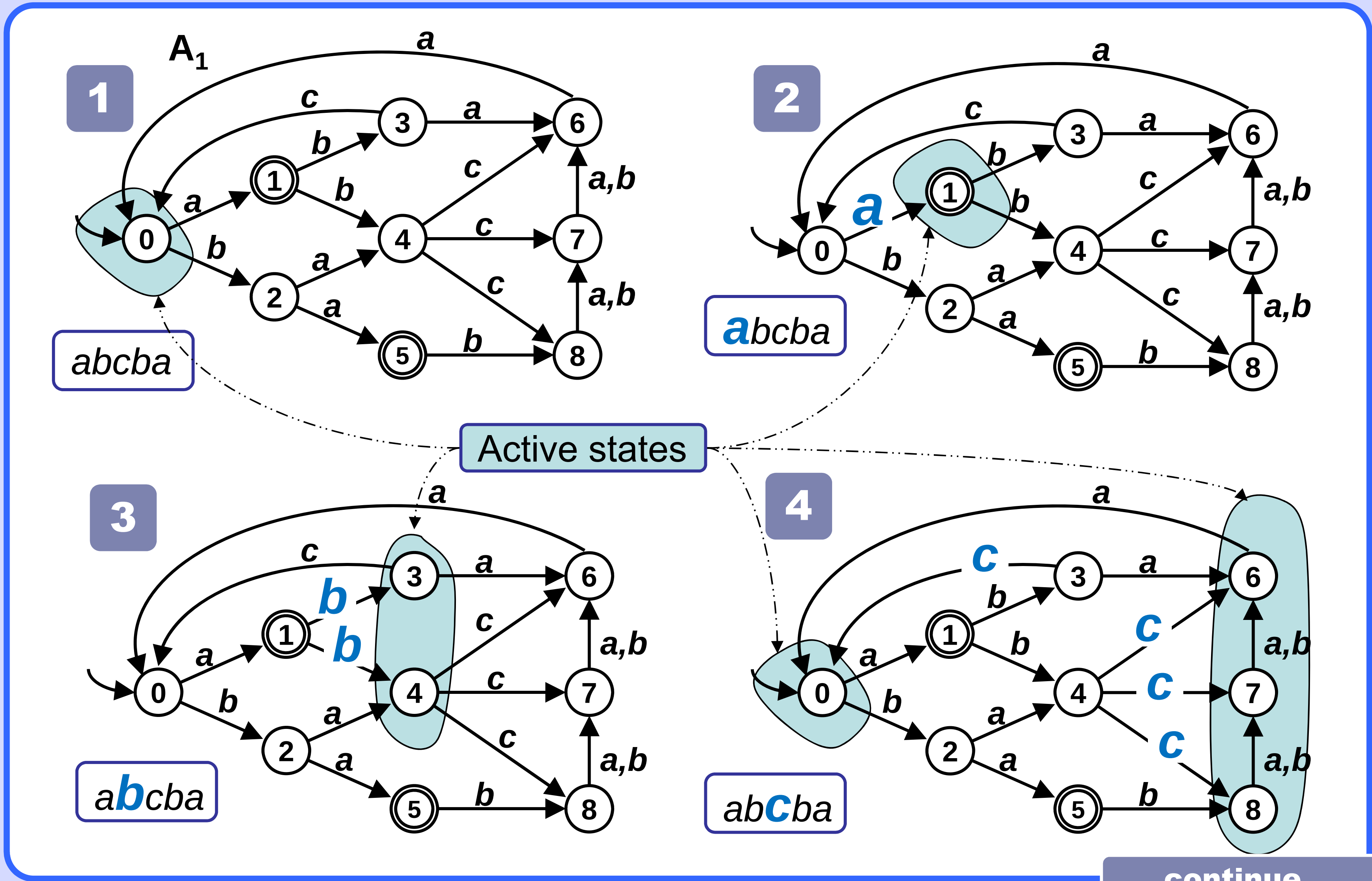


alphabet

states	*a*	*b*	*c*	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

accept states marked

NFA $\mathbf{A_1}$ processing input word *abcba*



continue...

...continued

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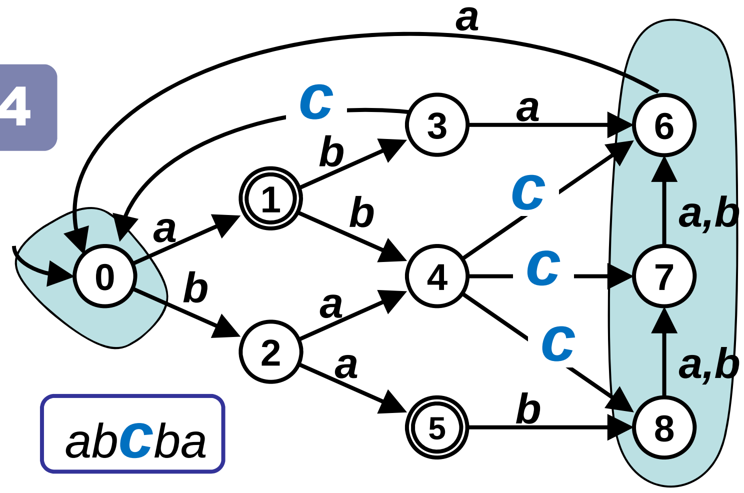

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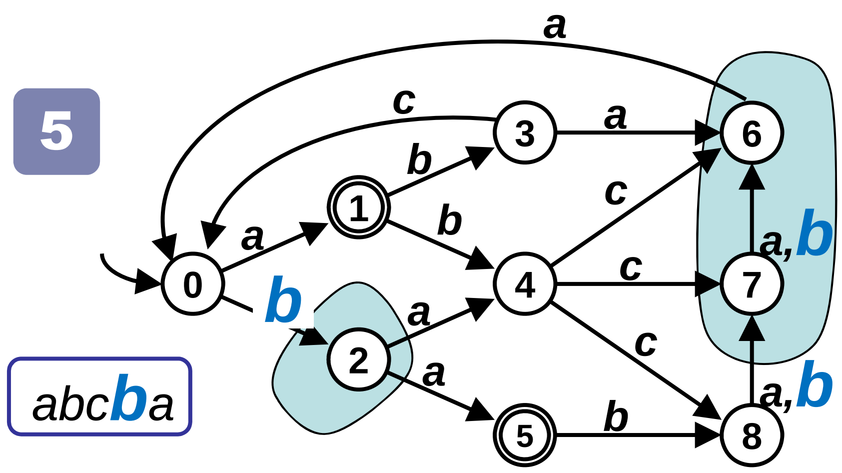

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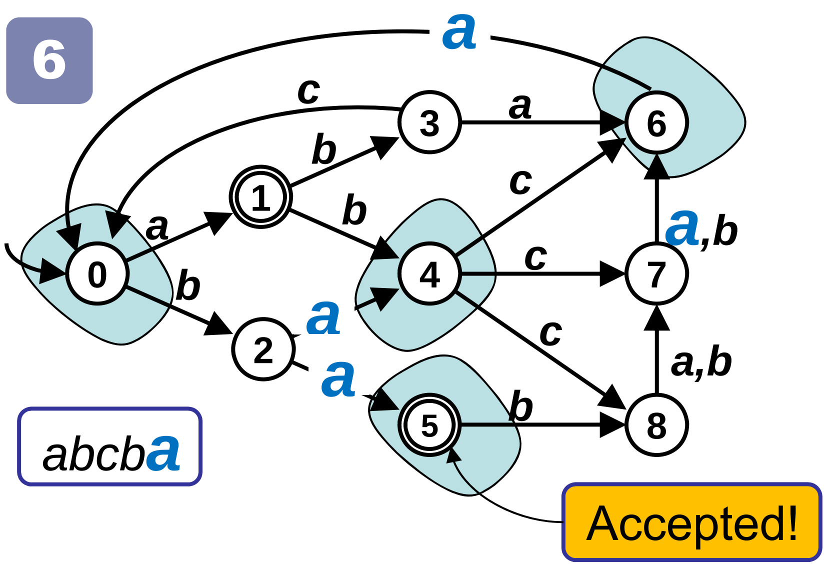


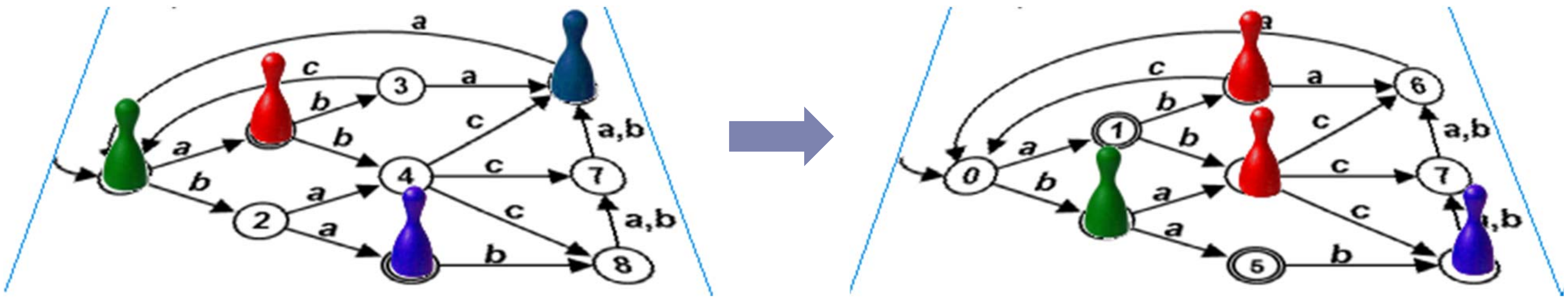
NFA $\mathbf{A_1}$ has processed the word *abcba* and went through the input characters and respective sets(!) of states

{0} → a → {1} → b → {3, 4} → c →
→ {0, 6, 7, 8} → b → {2, 6, 7} → a →
→ {0, 4, 5, 6}.

NFA simulation without transform to DFA

Each of the current states is occupied by one token.
Read an input symbol and move the tokens accordingly.
If a token has more movement possibilities it will split into two or more tokens,
if it has no movement possibility it will leave the board, uhm, the transition diagram.

Read **b** from input



NFA simulation without transform to DFA

Idea:
Register all states to which you have just arrived. In the next step, read the input symbol ***x*** and move SIMULTANEOUSLY to ALL states to which you can get from ALL active states along transitions marked by ***x***.

Input: NFA , text in array **t**

```
SetOfStates S = {q0}, S_tmp;

i = 1;
while( (i <= t.length) && (!S.isEmpty()) ) {
  S_tmp = Set.emptySet();
  for( q in S )                    // for each state in S
    S_tmp.union( delta(q, t[i]) );
  S = S_tmp;
  i++;
}
return S.containsFinalState();   // true or false
```

Generating DFA $\mathbf{A_2}$ equivalent to NFA $\mathbf{A_1}$ using transition tables

Data

Each state of DFA is a subset of states of NFA.
Start state of DFA is an one-element set containing the start state of NFA.
A state of DFA is an accept state iff it contains at least one accept state of NFA.

Construction

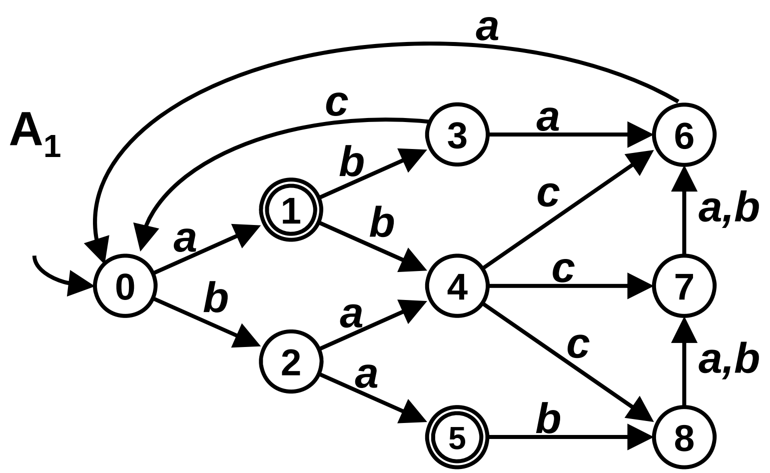
Create the start state of DFA and the corresponding first line of its transition table (TT).

```
For each state Q of DFA not yet processed do {
   Decompose Q into its constituent states Q1, ..., Qk of NFA
    For each symbol x of alphabet do {
       S = union of all references in NFA table at positions [Q1] [x], ..., [Qk][x]
        if (S is not among states of DFA yet)
             add S to the states of DFA and add a corresponding line to TT of DFA
        TT[Q][x] := S
     } // for each symbol
  Mark Q as processed
} // for each state
```

// Remember, empty set is also a set ot states, it can be a state of DFA

Generating DFA A_2 equivalent to NFA A_1

	a	b	c	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		



Copy start state

A_2

	a	b	c
0	1	2	
...			

Add new state(s)

	a	b	c
0	1	2	
1			
2			
...			

continue...

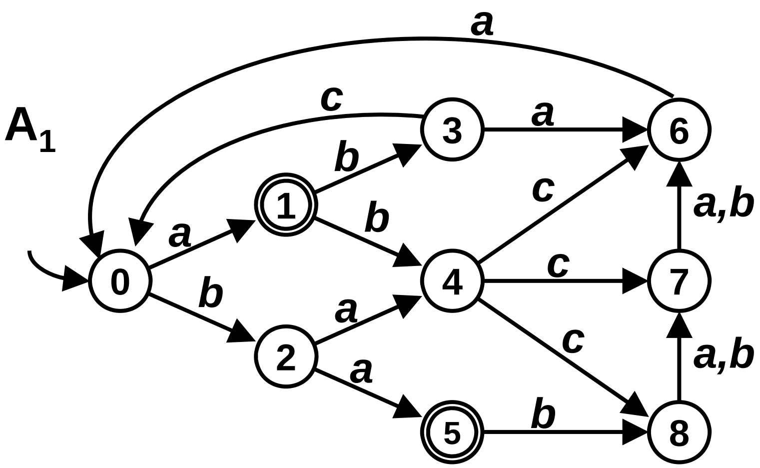
Generating DFA A_2 equivalent to NFA A_1

	a	b	c	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

Add new state(s)

A_2

	a	b	c	
0	1	2		
1		34		F
2				
34				
...				



continue...

Generating DFA A_2 equivalent to NFA A_1

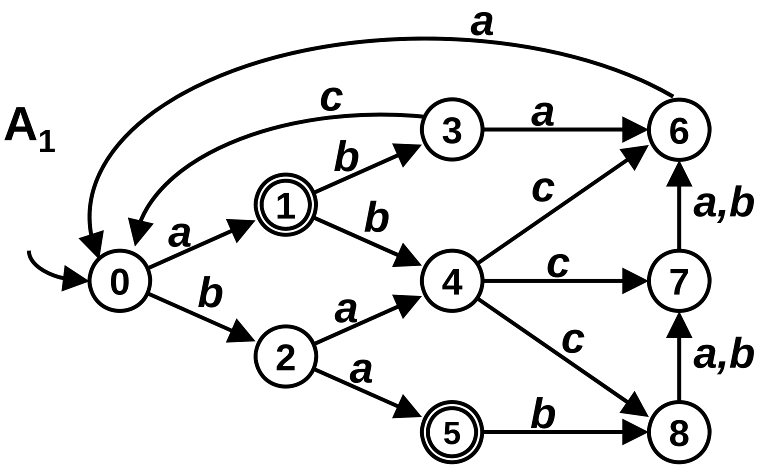
	a	b	c	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

Add new state(s)

A_2

	a	b	c	
0	1	2		
1		34		F
2	45			
34				
45				
...				

A_1



continue...

Generating DFA $\mathbf{A_2}$ equivalent to NFA $\mathbf{A_1}$

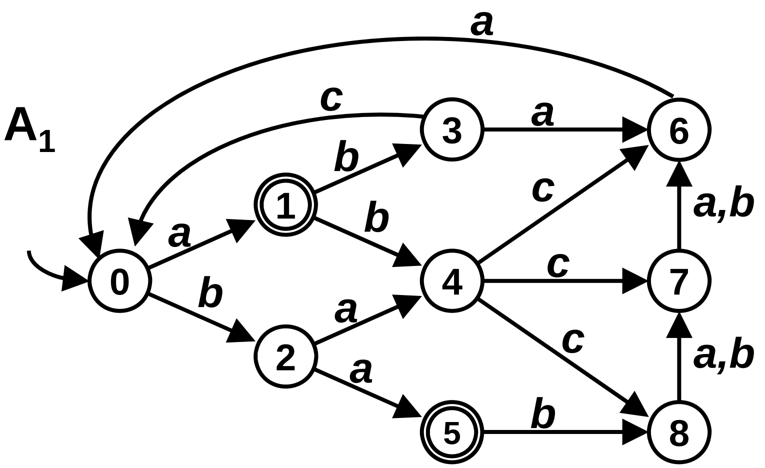
	a	*b*	*c*	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

Add new state(s)

A_2

	a	*b*	*c*	
0	1	2		
1		34		F
2	45			
34	6		0678	
45				
6				
0678				
...				

A_1



continue...

Generating DFA A_2 equivalent to NFA A_1

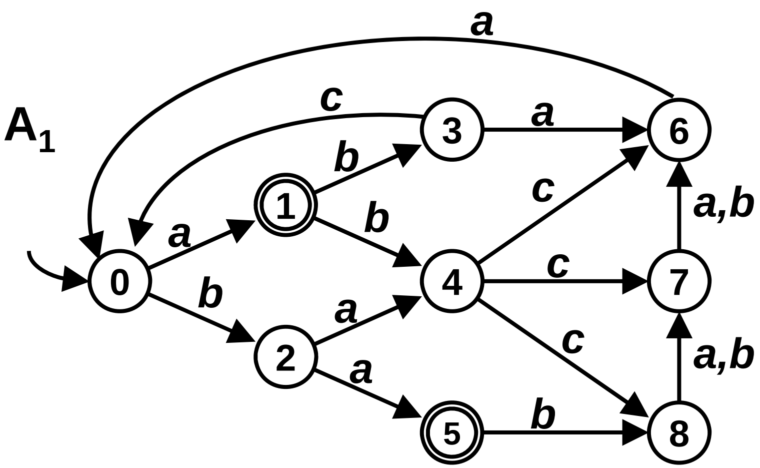
	a	b	c	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

Add new state(s)

A_2

	a	b	c	
0	1	2		
1		34		F
2	45			
34	6		0678	
45		8	678	F
6				
0678				
8				
678				
...				

A_1



continue...

Generating DFA A_2 equivalent to NFA A_1

	a	*b*	*c*	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

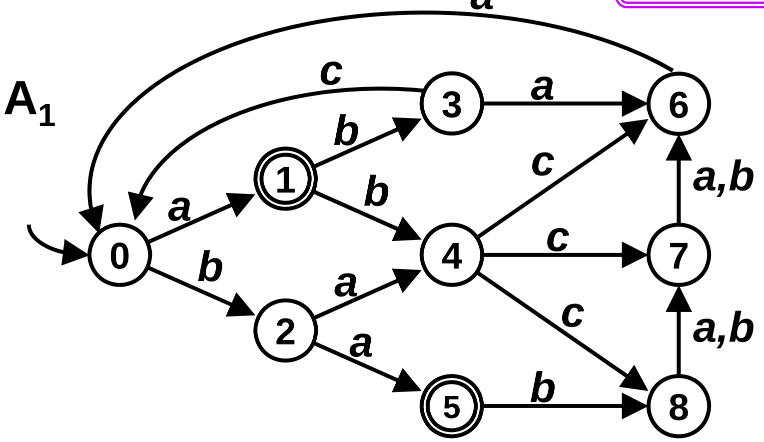
Add new state(s)

A_2

	a	*b*	*c*	
0	1	2		
1		34		F
2	45			
34	6		0678	
45		8	678	F
6	0			
0678				
8				
678				
...				

No new state

A_1

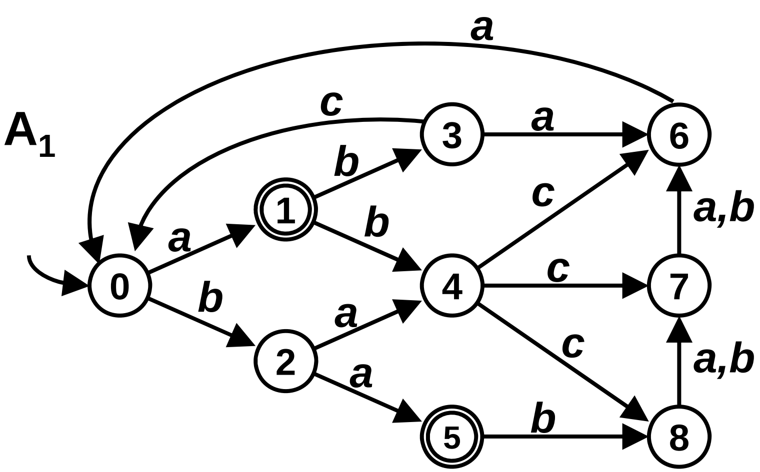


continue...

Generating DFA A_2 equivalent to NFA A_1

	a	*b*	*c*	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

A_1



Add new state(s)

A_2

	a	*b*	*c*	
0	1	2		
1		34		F
2	45			
34	6		0678	
45		8	678	F
6	0			
0678	0167	267		
8				
678				
0167				
267				
...				

continue...

Generating DFA A_2 equivalent to NFA A_1

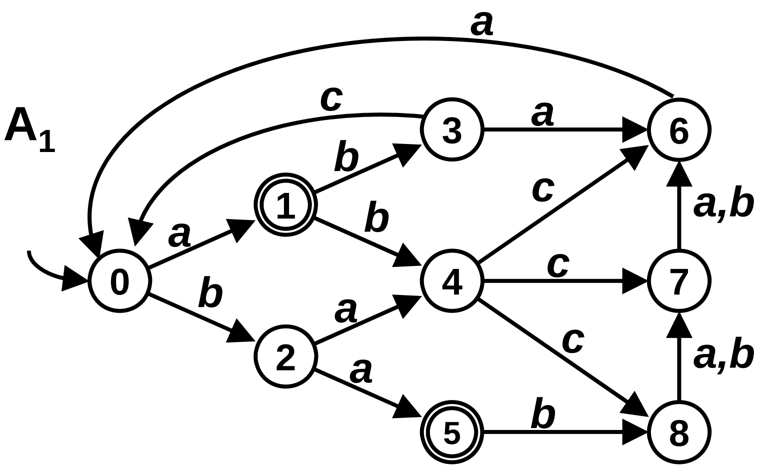
	a	*b*	*c*	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

Add new state(s)

A_2

	a	*b*	*c*	
0	1	2		
1		34		F
2	45			
34	6		0678	
45		8	678	F
6	0			
0678	0167	267		
8	7	7		
678				
0167				
267				
7				
...				

A_1

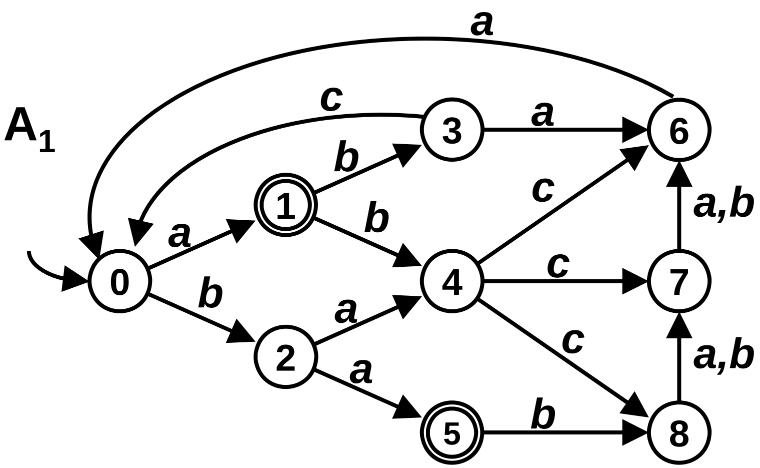


continue...

Generating DFA A_2 equivalent to NFA A_1

	a	*b*	*c*	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

A_1



A_2

Add new state(s)

	a	*b*	*c*	
0	1	2		
1		34		F
2	45			
34	6		0678	
45		8	678	F
6	0			
0678	0167	267		
8	7	7		
678	067	67		
0167				F
267				
7				
067				
67				
...				

continue...

continue...

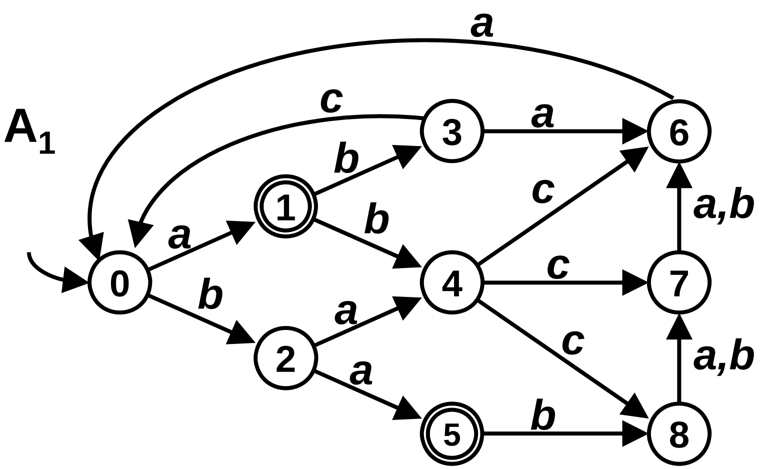
continue...

DFA A_2 equivalent to NFA A_1

...FINISHED!

	a	b	c	
0	1	2		
1		3,4		F
2	4,5			
3	6		0	
4			6,7,8	
5		8		F
6	0			
7	6	6		
8	7	7		

A_1



A_2

	a	b	c	
0	1	2	n	
1	n	34	n	F
2	45	n	n	
34	6	n	0678	
45	n	8	678	F
6	0	n	n	
0678	0167	267	n	
8	7	7	n	
678	067	67	n	
0167	016	2346	n	F
267	0456	6	n	
7	6	6	n	
067	016	2346	n	
67	06	6	n	
016	01	234	n	F
2346	0456	n	0678	
0456	01	28	678	F
06	01	2	n	
01	1	234	n	F
234	456	n	0678	
28	457	7	n	
456	0	8	678	F
457	6	68	678	F
68	07	7	n	
07	16	26	n	
16	0	34	n	
26	045	n	n	
654	1	28	678	F
n	n	n	n	

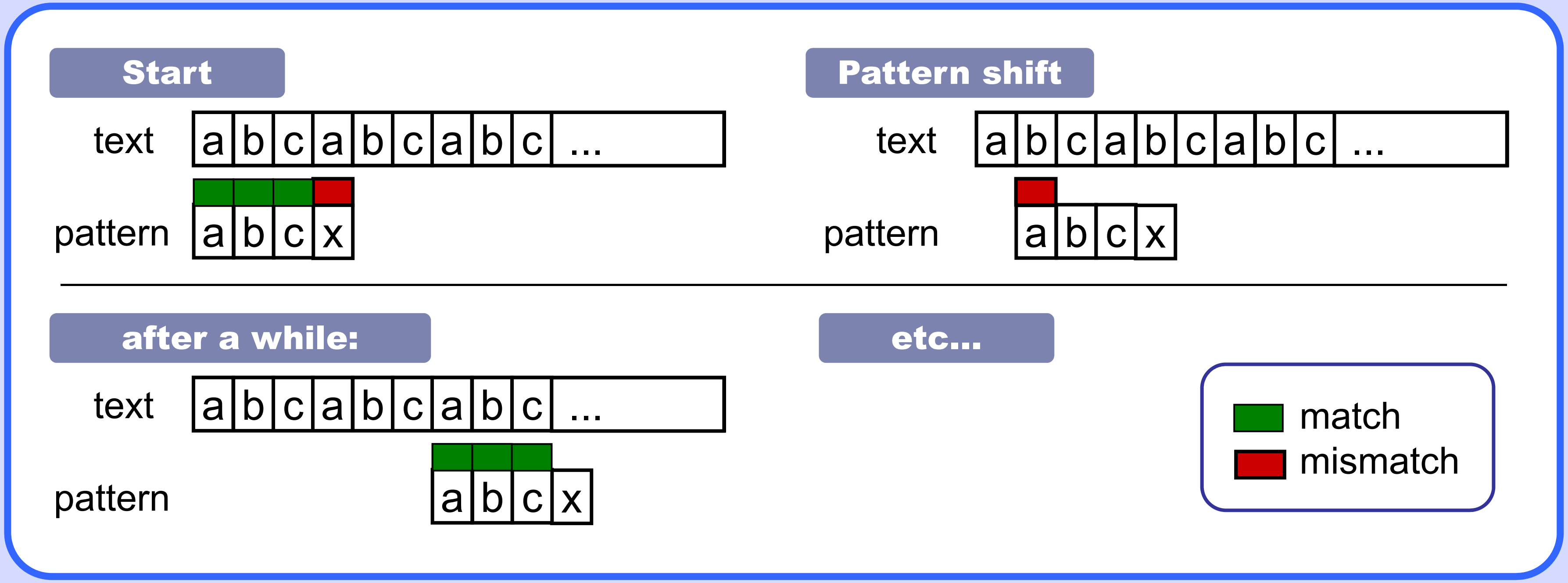
Text Search

To be used with great caution!

Naïve approach

1. Align the pattern with the beginning of the text.
2. While corresponding symbols of the pattern and the text match each other
   move forward by one symbol in the pattern.
3. When symbol mismatch occurs shift the pattern forward by one symbol, reset position in the pattern to the beginning of the pattern and go to 2.
4. When the end of the pattern is passed report success, shift the pattern forward by one symbol, reset position in the pattern to its beginning and go to 2.
5. When the end of the text is reached stop.

Might be efficient in a favourable text



Text Search

Alphabet: Finite set of symbols.
Text: Sequence of symbols of the alphabet.
Pattern: Sequence of symbols of the same alphabet.
Goal: Pattern occurence is to be detected in the text.

Text is often fixed or seldom changed, pattern typically varies (looking for different words in the same document), pattern is often significantly shorter than the text.

Notation

Alphabet: Σ

Symbols in the text: $t_1, t_2, \ldots, t_n$.

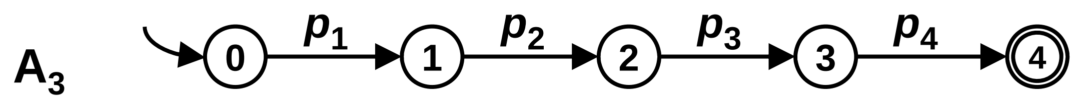
Symbols in the pattern: $p_1, p_2, \ldots, p_m$.

It holds $m \leq n$, usually $m << n$

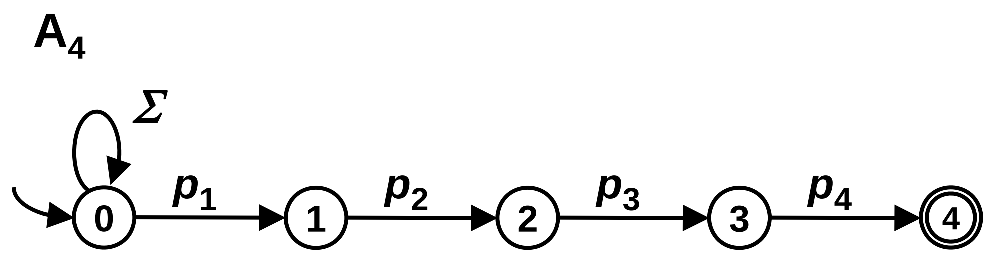
Example

Text: `...task is very simple but it is used very freq...`
Pattern: `simple`

NFA A_3 which accepts just a single word $p_1p_2p_3p_4$.



NFA A_4 which accepts each word with suffix $p_1\ p_2\ p_3\ p_4$ and its transition table.



	p_1	p_2	p_3	p_4	z *)	
0	0,1	0	0	0	0	
1		2				
2			3			
3				4		
4						F

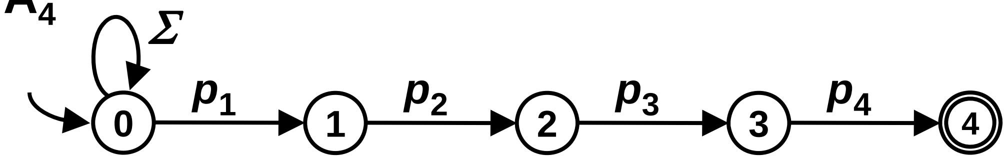
$z \in \Sigma - \{p1, p2, p3, p4\}$

*) *all other characters in the alphabet, each over its own column*

repeated

NFA A_4 which accepts
each word with suffix $p_1\, p_2\, p_3\, p_4$
and its transition table.

A_4



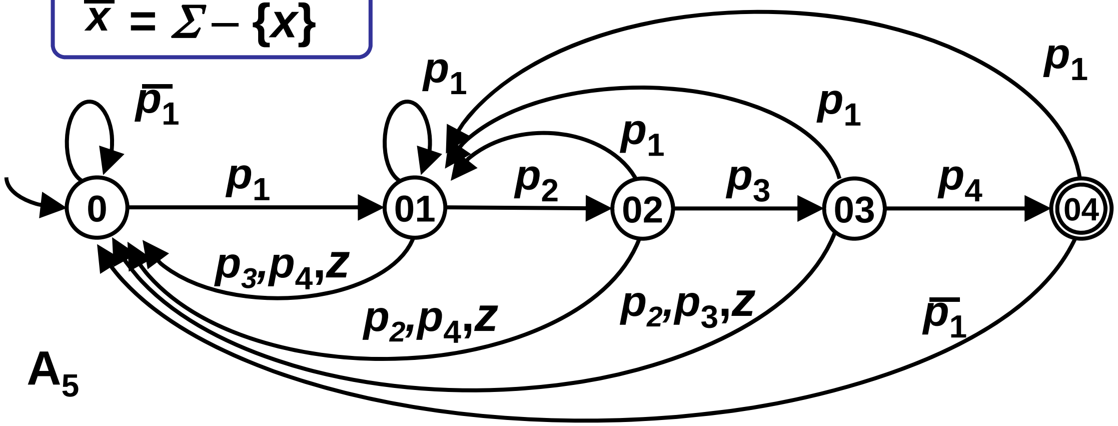
	p_1	p_2	p_3	p_4	z	
0	0,1	0	0	0	0	
1		2				
2			3			
3				4		
4						F

$z \in \Sigma - \{p1, p2, p3, p4\}$

equivalently

DFA A_5 is a deterministic equivalent of NFA A_4.

$\overline{x} = \Sigma - \{x\}$



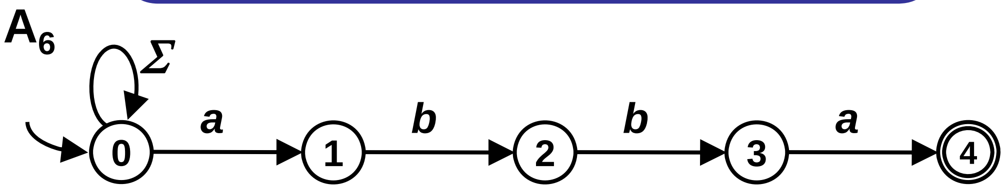
A_5

	p_1	p_2	p_3	p_4	z	
0	01	0	0	0	0	
01	01	02	0	0	0	
02	01	0	03	0	0	
03	01	0	0	04	0	
04	01	0	0	0	0	F

Supposing $p_1\, p_2\, p_3\, p_4$ are mutually different!

example

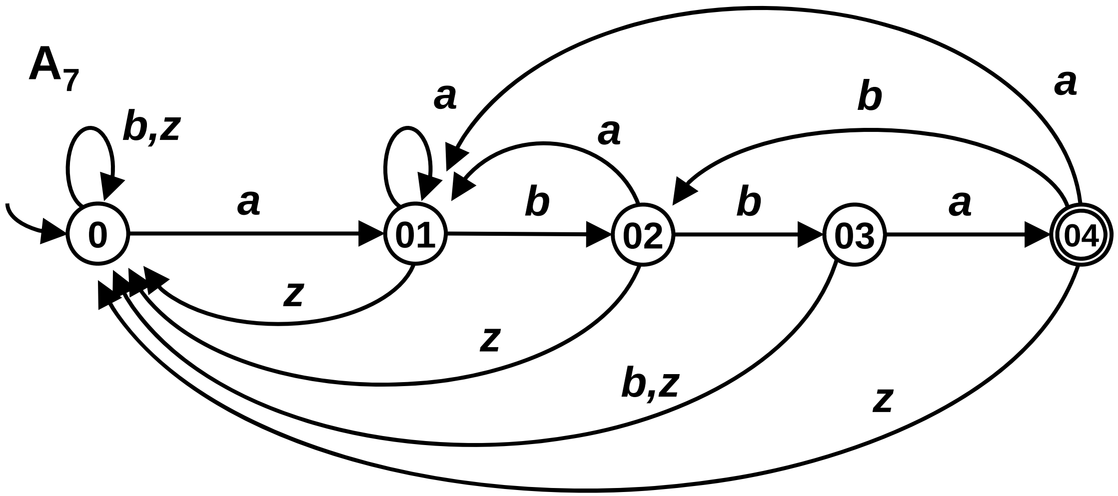
NFA A_6 which accepts
each word with suffix *abba*
and its transition table



	a	*b*	*z*	
0	0,1	0	0	
1		2		
2		3		
3	4			
4				F

$z \in \Sigma - \{a, b\}$

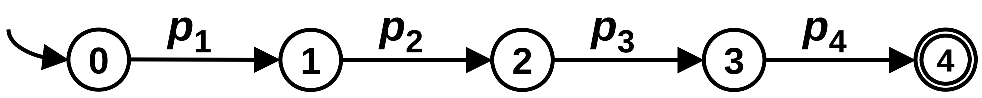
DFA A_7 is a deterministic equivalent of NFA A_6.
It also accepts each word with suffix *abba*.



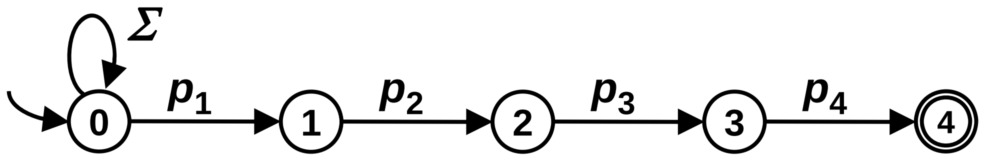
	a	*b*	*z*	
0	01	0	0	
01	01	02	0	
02	01	03	0	
03	014	0	0	
04	01	02	0	F

Note the structural difference between A_5 and A_7.

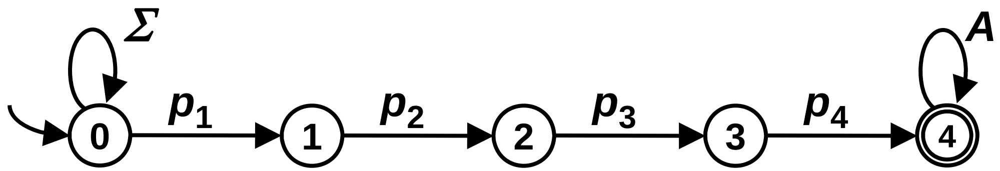
NFA accepting exactly one word $p_1p_2p_3p_4$.



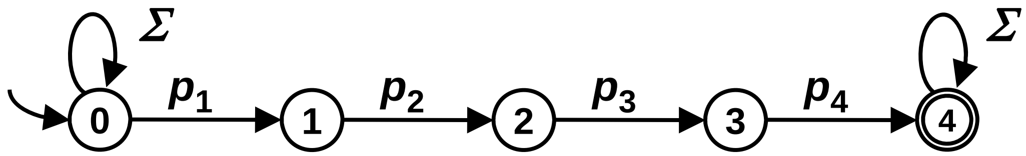
NFA accepting any word with suffix $p_1p_2p_3p_4$.



NFA accepting any word with substring (factor) $p_1p_2p_3p_4$ anywhere in it.

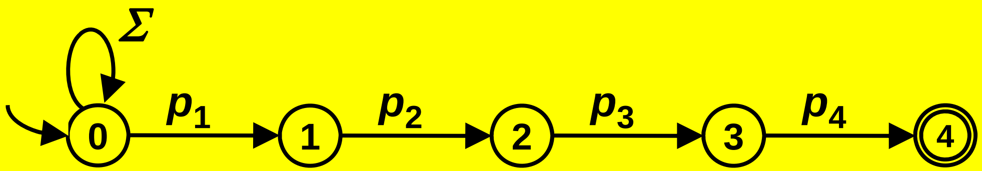


NFA accepting any word with substring (factor) $p_1p_2p_3p_4$ anywhere in it.



Can be used for searching, but the following reduction is more frequent.

Text search NFA for finding pattern $P = p_1p_2p_3p_4$ in the text.



Whenever at least one of the active states is final, report pattern detection in the text.

Note that multiple occurences of the patern in the text, even overlapping ones, are all detected,
due to indeterminism and Sigma-loop in the start state.

Text search automaton

Text search automaton may be defined as a 6-tuple consisting of

1. Finite input alphabet Σ.
2. Finite set of internal states Q.
3. One start state $q_0 \in Q$.
4. Nonempty set of accept states $F \subseteq Q$.
5. Transition function $\delta: \ Q \times \Sigma \rightarrow P(Q)$ ($P(Q)$ is the powerset of Q)
6. Detection function $\chi: \ P(Q) \rightarrow \{0, 1\}$

With the properties:

A. $\forall \alpha \in \Sigma: \quad q_0 \in \delta(q_0, \ \alpha)$ (loop in the start state labeled by the whole alphabet)

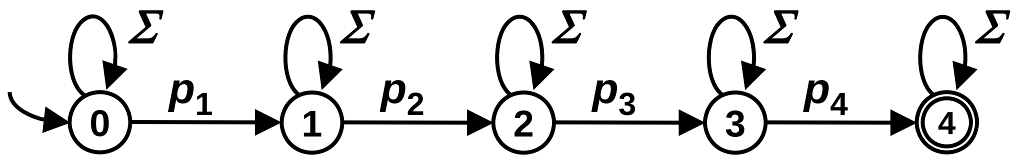
B. $\forall S \subseteq Q: \quad \chi(S) = 1 \ \Leftrightarrow \ S \cap F \neq \varnothing$ (a string in text is detected when χ({active states}) = 1)

Notation and terminology note:
Formally speaking, a text search automaton is clearly neither DFA nor NFA. However, when component 6. and property B are removed from the definition the result is a NFA. This NFA is specified unambiguously by the text search automaton.

Usually, when speaking about "text search NFA x" we keep in mind a "text search automaton y", from which x is obtained by removing component 6 and property B.
The rest of the slides follows this slightly inexact terminology, as do also many other sources.

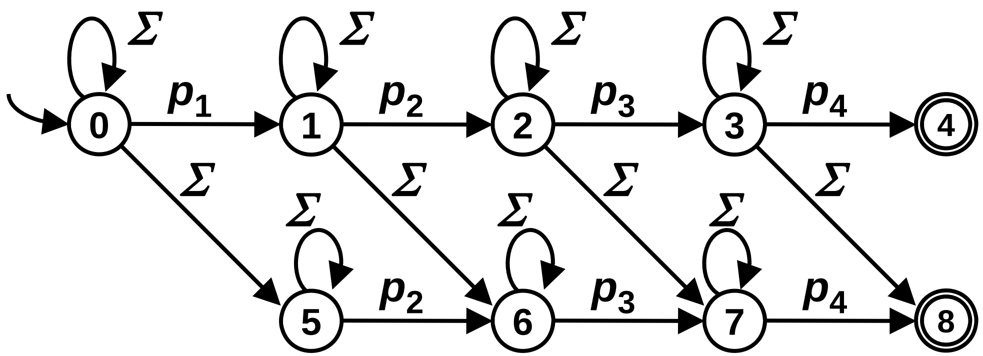
Example

NFA accepting any word with subsequence $p_1p_2p_3p_4$ anywhere in it.



Example

NFA accepting any word with subsequence $p_1p_2p_3p_4$ anywhere in it, one symbol in the sequence may be altered.



Alternatively: NFA accepting any word containing a subsequence Q whose Hamming distance from $p_1p_2p_3p_4$ is at most 1.

Languages Hierarchy

Search NFA can search for more than one pattern simultaneously.
The number of patterns can be
finite -- this leads also to a dictionary automaton (we will meet it later)
or infinite -- this leads to a regular language.

Chomsky language hierarchy remainder

Grammar	Language	Automaton
Type-0	Recursively enumerable	Turing machine
Type-1	Context-sensitive	Linear-bounded non-deterministic Turing machine
Type-2	Context-free	Non-deterministic pushdown automaton
Type-3	Regular	Finite state automaton (NFA or DFA)

Only regular languages can be processed by NFA/DFA. More complex languages cannot. For example, any language containing *well-formed parentheses* is context-free and not regular and cannot be recognized by NFA/DFA.

Operations on regular languages

Let L_1 and L_2 be any languages. Then

$L_1 \cup L_2$ is **union** of L_1 and L_2. It is a set of all words which are in L_1 or in L_2.
$L_1.L_2$ is **concatenation** of L_1 and L_2. It is a set of all words w for which holds $w = w_1w_2$ (concatenation of words w_1 and w_2), where $w_1 \in L_1$ and $w_2 \in L_2$.
L_1^* is **Kleene star** or Kleene closure of language L_1. It is a set of all words which are concatenations of any number (incl. zero) of any words of L_1 in any order.

Closure property
Whenever L_1 and L_2 are regular languages
then $L_1 \cup L_2$, $L_1.L_2$, L_1^* are regular languages too.

Example $L_1 = \{001, 0001, 00001, ...\}$, $L_2 = \{110, 1110, 11110, ...\}$.

$L_1 \cup L_2 = \{001, 110, 0001, 1110, 0001, 1110, ...\}$
$L_1.L_2 = \{001110, 0011110, 00111110, ..., 0001110, 00011110, 000111110, ... \}$
$L_1^* = \{\varepsilon, 001, 001001, 001001001, ...\ 0010001, 00100010001, ...$
$..., 00100001, 001000001, ... \}$ // this one is not easy to list nicely... or is it?

Regular expressions defined recursively

Symbol ε is a regular expression.

Each symbol of alphabet Σ is a regular expression.

Whenever e_1 and e_2 are regular expressions then also strings

(e_1), e_1+e_2, e_1e_2, $(e_1)^*$ are regular expressions.

Languages represented by regular expressions (RE) defined recursively

RE ε represents language containing only empty string.

RE x, where $x \in \Sigma$, represents language {x}.

Let RE's e_1 and e_2 represent languages L_1 and L_2. Then

RE (e_1) represents L_1, RE e_1+e_2 represents $L_1 \cup L_2$,

REs e_1e_2, $e_1.e_2$ represent $L_1.L_2$, RE $(e_1)^*$ represents L_1^*.

Examples

$0+1(0+1)^*$ all integers in binary without leading 0's

$0.(0+1)^*1$ all finite binary fractions $\in$ (0, 1) without trailing 0's

((0+1)(0+1+2+3+4+5+6+7+8+9) + 2(0+1+2+3)):(0+1+2+3+4+5)(0+1+2+3+4+5+6+7+8+9)

all 1440 day's times in format hh:mm from 00:00 to 23:59

(mon+(wedne+t(ue+hur))s+fri+s(atur+un))day

English names of days in the week

$(1+2+3+4+5+6+7+8+9)(0+1+2+3+4+5+6+7+8+9)^*((2+7)5+(5+0)0)$

all decimal integers ≥ 100 divisible by 25

Convert regular expression to NFA

Input: Regular expression R containing *n* characters of the given alphabet.
Output: NFA recognizing language L(R) described by R.

Create start state S

```
for each k (1 ≤ k ≤ n) {
   assign index k  to the k-th character in R
     // this makes all characters in R unique: c[1], c[2], ..., c[n].
   create state S[k]          // S[k] corresponds directly to c[k]
}

for each k (1 ≤ k ≤ n) {
    if c[k] can be the first character in some string described by R
       then create transition S → S[k]  labeled by c[k] with index stripped off
    if c[k] can be the last character in some string described by R
       then mark S[k] as final state
    for  each p (1 ≤ p ≤ n)
       if (c[k] can follow immediately after c[p] in some string described by R)
         then create transition S[p] → S[k]  labeled by c[k] with index stripped off
}
```

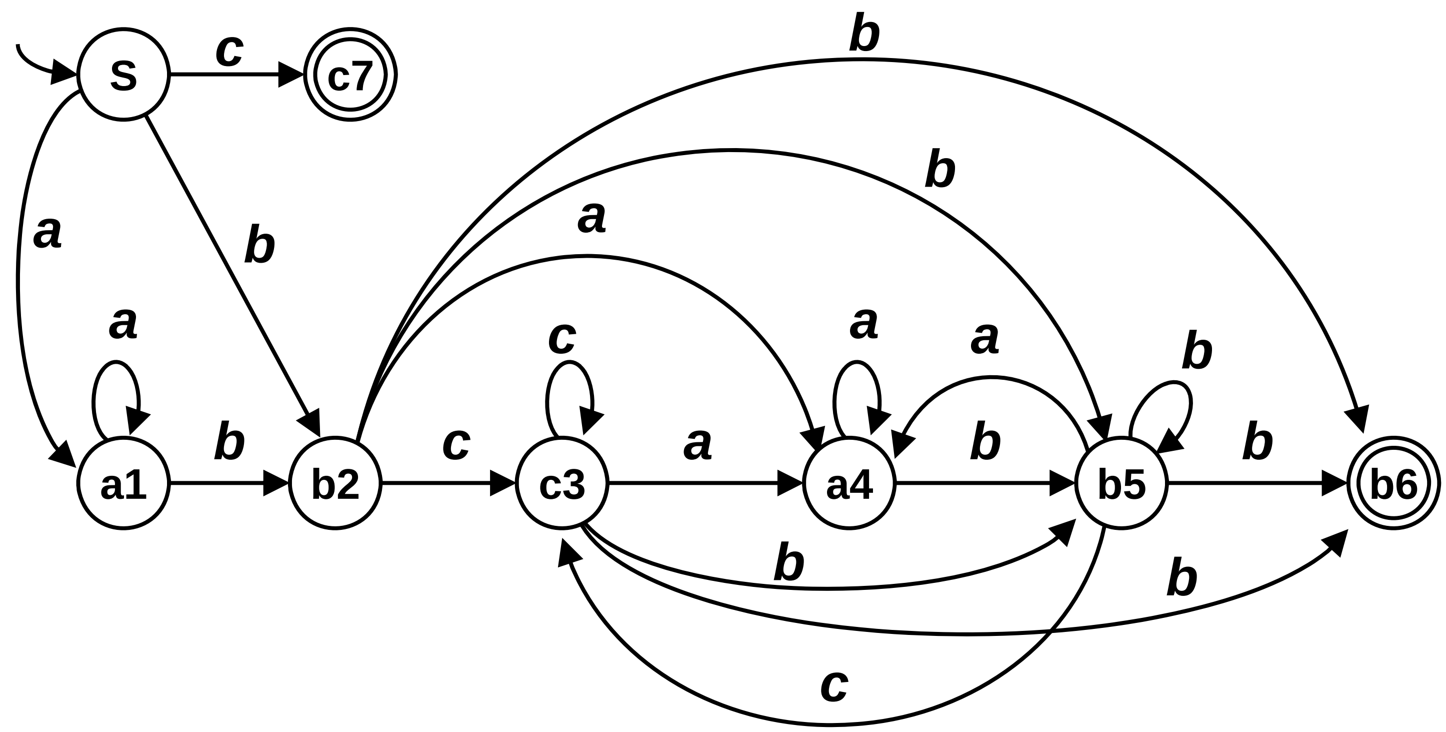
Regular expression

R = a*b(c + a*b)*b + c

Add indices:

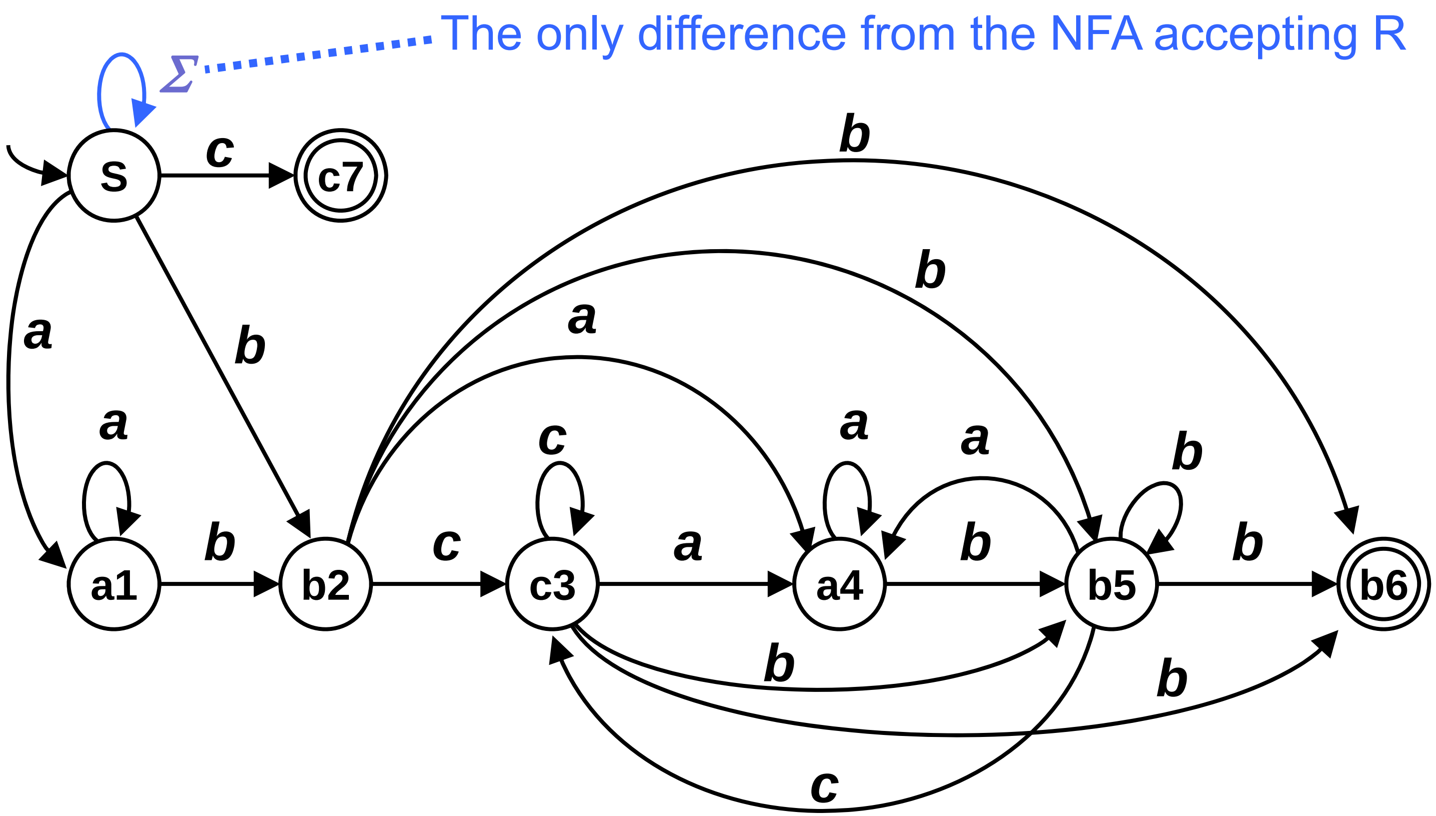
$R = a_1{}^*b_2(c_3 + a_4{}^*b_5)^*b_6 + c_7$

NFA accepts L(R)



NFA searches the text for any occurence of any word of L(R)

R = a*b (c + a*b)* b + c



Bonus

To find a subsequence representing a word $\in$ L(R), where R is a regular expression, do the following:

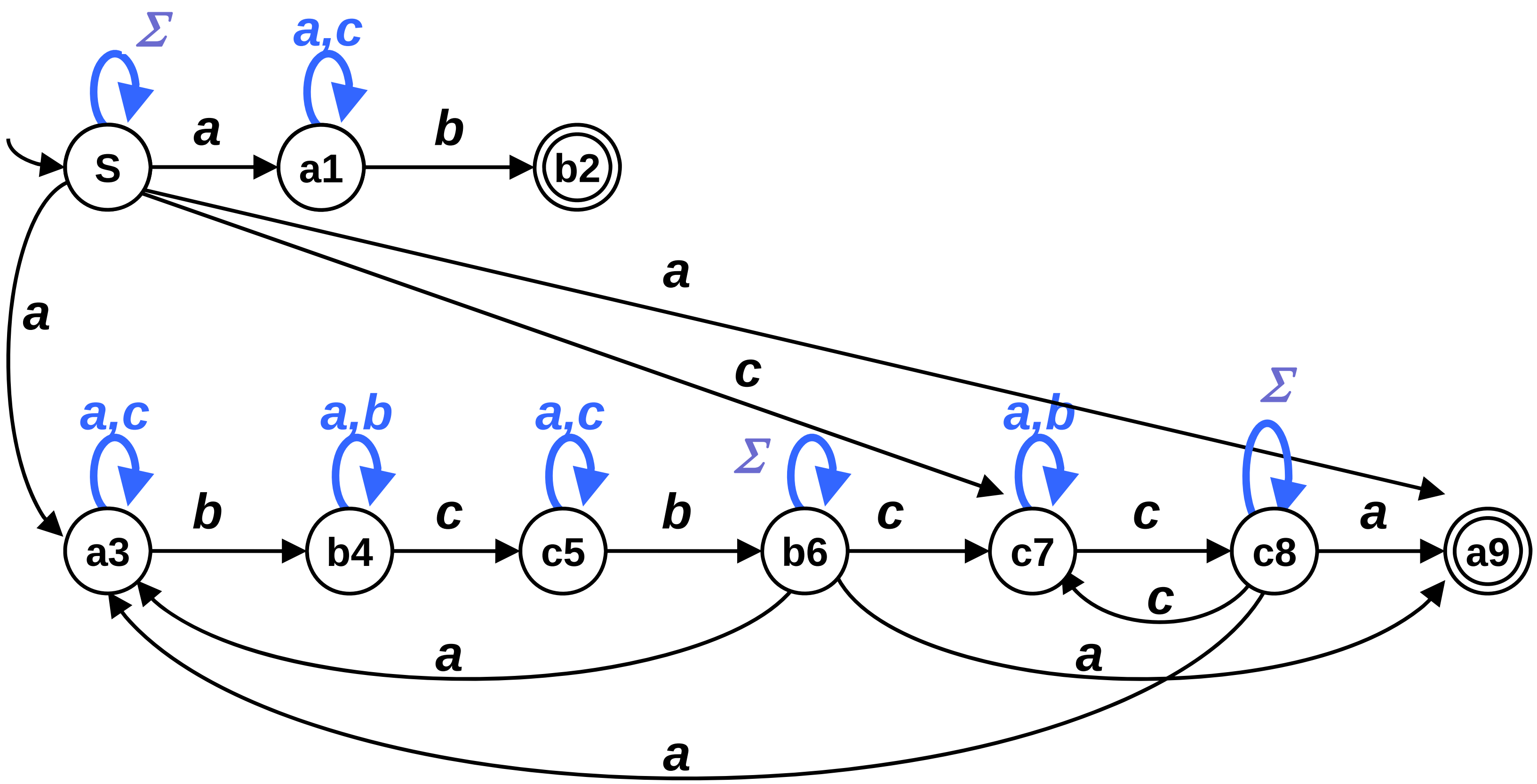
Create NFA acepting L(R)
Add self loops to the states of NFA:

1. Self loop labeled by Σ (whole alphabet) at the start state.
2. Self loop labeled $\Sigma - \{x\}$ at each state whose outgoing transition(s) are labeled by single x $\in$ Σ. // serves as an "optimized" wait loop
3. Self loop labeled by Σ at each state whose outgoing transition(s) are labeled by more than single symbol from Σ. // serves as an "usual" wait loop
4. No self loop to all other states. // which have no outgoing loop = final ones

Bonus

NFA searches the text for any occurence of any subsequence representing a word of L(R)

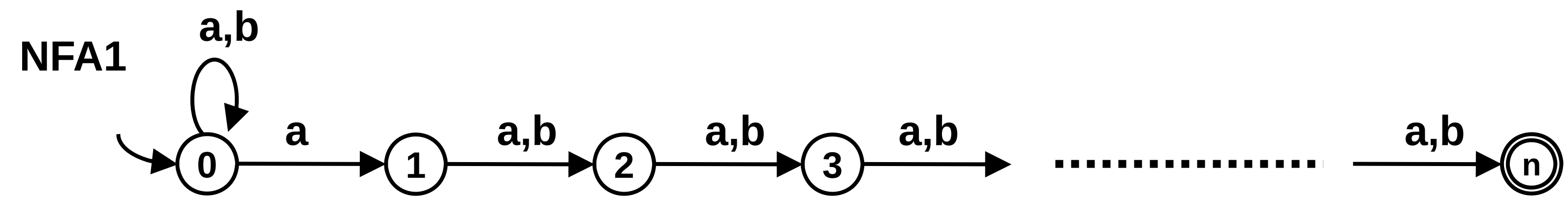
R = ab + (abcb + cc)* a



Transforming NFA which searches text for an occurence of a word of a given regular language into the equivalent DFA might take exponential space and thus also exponential time. Not always, but sometimes yes:

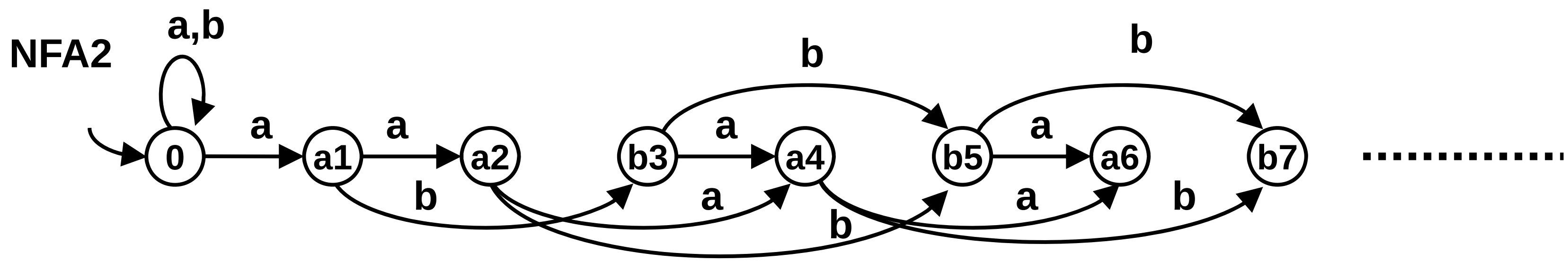
Consider regular expression **R = a(a+b)(a+b)...(a+b)** over alphabet {a, b}.

Text search NFA1 for R



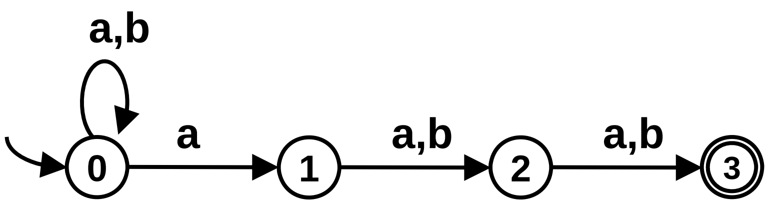
Mystery

Text search NFA2 for R, why not this one?



R = a(a+b)(a+b)

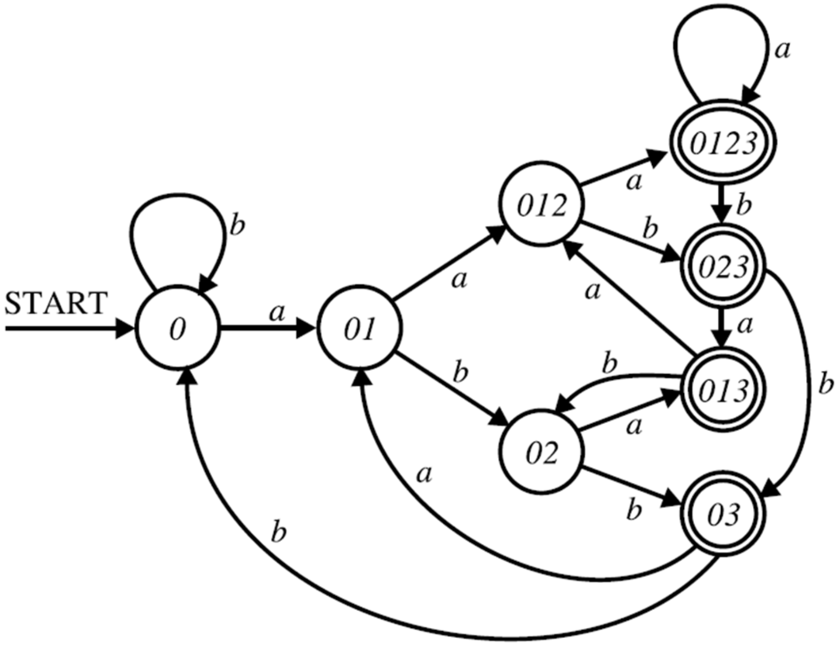
Text search NFA for R



NFA table

	a	b	
0	0,1	0	
1	2	2	
2	3	3	
3	-	-	F

Text search DFA for R



DFA table

	a	b	
0	01	0	
01	012	02	
012	0123	023	
0123	0123	023	F
02	013	03	
023	013	03	F
013	012	02	F
03	01	0	F

Search the text for more than just exact match

NFA with ε–transitions

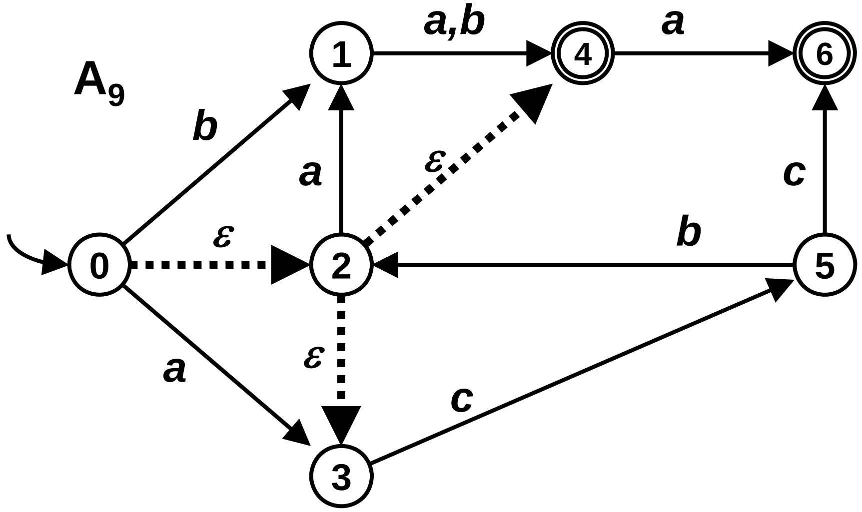
The transition from one state to another can be performed **without** reading any input symbol. Such transition is labeled by symbol ε.

ε–closure

Symbol ε–CLOSURE(p) denotes the union of $\{p\}$ and the set of all states q, which can be reached from state p using only ε–transitions

By definition, ε–CLOSURE(p) = $\{p\}$ when there is no ε–transition out from p.

ε–CLOSURE(0) = {0, 2, 3, 4}
ε–CLOSURE(1) = {1}
ε–CLOSURE(2) = {2, 3, 4}
ε–CLOSURE(3) = {3}
...

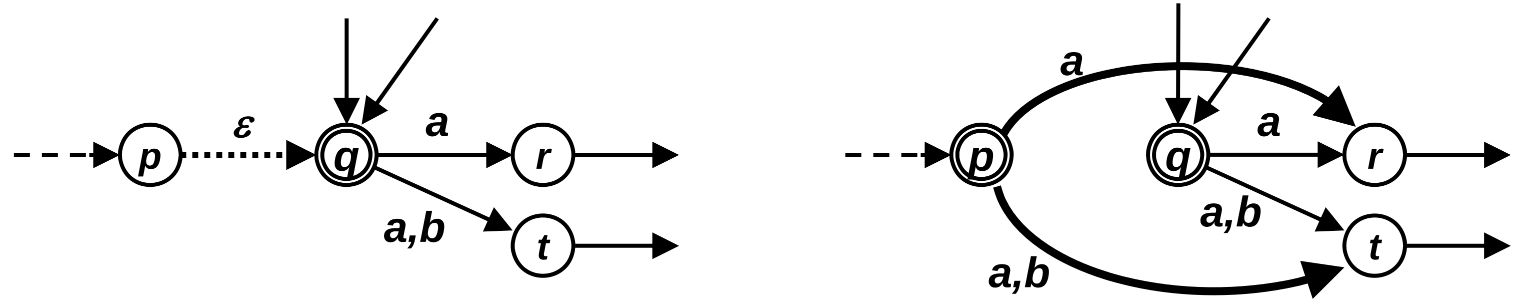


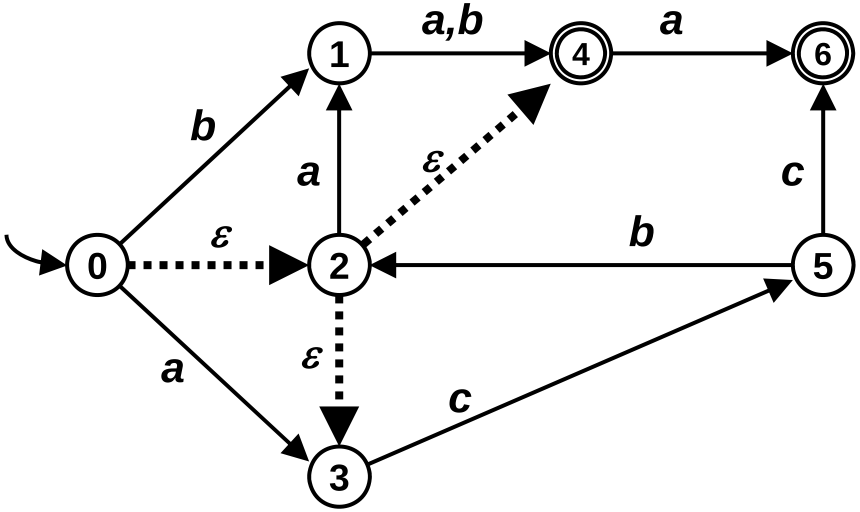
Construction of equivalent NFA without ε–transitions

Input: NFA A with some ε–transitions.
Output: NFA A' without ε–transitions.

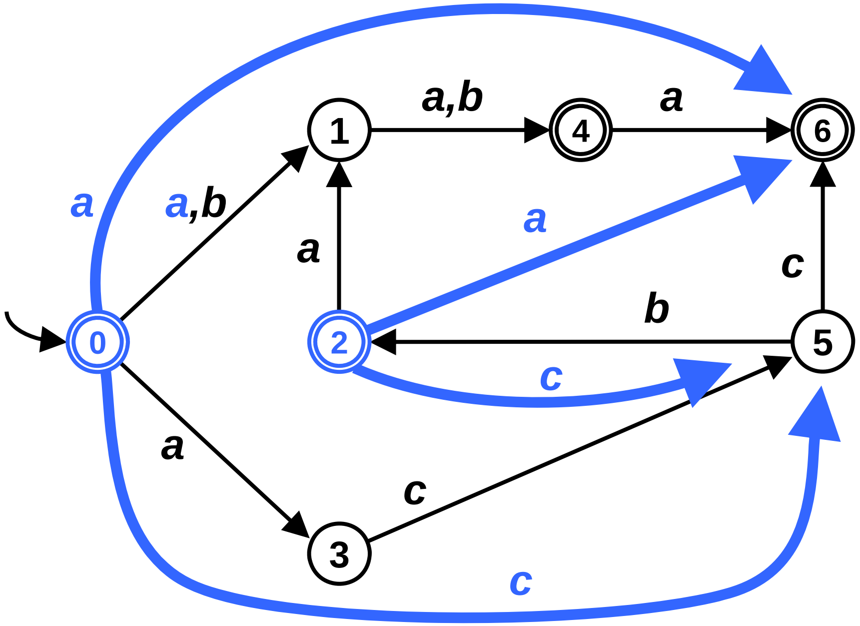
1. A' = exact copy of A.
2. Remove all ε–transitions from A'.
3. In A' for each (q, a) do:
   add to the set $\delta(p,a)$ all such states r for which it holds
   $q \in \varepsilon$–CLOSURE(p) and $\delta(q,a) = r$.
4. Add to the set of final states F in A' all states p for which it holds
   ε–CLOSURE$(p) \cap F \neq \emptyset$.

easy construction





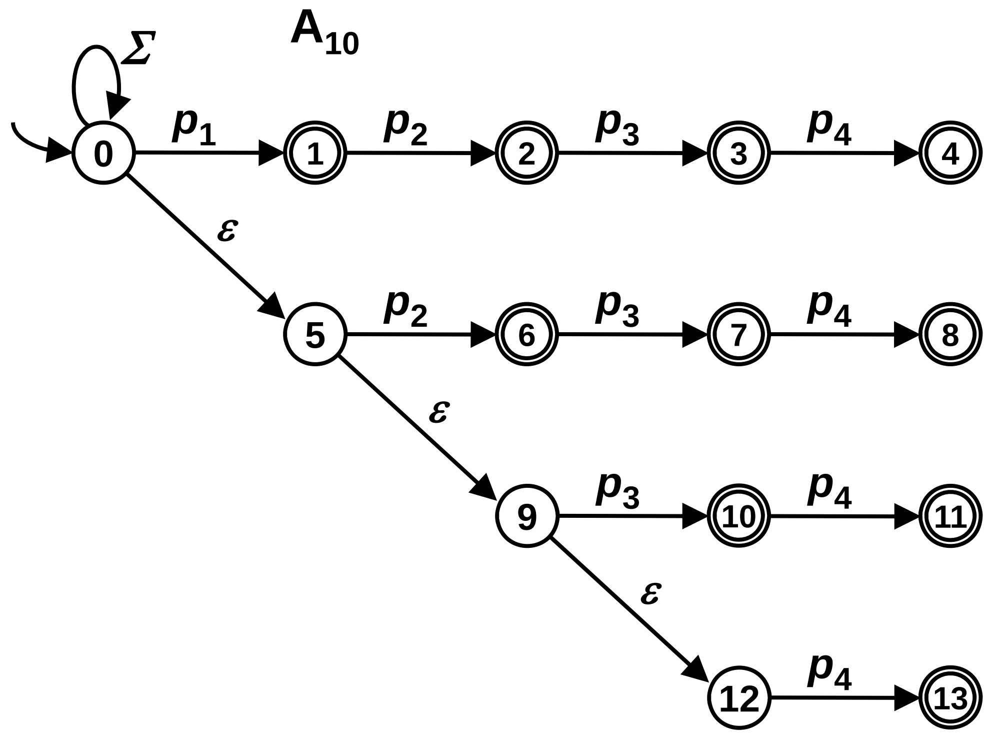
NFA with s ε–transitions



Equivalent NFA
without ε–transitions

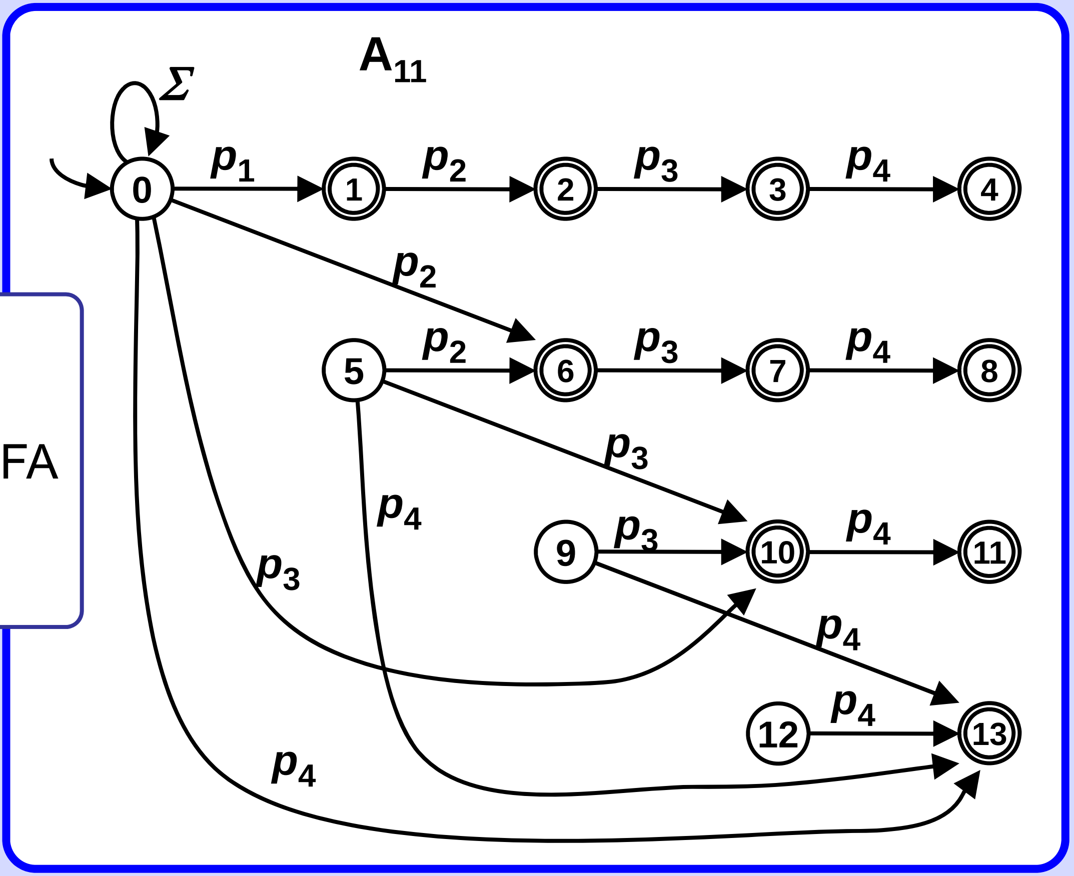
New transitions and accept states are highlighted

NFA for search for any unempty substring of pattern $p_1p_2p_3p_4$ over alphabet Σ.
Note the ε–transitions.



Powerful trick!

Union of two or more NFA:
Create additional start state S and add ε–transitions from S to the start states of all involved NFA's. Draw an example yourself!



States 5, 9, 12 are unreachable.
Transformation algorithm NFA -> DFA
if applied, will neglect them.

Equivalent NFA for search for any unempty substring of pattern $p_1p_2p_3p_4$
with ε–transitions removed.

A_{11}

	p_1	p_2	p_3	p_4	z	
0	0,1	0,6	0,10	0,13	0	
1		2			0	F
2			3		0	F
3				4	0	F
4					0	F
5		6	10	13	0	
6			7		0	F
7				8	0	F
8					0	F
9			10	13	0	
10				11	0	F
11					0	F
12				13	0	
13					0	F

	p_1	p_2	p_3	p_4	z	
0	0.1	0.6	0.10	0.13	0	
0.1	0.1	0.2.6	0.10	0.13	0	F
0.6	0.1	0.6	0.7.10	0.13	0	F
0.10	0.1	0.6	0.10	0.11.13	0	F
0.13	0.1	0.6	0.10	0.13	0	F
0.2.6	0.1	0.6	0.3.7.10	0.13	0	F
0.7.10	0.1	0.6	0.10	0.8.11.13	0	F
0.11.13	0.1	0.6	0.10	0.13	0	F
0.3.7.10	0.1	0.6	0.10	0.4.8.11.13	0	F
0.8.11.13	0.1	0.6	0.10	0.13	0	F
0.4.8.11.13	0.1	0.6	0.10	0.13	0	F

Transition table of NFA A_{11} (without ε–transitions).

Transition table of DFA which is equivalent to A_{11}.

DFA in this case has less states than the equivalent NFA.
Q: Does it hold for any automaton of this type? Proof?

Text search using NFA simulation without transform to DFA

Input: NFA , text in array t

```
SetOfStates S = eps_CLOSURE(q0), S_tmp;
int i = 1;
while ((i <= t.length) && (!S.empty())) {
  for (q in S)
    if (q.isFinal)                      // if( chi(S) == 1 )
      print(q.final_state_info);        // pattern found

  S_tmp = Set.empty();                  // transiton to next
  for (q in S)                          // set of states
    S_tmp.union(eps_CLOSURE(delta(q, t[i])));
  S = S_tmp;
  i++;                                  // next char in text
}

return S.containsFinalState();          // true or false
```